

### P-2165

# DETECTION AND REMOVAL OF CRACKS IN DIGITIZED PAINTING



#### A PROJECT REPORT

### Submitted by

BHARATHI KANNAN.K

71204205004

SELVA KUMAR.K.R

71204205047

**RAMALINGAM.S** 

71204205305

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**ANNA UNIVERSITY: CHENNAI 600025** 

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# ANNA UNIVERSITY: CHENNAI 600025

#### **BONAFIDE CERTIFICATE**

Certified that this report "DETECTION AND REMOVAL OF CRACKS IN DIGITIZED PAINTING" is the bonafide work of "Mr.BHARATHI KANNAN.K (71204205004), Mr. SELVA KUMAR.K.R (71204205047), Mr.RAMALINGAM.S (71204205305)" who carried out the project work under my supervision.

SIGNATURE

SIGNATURE

Dr. S. Thangasamy

Mr.E.A.Vimal

HEAD OF THE DEPARTMENT

SUPERVISOR, Lecturer

Computer science and Engineering

**Information Technology** 

Department of Computer Science & Engineering, Kumaraguru College of Technology, Coimbatore - 641006

Department of Information Technology, Kumaraguru College of Technology, Coimbatore - 641006

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Internal Examiner

External Examiner

#### DECLARATION

We hereby declare that the project entitled "DETECTION AND REMOVAL OF CRACKS IN DIGITIZED PAINTING" is done by us and to the best of our knowledge a similar work has not been submitted to the Anna University or any other Institution, for fulfillment of the requirement of the course study.

This report is submitted on the partial fulfillment of the requirement for all awards of the Degree of Bachelor of Information Technology of Anna University, Chennai.

Place: Coimbatore

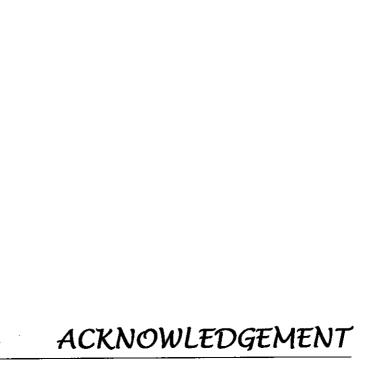
Date:

Bharathi Kannan.K

Selva Kumar.K.R

Mr.E.A.Vimal

Ramalingam.S



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#### **ABSTRACT**

An integrated methodology for the detection and removal of cracks on digitized paintings is implemented in this project. The cracks are detected by threshold the output of the morphological top-hat transformation. Afterwards the thin dark brush strokes which have been misidentified as cracks are removed using either a median radial basis function neural network on hue and saturation data or a semi-automatic procedure based on region growing. Finally, crack filling using order statistics filters or controlled anisotropic diffusion is performed. The methodology has been shown to perform very well on digitized paintings suffering from cracks.

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## 1. INTRODUCTION

#### **GENERAL**

Many paintings especially old ones suffer from breaks in the substrate, the paint or the varnish. These patterns are usually called cracks or craquelure and can be caused by aging, drying, and mechanical factors. Age cracks can result from non uniform contraction in the canvas or wood-panel support of the painting which stresses the layers of the painting. Drying cracks are usually caused by the evaporation of volatile paint components and the consequent shrinkage of the paint. Finally, mechanical cracks result from painting deformations due to external causes, e.g., vibrations and impacts.

The appearance of cracks on paintings deteriorates the perceived image quality. However, one can use digital image processing techniques to detect and eliminate the cracks on digitized paintings. Such a "virtual" restoration can provide clues to art historians, museum curators and the general public on how the painting would look like in its initial state, i.e., without the cracks. Furthermore, it can be used as a nondestructive tool for the planning of the actual restoration. A system that is capable of tracking and interpolating cracks. The user should manually select a point on each crack to be restored. A method for the detection of cracks using multioriented Gabor filters. Crack detection and removal bears certain

similarities with methods proposed for the detection and removal of scratches and other artifacts from motion picture films. However, such methods rely on information obtained over several adjacent frames for both artifact detection and filling. Thus they are not directly applicable in the case of painting cracks. Other research areas that are closely related to crack removal include image in painting which deals with the reconstruction of missing or damaged image areas by filling in information from the neighboring areas and disclosing, i.e., recovery of object parts that are hidden behind other objects within an image.

Methods developed in these areas assume that the regions where information has to be filled in are known. Different approaches for interpolating information in structured and textured image areas have been developed. The former are usually based on partial differential equations (PDEs) and on the calculus of variations whereas the latter rely on texture synthesis principles. A technique that decomposes the image to textured and structured areas and uses appropriate interpolation techniques depending on the area where the missing information. The results obtained by these techniques are very good. A methodology for the restoration of cracks on digitized paintings which adapts and integrates a number of image processing and analysis tool is proposed in this paper.

The methodology is an extension of the crack removal framework. The technique consists of the following stages:

- crack detection;
- Separation of the thin dark brush strokes, which have been misidentified as cracks;
- crack filling (interpolation).

A certain degree of user interaction most notably in the crack-detection stage is required for optimal results. User interaction is rather unavoidable since the large variations observed in the typology of cracks would lead any fully automatic algorithm to failure. However, all processing steps can be executed in real time and thus the user can instantly observe the effect of parameter tuning on the image under study and select in an intuitive way the values that achieve the optimal visual result. Needless to say, only subjective optimality criteria can be used in this case since no ground truth data are available. The opinion of restoration experts that inspected the virtually restored images were very positive. Two methods for the separation of the brush strokes which have been falsely identified as cracks. Methods for filling the cracks with image content from neighboring pixels.

#### PROBLEM DEFINITION

Many paintings especially old ones suffer from breaks in the substrate, the paint or the varnish. These patterns are usually called cracks or craquelure and can be caused by aging, drying, and mechanical factors. Age cracks can result from non uniform contraction in the canvas or wood-panel support of the painting which stresses the layers of the painting. Drying cracks are usually caused by the evaporation of volatile paint components and the consequent shrinkage of the paint. Finally, mechanical cracks result from painting deformations due to external causes, e.g., vibrations and impacts. The appearance of cracks on paintings deteriorates the perceived image quality.

- Problem for segmenting the lines and strokes of the under drawing.
- > Cracks not only disturb the appearance of a painting.
- ➤ One major goal of the project is to identify the drawing tools used by the painter to create the under drawing from the appearance of the strokes in the infrared reflectogram.



# 2. LITERATURE REVIEW

#### 2.1 FEASIBILITY STUDY

### 2.1.1 CURRENT STATUS OF THE PROBLEM

The existing methods for processing digital images are there which actually deal with enhancing the image picture quality, brightness, color etc. These factors can be degraded due to aging process. Such an image processing technique algorithm concentrates on improving those factor alone. There are not designed to analysis and improve in the cracks region. The cracks removal has to be rectified in the different manner. The principle applied to improve image color, brightness and other characteristic can not be used for crack detection and removal. This project concentrates on the digital image processing algorithm that deals only with crack detection and removal.

## 2.1.2 PROPOSED SYSTEM AND ADVANTAGES

The proposed system deals with digital image processing technique that detects and removes the cracks in the images. A system that is capable of tracking and interpolating cracks. The user should manually select a point on each crack to be restored. A method for the detection of cracks using multioriented Gabor filters. Crack detection and removal bears certain similarities with methods proposed for the detection and removal of scratches and other artifacts from motion picture films.

frames for both artifact detection and filling. Other research areas that are closely related to crack removal include image in painting which deals with the reconstruction of missing or damaged image areas by filling in information from the neighboring areas and disclosing. Methods developed in these areas assume that the regions where information has to be filled in are known. Different approaches for interpolating information in structured and textured image areas have been developed. The former are usually based on partial differential equations (PDEs) and on the calculus of variations whereas the latter rely on texture synthesis principles. A technique that decomposes the image to textured and structured areas and uses appropriate interpolation techniques depending on the area where the missing information. A methodology for the restoration of cracks on digitized paintings which adapts and integrates a number of image processing and analysis tool is proposed in this paper. The technique consists of the following stages:

- There should be some method through which crack area in the digital image can be detection;
- Separation of the thin dark brush strokes which have been misidentified as cracks;
- Crack filling (interpolation).

A certain degree of user interaction most notably in the

# 2.2 HARDWARE REQUIREMENTS: (Minimum Requirements)

Processor : Intel Processor IV

RAM : 256 MB

Hard disk : 40 GB

CD drive : 40 x Samsung

Floppy drive : 1.44 MB

Monitor : 15" Samtron color

Keyboard : 108 mercury keyboard

Mouse : Logitech mouse

## 2.3 SOFTWARE REQUIREMENTS:

Operating System – Windows XP/2000

Language used - VB .Net

### 2.4 SOFTWARE OVERVIEW

Microsoft Visual Basic .Net used as front end tool.

The reason for selecting Visual Basic dot Net as front end tool as follows:

- Visual Basic .Net has flexibility, allowing one or more language to interoperate to provide the solution. This Cross Language Compatibility allows to do project at faster rate.
- Visual Basic .Net has Common Language Runtime, that allows the entire component to converge into one intermediate format and then can interact.
- Visual Basic .Net has provided excellent security when your application is executed in the system.
- Visual Basic .Net has flexibility, allowing us to configure the
  working environment to best suit our individual style. We can
  choose between a single and multiple document interfaces, and
  we can adjust the size and positioning of the various IDE
  elements.
- Visual Basic .Net has Intelligence feature that make the coding easy and also dynamic help provides very less coding time.
- The working environment in Visual Basic .Net is often referred to as IDE because it integrates many different functions such as design, editing, compiling and debugging within a common

- environment. In most traditional development tools each of separate programs with its own interface.
- The Visual Basic .Net language is quite powerful if we can imagine a programming task and accomplished using Visual Basic .Net.
- After creating a Visual Basic .Net application, if we want to
  distribute it to others we can freely distribute any application to
  anyone who uses windows. We can distribute our applications
  on disk, CDs, across networks, over an intranet or the internet.
- Toolbars provide quick access to commonly used commands in the programming environment. We click a button on the toolbar once to carry out the action represented by that button.
   Additional toolbars for editing, form design and debugging can be toggled on or off from the toolbars command on view menu.
- Many parts of Visual Basic are context sensitive. Context sensitive means we can get help on these parts directly without having to go through the help menu.
- Visual Basic interprets our code as we enter it, catching and highlighting most syntax or spelling errors on the fly. It's almost like having an expert watching over our shoulder as we enter our code.

# 3. DETAILS OF THE METHODOLOGY EMPLOYED

#### 3.1 DETECTION OF CRACKS

Cracks usually have low luminance and can be considered as local intensity minima with rather elongated structural characteristics. Therefore, a crack detector can be applied on the luminance component of an image and should be able to identify such minima. A crack-detection procedure top-hat transform is proposed in this paper. The top-hat transform is a grayscale morphological filter defined as follows:

$$Y(x) = f(x) - f_{nB}(x)$$
 (1)

Where  $f_{nB}(x)$  is the opening of the function f(x) with the structuring set, defined as

$$nB = B \Phi B \Phi \dots \Phi B \text{ (n times)}$$
 (2)

In the previous equation,  $\Phi$  denotes the dilation operation. A square or a circle can be used as structuring element B. The final structuring set nB is evaluated only once using in the opening operation of (1). The opening f nB of a function is a low-pass nonlinear filters that erases all peaks (local maxima) in which the structuring element nB cannot fit. Thus, the image f –  $f_{nB}$  contains only those peaks and no background at all. Since cracks are local minima rather than local maxima, the top-hat transform should be applied on the negated luminance image. Alternatively, one can detect cracks by performing closing on the original image f(x) with the structuring

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$$Y(x) = f^{nB}(x) - f(x)$$
 ----- (3)

It can be easily shown that the result of (3) is identical to that of applying (1) on the negated image. Use of (3) does not require negation of f(x) which grands it a small but not negligible computational advantage over (1).

In situations where the crack-like artifacts are of high luminance, as in the case of scratches on photographs, negation of the luminance component prior to the crack detection is not required, i.e., the crack detection procedure can be applied directly on the luminance image. The user can control the result of the crack-detection procedure by choosing appropriate values for the following parameters:

- o The type of the structuring element B,
- The size of the structuring element B and the number n of dilations.

These parameters affect the size of the "final" structuring element nB and must be chosen according to the thickness of the cracks to be detected. It should be noted that these parameters are not very critical for the algorithm performance due to the threshold operation and also due to the existence of the brush-stroke/crack separation procedure, which is able to remove crack-like brush strokes that have been erroneously identified as cracks. The fact that all the results presented in this paper have been

. . . .

indication that the above statement is indeed true. These parameters were the following:

- Structuring element type: square;
- Structuring element size: 3 X 3;
- Number n of dilations in (2): 2.

The top-hat transform generates a grayscale output image t (k, l) where pixels with a large grey value are potential crack or crack-like elements. Therefore, a threshold operation on t (k, l) is required to separate cracks from the rest of the image. The threshold can be chosen by a trial and error procedure, i.e., by inspecting its effect on the resulting crack map. The low computational complexity of the threshold operation enables the user to view the crack-detection results in real time while changing the threshold value, e.g., by moving a slider. This fact makes interactive threshold selection very effective and intuitive. Alternatively, threshold selection can be done by inspecting the histogram of for a lobe close to the maximum intensity value and assigning it a value that separates this lobe from the rest of the intensities. The result of the threshold is a binary image marking the possible crack locations. Instead of this global thersholding technique more complex threshold schemes, which use a spatially varying threshold can be used. Obviously, as the threshold value increases the number of image pixels that are identified as cracks decreases. Thus, certain cracks, especially in can remain undetected. In principle, it is more preferable to select the threshold so that some cracks remain undetected than to choose a threshold that would result in the detection of all cracks but will also falsely identify as cracks and subsequently modify other image structures. The threshold (binary) output of the top-hat transform on the luminance component of an image containing cracks.

# 3.2 SEPARATION OF THE BRUSH STROKES FROM THE

#### **CRACKS**

In some paintings, certain areas exist where brush strokes have almost the same thickness and luminance features as cracks. The hair of a person in a portrait could be such an area. Therefore, the top-hat transform might misclassify these dark brush strokes as cracks. Thus, in order to avoid any undesirable alterations to the original image, it is very important to separate these brush strokes from the actual cracks, before the implementation of the crack filling procedure. Two methods to achieve this goal are described in the following subsections.

A simple interactive approach for the separation of cracks from brush strokes is to apply a region growing algorithm on the threshold output of the top-hat transform, starting from pixels (seeds) on the actual cracks. The pixels are chosen by the user in an interactive mode. At least one seed per connected crack element should be chosen. Alternatively,

more convenient. The growth mechanism that was used implements the well-known grassfire algorithm that checks recursively for unclassified pixels with value 1 in the 8-neighborhood of each crack pixel. At the end of this procedure, the pixels in the binary image, which correspond to brush strokes that are not 8-connected to cracks will be removed. The above procedure can be used either in a stand-alone mode or applied on the output of the MRBF separation procedure described in the next section to eliminate any remaining brush strokes.

In our implementation, a MRBF network with two outputs was used. The first output represents the class of cracks while the second one the class of brush strokes. Input vectors were two-dimensional and consisted of the hue and saturation values of pixels identified as cracks by the top-hat transform. The number of clusters (hidden units) chosen for each class depends on the overlap between the populations of cracks and brush strokes. If there is a substantial overlap, the number should be increased, in order to reduce the classification error. In our implementation three hidden units have been incorporated. Training was carried out by presenting the network with hue and saturation values for pixels corresponding to cracks and crack-like brushstrokes. Data from 24 digitized portable religious icons from the Byzantine era were used for this purpose. The system trained using this specific training set can be considered to be might result in somewhat suboptimal results. However, appropriately selected training sets can be used to train the system to separate cracks from brush strokes on paintings of different artistic styles or content. In order to select pixels corresponding to cracks and crack-like brush strokes the crack detection algorithm presented was applied on these images. Results were subsequently post processed by an expert using the semi-automatic approach.

The aim of this post processing step was twofold: to remove pixels that are neither cracks nor crack-like brush strokes and to separate cracks and crack-like brush strokes for the supervised step of the training procedure. In this supervised training step, the network was presented with these labeled inputs, i.e., pairs of hue-saturation values that corresponded to image pixels that have been identified as belonging to cracks and crack-like brush strokes. After the training session, the MRBF neural network was able to classify pixels identified as cracks by the top-hat transform to cracks or brush strokes. The trained network has been tested on 12 images from the training set and 15 images (of the same artistic style and era) that did not belong to the training set. Naturally, the performance of the cracks/brush-stroke separation procedure was judged only in a subjective manner (i.e., by visual inspection of the results), as ground truth data (i.e., brush stroke-free crack images) are not available. For this reason, two

after the application of the separation system and concluded that in the processed crack images the great majority of the brush strokes have been removed. A threshold top-hat transforms output containing many brush strokes. A great part of these brush strokes is separated by the MRFB

## 3.3 CRACK-FILLING METHODS

After identifying cracks and separating misclassified brush strokes, the final task is to restore the image using local image information to fill (interpolate) the cracks. Two classes of techniques, utilizing order statistics filtering and anisotropic diffusion are proposed for this purpose. Both are implemented on each RGB channel independently and affect only those pixels which belong to cracks. Therefore, provided that the identified crack pixels are indeed crack pixels, the filling procedure does not affect the "useful" content of the image. Image in painting techniques can also be used for crack filling.

The performance of the crack filling methods presented below was judged by visual inspection of the results. Obviously, measuring the performance of these methods in an objective way is infeasible since ground truth data are not available. For the evaluation of the results, two restoration experts were asked to inspect several images restored using the various methods and comment based on their experience and quality of the filling results, whether the color used for filling was the correct one, whether

# 4. PERFORMANCE EVALUATION

Testing is a critical element of software quality and assurance and represents the ultimate review of specification design and coding. It is a vital activity that has to be enforced in the development of any system. This could be done in parallel during all the phases of system development. The feedback received from these texts can be used for further enhancement of the system under consideration. The testing phase conducts test using the Software Requirement Specification as a reference and with the goal to see whether system satisfies the specified requirements.

Standard procedures have been followed in testing our system. Test cases are generated for each screen. These test cases will cover every possibility which could result in both positive and negative results. These test plans are maintained for any further testing done on the system.

- > Software Testing
- > Functional Testing
- > System Testing

## 4.1 Software Testing:

Software Testing is the process of confirming the functionality and correctness of software by running it. Software testing is usually performed for one of two reasons:

1) Defect detection

The problem of applying software testing to defect detection is that software can only suggest the presence of flaws, not their absence (unless the testing is exhaustive). The problem of applying software testing to reliability estimation is that the input distribution used for selecting test cases may be flawed. It is common place to attempt to test as many of the syntactic features of the code as possible (within some set of resource constraints) are called *white box* software testing technique. Techniques that do not consider the code's structure when test cases are selected are called *black box technique*.

# 4.2 Functional Testing:

Functional testing is a testing process that is black box in nature. It is aimed at examine the overall functionality of the product. It usually includes testing of all the interfaces and should therefore involve the clients in the process.

#### 4.3 System Testing:

System Testing should be the final stage of the testing process. This type of test involves examination of the whole computer system, all the software components, all the hard ware components and any interfaces.

The whole computer based system is checked not only for validity but also to meet the objectives.

# 5. CONCLUSION

In this paper, we have presented an integrated strategy for crack detection and filling in digitized paintings. Cracks are detected by using top-hat transform, whereas the thin dark brush strokes, which are misidentified as cracks, are separated either by an automatic technique (MRBF networks) or by a semi-automatic approach. Crack interpolation is performed by appropriately modified order statistics filters or controlled anisotropic diffusion. The methodology has been applied for the virtual restoration of images and was found very effective by restoration experts.

However, there are certain aspects of the proposed methodology that can be further improved. For example, the crack-detection stage is not very efficient in detecting cracks located on very dark image areas, since in these areas the intensity of crack pixels is very close to the intensity of the surrounding region. A possible solution to this shortcoming would be to apply the crack-detection algorithm locally on this area and select a low threshold value.

Another situation where the system (more particularly, the crack filling stage) does not perform as efficiently as expected is in the case of cracks that cross the border between regions of different color. In such situations, it might be the case that part of the crack in one area is filled with color from the other area, resulting in small spurs of color in the border

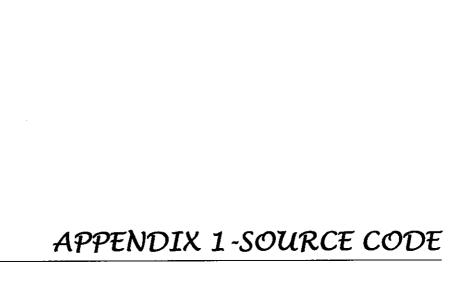
between the two regions. However, this phenomenon is rather seldom and furthermore, the extent of these erroneously filled areas is very small (2–3 pixels maximum). A possible solution would be to perform edge detection or segmentation on the image and confine the filling of cracks that cross edges or region borders to pixels from the corresponding region.



# **6. FUTURE ENHANCEMENT**

This project can be enhanced by

- > Applying these algorithms to colored paintings.
- ➤ Instead of PGM format files, it can be implemented in other files like JPEG, BMP, etc.,
- ➤ Perfect crack detection can be performed automatically without selecting a particular area.



## 7. APPENDIX

#### 7.1 SAMPLE CODE:

```
Public Class frmMDIMain
    Inherits System. Windows. Forms. Form
Dim InputFilePath As String = ""
Private Sub mnuImageOpenInputImage Click(ByVal sender As
System.Object, ByVal e As System. EventArgs) Handles
mnuImageOpenInputImage.Click
        openDialog1.Filter = "PGM Images (*.pqm) | *.pqm"
        openDialog1.FileName = Application.StartupPath +
                           "\images\in.pgm"
        If openDialog1.ShowDialog() =
                  Windows.Forms.DialogResult.OK Then
            InputFilePath = openDialog1.FileName
            StatusBar1.Panels(0).Text = "InputFilePath: " +
                                          InputFilePath
            AddImage(openDialog1.FileName)
        End If
End Sub
Private Sub mnuImageOpenImage Click(ByVal sender As
System.Object, ByVal e As System.EventArgs) Handles
mnuImageOpenImage.Click
        openDialog1.Filter = "PGM Images (*.pgm)|*.pgm"
        openDialog1.FileName = Application.StartupPath +
                               "\images\in.pgm"
        If openDialog1.ShowDialog() =
                   Windows.Forms.DialogResult.OK Then
            AddImage(openDialog1.FileName)
        End If
End Sub
Private Sub mnuCrackDetectionTophatTransform Click(ByVal
sender As System. Object, ByVal e As System. EventArgs)
Handles mnuCrackDetectionTophatTransform.Click
        If InputFilePath <> "" Then
            Dim tCrackDetection As New CrackDetection
           tCrackDetection.setInFilePath(InputFilePath)
       tCrackDetection.setOutFilePath("out 3 tophat.pgm")
            tCrackDetection.TopHatTransform()
            TophatFinished = True
      Call MsgBox("Tophat Transform, Finished.",
   MsgBoxStyle.Information Or MsgBoxStyle.OkOnly, strTitle)
        End If
End Sub
```

```
Private Sub mnuCrackDetectionThreshold Click(ByVal sender
As System. Object, ByVal e As System. EventArgs) Handles
mnuCrackDetectionThreshold.Click
        If TophatFinished = True Then
            Dim tfrmThreshold As New frmThreshold
            tfrmThreshold.MdiParent = tfrmMDIMain
            tfrmThreshold.Show()
        End If
End Sub
Private Sub mnuCrackRemovalOrderStatisticsFilter Click
(ByVal sender As System.Object, ByVal e As
System.EventArgs) Handles
mnuCrackRemovalOrderStatisticsFilter.Click
        ThresholdFinished = True
        If ThresholdFinished = True Then
            Dim tCrackRemoval As New CrackRemoval
            tCrackRemoval.setInFilePath(InputFilePath)
            tCrackRemoval.setOutFilePath("t.pgm")
            tCrackRemoval.ModifiedTrimmedMeanFilter(20)
            tCrackRemoval.setInFilePath("t.pgm")
          tCrackRemoval.setOutFilePath("out 6 removed.pgm")
            tCrackRemoval.RecursiveMeanFilter(5)
            Kill("t.pgm")
            Call MsgBox("Crack Removal, Finished.",
MsqBoxStyle.Information Or MsqBoxStyle.OkOnly, strTitle)
        End If
End Sub
Private Sub
mnuThinBrushStrokesRemovalRemoveThinBrushStrokes Click
(ByVal sender As System.Object, ByVal e As
System. EventArgs) Handles
mnuThinBrushStrokesRemovalRemoveThinBrushStrokes.Click
        'stop roi
        ROICaptureStarted = False
        StatusBar1.Panels(1).Text = ""
        'call grassfire algorithm
        If ThresholdFinished = True Then
            Dim tCrackDetection As New CrackDetection
tCrackDetection.setInFilePath("out 4 threshold.pgm")
tCrackDetection.setOutFilePath("out 5 cracks.pgm")
            tCrackDetection.GrassFire()
            RemoveThinBrushStrokesFinished = True
            Call MsgBox("RemoveThinBrushStrokes,
Finished.", MsgBoxStyle.Information Or MsgBoxStyle.OkOnly,
strTitle)
        End If
```

End Sub

#### Module modCrackDetection

```
Module modCrackDetection
Public Class CrackDetection
 Dim InFilePath As String, OutFilePath As String
   'constructor
     Public Sub New()
      InFilePath = ""
      OutFilePath = ""
End Sub
Public Function EdgeDetection(ByVal tIntensityDifference As
Integer) As PGM
 Dim imgIn As PGM = New PGM
 Dim imgOut As PGM = New PGM
 Dim r As Integer, c As Integer, inval As Integer,
     outval As Integer
     'read input image
     imgIn.setFilePath(InFilePath)
     imgIn.readImage()
     'set output-image header
     imgOut.setFilePath(OutFilePath)
     imgOut.setMagicString("P5")
     imgOut.setComment("#edge image")
     imgOut.setDimension(imgIn.getCols(),
                                 imaIn.getRows())
     imgOut.setMaxGray(imgIn.getMaxGray())
     'edgefinding algorithm
     For r = 0 To imgOut.getRows() - 1
      For c = 0 To imgOut.getCols() - 1
       inval = imgIn.getPixel(r, c) 'qet current pixel
       Dim tinval(2) As Integer
       Dim fval As Boolean
       Dim flag1 As Boolean, flag2 As Boolean
       tinval(0) = imgIn.getPixel(r, c + 1)'get right pixel
       tinval(1) = imgIn.getPixel(r + 1, c)'get down pixel
       flag1 = IIf(Math.Abs(inval - tinval(0)) >
                          tIntensityDifference, True, False)
       flag2 = IIf(Math.Abs(inval - tinval(1)) >
                          tIntensityDifference, True, False)
       fval = flag1 Or flag2
       outval = IIf(fval = True, 0, 255)
       imgOut.setPixel(r, c, outval)
      Next
     Next
       'write output image
      imgOut.writeImage()
      Return (imgOut)
```

```
'mean filter algorithm (low-pass filter)
Public Function MeanFilter(ByVal tIterations As Integer) As
PGM
      Dim imgIn As PGM = New PGM
      Dim imgOut As PGM = New PGM
      Dim r As Integer, c As Integer
      Dim inval As Integer, outval As Integer
       'read input image
        imgIn.setFilePath(InFilePath)
        imgIn.readImage()
        'set output-image header
        imgOut.setFilePath(OutFilePath)
        imgOut.setMagicString("P5")
        imgOut.setComment("#smoothed image")
        imgOut.setDimension(imgIn.getCols(),
                            imgIn.getRows())
        imgOut.setMaxGray(imgIn.getMaxGray())
        'smoothing algorithm (mean)
        Dim t As Integer
        For t = 1 To tIterations
         For r = 0 To imgOut.getRows() - 1
          For c = 0 To imgOut.getCols() - 1
           inval = imgIn.getPixel(r, c) 'get current pixel
           'get neighbourhood pixel intensity values
           Dim neighbour(8) As Integer
           neighbour(0) = imqIn.getNeighbor(r, c,
                                             Directions.NW)
           neighbour(1) = imgIn.getNeighbor(r, c,
                                             Directions.W)
           neighbour(2) = imgIn.getNeighbor(r, c,
                                             Directions.SW)
           neighbour(3) = imqIn.getNeighbor(r, c,
                                             Directions.S)
           neighbour(4) = imqIn.getNeighbor(r, c,
                                             Directions.SE)
           neighbour(5) = imgIn.getNeighbor(r, c,
                                             Directions.E)
           neighbour(6) = imgIn.getNeighbor(r, c,
                                             Directions.NE)
           neighbour(7) = imgIn.getNeighbor(r, c,
                                             Directions.N)
           'calculate new intensity value
           Dim tsum As Integer = inval
           Dim k As Integer
           For k = 0 To 7
            tsum = tsum + neighbour(k) 'calc sum
            outval = tsum / 9 'calc mean
```

imgOut.setPixel(r, c, outval)

```
Next
```

```
'set outputimage as input to next iteration (if not last
iteration)
            If t <> tIterations Then
             Dim r1 As Integer
             For r1 = 0 To imgIn.getRows() - 1
              For c = 0 To imgIn.getCols() - 1
               imgIn.setPixel(r1, c, imgOut.getPixel(r1, c))
              Next
             Next
            End If
            Next
           'write output image
            imgOut.writeImage()
            Return (imgOut)
End Function
 'thresholding
 Public Function Thresholding (ByVal tIntensityThreshold As
 Integer) As PGM
   Dim imgIn As PGM = New PGM
   Dim imqOut As PGM = New PGM
   Dim r As Integer, c As Integer, inval As Integer,
       outval As Integer
   'read input image
   imgIn.setFilePath(InFilePath)
   imgIn.readImage()
   'set output-image header
   imgOut.setFilePath(OutFilePath)
   imgOut.setMagicString("P5")
   imgOut.setComment("#thresholded image")
   imgOut.setDimension(imgIn.getCols(), imgIn.getRows())
   imgOut.setMaxGray(imgIn.getMaxGray())
   'binary thresholding algorithm
    For r = 0 To imgOut.getRows() - 1
     For c = 0 To imgOut.getCols() - 1
      inval = imgIn.getPixel(r, c) 'get current pixel
      outval = IIf(inval >= tintensityThreshold, 0, 255)
      imgOut.setPixel(r, c, outval)
     Next
    Next
          'write output image
          imgOut.writeImage()
          Return (imgOut)
 End Function
'erosion
 Public Function TopHatTransform() As PGM
   Dim imgIn As PGM = New PGM
```

```
Dim imgDilation As PGM = New PGM
 Dim imgTophat As PGM = New PGM
 Dim r As Integer, c As Integer
 Dim inval As Integer, outval As Integer
  'read input image
   imgIn.setFilePath(InFilePath)
   imgIn.readImage()
  'set erosion-image header
   imgErosion.setFilePath("out 1 erosion.pgm")
   imgErosion.setMagicString("P5")
   imgErosion.setComment("#eroded image")
   imgErosion.setDimension(imgIn.getCols(),
                            imgIn.getRows())
   imgErosion.setMaxGray(imgIn.getMaxGray())
  'set dilation-image header
   imgDilation.setFilePath("out 2 dilation.pgm")
   imgDilation.setMagicString("P5")
   imgDilation.setComment("#dilated image")
   imgDilation.setDimension(imgIn.getCols(),
                             imgIn.getRows())
   imqDilation.setMaxGray(imgIn.getMaxGray())
  'set tophat-image header
   imgTophat.setFilePath(OutFilePath)
   imgTophat.setMagicString("P5")
   imgTophat.setComment("#tophat-transformed image")
   imgTophat.setDimension(imgIn.getCols(),
                           imgIn.getRows())
   imgTophat.setMaxGray(imgIn.getMaxGray())
   'erosion algorithm
   For r = 0 To imgErosion.getRows() - 1
    For c = 0 To imgErosion.getCols() - 1
     inval = imgIn.getPixel(r, c)
     'get neighborhood pixel intensity values
     Dim neighbor(8) As Integer
     neighbor(0) = imgIn.getNeighbor(r, c, Directions.NW)
     neighbor(1) = imgIn.getNeighbor(r, c, Directions.W)
     neighbor(2) = imqIn.getNeighbor(r, c, Directions.SW)
     neighbor(3) = imgIn.getNeighbor(r, c, Directions.S)
     neighbor(4) = imgIn.getNeighbor(r, c, Directions.SE)
     neighbor(5) = imgIn.getNeighbor(r, c, Directions.E)
     neighbor(6) = imgIn.getNeighbor(r, c, Directions.NE)
     neighbor(7) = imqIn.getNeighbor(r, c, Directions.N)
     Dim flag As Boolean = True, t As Integer
     For t = 0 To 7
      If Math.Abs(neighbor(t) - inval) > 5 Then
       flag = False
      Exit For
      End If
     Next
      outval = IIf(flag, inval, 255)
```

```
Next
    Next
   'dilation algorithm (grayscale opening)
    For r = 0 To imgErosion.getRows() - 1
     For c = 0 To imgErosion.getCols() - 1
      inval = imgErosion.getPixel(r, c)
      imgDilation.setPixel(r - 1, c - 1, inval)
      imgDilation.setPixel(r - 1, c, inval)
      imgDilation.setPixel(r - 1, c + 1, inval)
      imgDilation.setPixel(r, c - 1, inval)
      imgDilation.setPixel(r, c, inval)
      imgDilation.setPixel(r, c + 1, inval)
      imgDilation.setPixel(r + 1, c - 1, inval)
      imgDilation.setPixel(r + 1, c, inval)
       imgDilation.setPixel(r + 1, c + 1, inval)
     Next
    Next
  'tophat transform (originalImage - grayscaleOpenedImage)
  Dim invall As Integer
  For r = 0 To imgIn.getRows() - 1
   For c = 0 To imgIn.getCols() - 1
     inval = imgIn.qetPixel(r, c)'pixel from originalImage
    inval1 = imgDilation.getPixel(r, c) 'pixel from
                                       grayscaleOpenedImage
    outval = Math.Abs(inval - inval1)
     imgTophat.setPixel(r, c, outval)
   Next
  Next
    imgErosion.writeImage()
    imgDilation.writeImage()
    imgTophat.writeImage()
   Return (imgErosion)
   Return (imgDilation)
    Return (imgTophat)
End Function
'grassfire algorithm (removal of thin brush strokes)
Public Function GrassFire() As PGM
  Dim imgIn As PGM = New PGM
  Dim imgOut As PGM = New PGM
  Dim r As Integer, c As Integer
  Dim inval As Integer
  'read input image
    imgIn.setFilePath(InFilePath)
    imgIn.readImage()
  'set output-image header
    imgOut.setFilePath(OutFilePath)
    imgOut.setMagicString("P5")
    imgOut.setComment("#cracks image")
    imgOut.setDimension(imgIn.getCols(), imgIn.getRows())
```

```
'grass algorithm
'set background as white
 For r = 0 To imgOut.getRows() - 1
  For c = 0 To imgOut.getCols() - 1
   imgOut.setPixel(r, c, 255)
  Next
 Next
 Dim i As Integer
 For i = 0 To nROI - 1
'turn roi pizel of output-image into black
 Dim tX As Integer, tY As Integer
  tX = ROIX(i)
  tY = ROIY(i)
  imgOut.setPixel(tY, tX, 0)
 'perform the algorithm
  Dim nIterations As Integer
  Dim nPrevHits As Integer
  While True
   Dim nHits As Integer
   nHits = 0
   For r = 0 To imgOut.qetRows() - 1
    For c = 0 To imgOut.getCols() - 1
      'get roi pixel, if any
      inval = imgOut.getPixel(r, c)
      If inval = 0 Then
      'check imgin's 8 neighbors
       Dim neighbor(8) As Integer
    neighbor(0) = imgIn.getNeighbor(r, c, Directions.NW)
    neighbor(1) = imgIn.getNeighbor(r, c, Directions.W)
    neighbor(2) = imgIn.getNeighbor(r, c, Directions.SW)
    neighbor(3) = imgIn.getNeighbor(r, c, Directions.S)
    neighbor(4) = imgIn.getNeighbor(r, c, Directions.SE)
    neighbor(5) = imgIn.getNeighbor(r, c, Directions.E)
    neighbor(6) = imgIn.getNeighbor(r, c, Directions.NE)
    neighbor(7) = imgIn.getNeighbor(r, c, Directions.N)
    Dim t As Integer, tCount As Integer
     tCount = 0
    For t = 0 To 7
     If neighbor(t) = 0 Then
      tCount += 1
     End If
   'if all neighbors are black
    If tCount = 8 Then
     nHits += 1
   'set all neighbors of current output pixel to black
     imgOut.setPixel(r - 1, c - 1, inval)
     imgOut.setPixel(r - 1, c, inval)
     imgOut.setPixel(r - 1, c + 1, inval)
     imgOut.setPixel(r, c - 1, inval)
```

```
imgOut.setPixel(r, c + 1, inval)
        imgOut.setPixel(r + 1, c - 1, inval)
        imgOut.setPixel(r + 1, c, inval)
        imgOut.setPixel(r + 1, c + 1, inval)
      End If
     End If
    Next
   Next
    nIterations += 1
    If nIterations = 1 Then
        nPrevHits = nHits
    Else
    If nPrevHits = nHits Then
        Exit While
    End If
        nPrevHits = nHits
    End If
   End While
   Next
   'write output image
    imgOut.writeImage()
   Return (imgOut)
 End Function
 End Class
End Module
```

### Module modCrackRemoval

```
Module modCrackRemoval
 Public Class CrackRemoval
  Dim InFilePath As String, OutFilePath As String
   'constructor
   Public Sub New()
     InFilePath = ""
     OutFilePath = ""
   End Sub
 Public Function RecursiveMeanFilter(PvVal tIterations As
Integer) As PGM
   Dim imqIn As PGM = New PGM
   Dim imgOut As PGM = New PGM
   'read input image
    imgIn.setFilePath(InFilePath)
    imgIn.readImage()
   'set output-image header
    imgOut.setFilePath(OutFilePath)
    imgOut.setMagicString("P5")
    imgOut.setComment("#mean-filtered image")
    imgOut.setDimension(imgIn.getCols(), imgIn.getRows())
    imgOut.setMaxGray(imgIn.getMaxGray())
```

```
'mean filter algorithm
    Dim r As Integer, c As Integer
    Dim inval As Integer, outval As Integer
    Dim t As Integer
    For t = 1 To tIterations
     For r = 0 To imgOut.getRows() - 1
      For c = 0 To imgOut.getCols() - 1
       inval = imgIn.getPixel(r, c) 'get carrent pixel
       'get neighborhood pixel intensity values
       Dim neighbor(8) As Integer
       neighbor(0) = imgIn.getNeighbor(r, c, Directions.NW)
       neighbor(1) = imgIn.getNeighbor(r, c, Directions.W)
       neighbor(2) = imgIn.getNeighbor(r, c, Directions.SW)
       neighbor(3) = imgIn.getNeighbor(r, c, Directions.S)
       neighbor(4) = imgIn.getNeighbor(r, c, Directions.SE)
       neighbor(5) = imgIn.getNeighbor(r, c, Directions.E)
       neighbor(6) = imgIn.getNeighbor(r, c, Directions.NE)
       neighbor(7) = imgIn.getNeighbor(r, c, Directions.N)
      'compute new intensity value as mean of neighborhood
       Dim tsum As Integer = inval
       Dim k As Integer
       For k = 0 To 7
        tsum = tsum + neighbor(k) 'calc sum
       Next
        outval = tsum / 9
        imgOut.setPixel(r, c, outval)
      Next
     Next.
    'set outputimage as input to next iteration (if not
last iteration)
      If t <> tIterations Then
      Dim rl As Integer
      For r1 = 0 To imgIn.getRows() - 1
       For c = 0 To imgIn.getCols() - 1
        imgIn.setPixel(r1, c, imgOut.getPixel(r1, c))
       Next
      Next
     End If
   Next
   'write output image
     imgOut.writeImage()
    Return (imgOut)
 End Function
End Class
End Module
```

#### Module modPGM

```
Module modPGM
  Public Enum Directions
        NW = 0
        Ν
        NF.
        E
        SE
        S
        SW
        ΤΛΤ
  End Enum
  'pgmimage
  Public Class PGM
   Dim tFilePath As String
   'pgm imageheader
   Dim MagicString As String
   Dim Comment As String
   Dim Cols As Integer, Rows As Integer, MaxGray As Integer
   'pgm imagedata
   Dim Pixels(,) As Integer
   'constructor
   Public Sub New()
            tFilePath = ""
            MagicString = ""
            Comment = ""
            Cols = 0
            Rows = 0
            MaxGray = 0
  End Sub
  Public Function getPixel(ByVal tr As Integer, ByVal tc
                                    As Integer) As Integer
   Dim tIntensity As Integer
   If tr >= 0 And tr <= Rows - 1 And tc >= 0 And tc <=
       Cols - 1 Then
         tIntensity = Pixels(tr, tc)
   End If
        Return (tIntensity)
  End Function
  Public Function getNeighbor(ByVal tr As Integer, ByVal
    tc As Integer, ByVal direction As Integer) As Integer
        Dim pval As Integer = 0
       If direction = Directions.NW Then
        pval = getPixel(tr - 1, tc - 1)
       ElseIf direction = Directions.W Then
        pval = getPixel(tr, tc - 1)
       ElseIf direction = Directions.SW Then
```

```
ElseIf direction = Directions.S Then
     pval = getPixel(tr + 1, tc)
    ElseIf direction = Directions.SE Then
     pval = getPixel(tr + 1, tc + 1)
    ElseIf direction = Directions.E Then
     pval = getPixel(tr, tc + 1)
    ElseIf direction = Directions.NE Then
     pval = getPixel(tr - 1, tc + 1)
    ElseIf direction = Directions.N Then
     pval = getPixel(tr - 1, tc)
     End If
   Return (pval)
End Function
'methods
Public Function readImage()
  Dim fin As IO.FileStream = New
    IO.FileStream(tFilePath, IO.FileMode.Open)
  Dim tByte As Byte, tStr As String
 'read magicstring
  tByte = fin.ReadByte()
  MagicString = Chr(tByte)
  tByte = fin.ReadByte()
  MagicString = MagicString + Chr(tByte)
 'read comment
  tByte = fin.ReadByte() 'read vbCr
  tByte = fin.ReadByte() 'read '#'
  If tByte = 10 Then tByte = fin.ReadByte()
   Do While Chr(tByte) = "#" 'read comment
    tStr = Chr(tByte)
     Do While Chr(tByte) <> vbLf
      tByte = fin.ReadByte()
      tStr = tStr + Chr(tByte)
     Loop
    tByte = fin.ReadByte() 'read next '#'
   If tStr <> "" Then
    Comment = Left(tStr, Len(tStr) - 1)
   End If
  'read cols
    tByte = 1
    tStr = ""
    fin.Seek(-1, IO.SeekOrigin.Current)
    tByte = fin.ReadByte()
    tStr = Chr(tByte)
    Do While Chr(tByte) <> " " And Chr(tByte) <> vbLf
     tByte = fin.ReadByte()
     tStr = tStr + Chr(tByte)
    Loop
     Cols = Int(tStr)
```

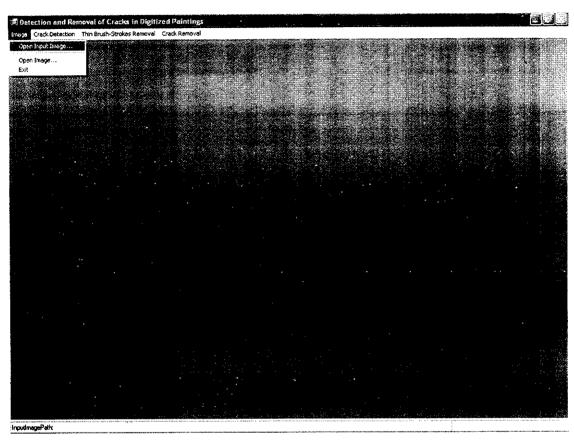
```
tBvte = fin.ReadBvte()
        Do While Chr(tByte) <> " " And Chr(tByte) <> vbLf
         tStr = tStr + Chr(tByte)
         tByte = fin.ReadByte()
        Loop
        Rows = Int(tStr)
       'read maxgray
        tBvte = 1
        tStr = ""
        tBvte = fin.ReadBvte()
        Do While Chr(tByte) <> " " And Chr(tByte) <> vbLf
         tStr = tStr + Chr(tByte)
         tByte = fin.ReadByte()
        Loop
         MaxGray = Int(tStr)
       'read imagedata
        ReDim Pixels (Rows, Cols)
        Dim x As Integer, y As Integer
         For y = 0 To Rows - 1
          For x = 0 To Cols - 1
            tByte = fin.ReadByte()
            Pixels(y, x) = tByte
           Next
          Next
         fin.Close()
    Catch err As Exception
      ShowError(err)
    End Try
   End Function
Public Function writeImage()
 Try
Dim fout As IO.FileStream = New IO.FileStream(tFilePath,
                                   IO.FileMode.Create)
Dim tByte As Byte,tStr As String,i As Integer,j As Integer
    'write image header
    'write magicstring
    tStr = "P5" + vbCrLf
    For i = 0 To Len(tStr) - 1
     tByte = Asc(tStr.Chars(i))
     fout.WriteByte(tByte)
    Next
   'write comment
    If Comment <> "" Then
     tStr = Comment + vbCrLf
     For i = 0 To Len(tStr) - 1
      tByte = Asc(tStr.Chars(i))
      fout.WriteByte(tByte)
```

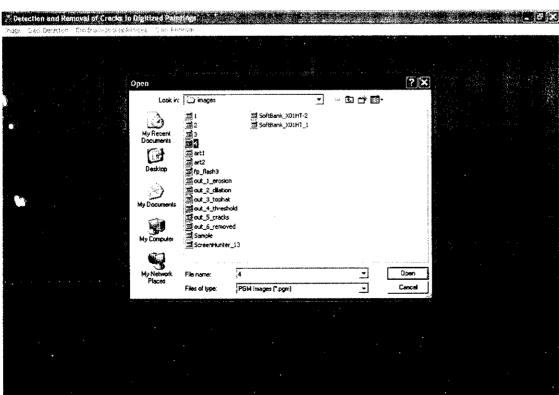
tByte = 1 tStr = ""

```
End If
 'write cols
  tStr = Trim(Str(Cols)) + " "
  For i = 0 To Len(tStr) - 1
   tByte = Asc(tStr.Chars(i))
   fout.WriteByte(tByte)
  Next
 'write rows
   tStr = Trim(Str(Rows)) + vbCrLf
   For i = 0 To Len(tStr) - 1
    tByte = Asc(tStr.Chars(i))
    fout.WriteByte(tByte)
   Next
  'write maxgrav
   tStr = Trim(Str(MaxGray)) + vbCrLf
   For i = 0 To Len(tStr) - 1
    tByte = Asc(tStr.Chars(i))
    fout.WriteByte(tByte)
   Next
   For i = 0 To Rows -1
    For j = 0 To Cols - 1
     tByte = Pixels(i, j)
     fout.WriteByte(tByte)
    Next
   Next
    fout.Close()
   Catch err As Exception
    ShowError(err)
   End Try
  End Function
 End Class
End Module
```



#### **7.2 OUTPUT SCREENS:**

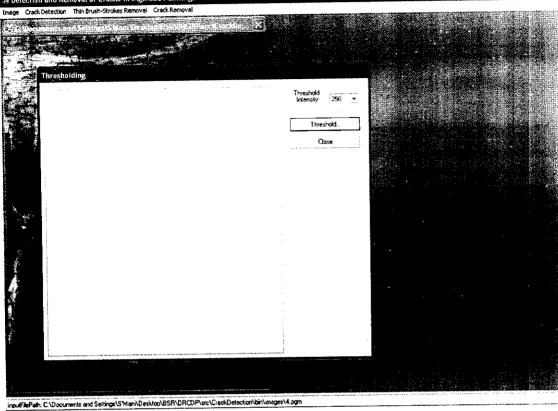


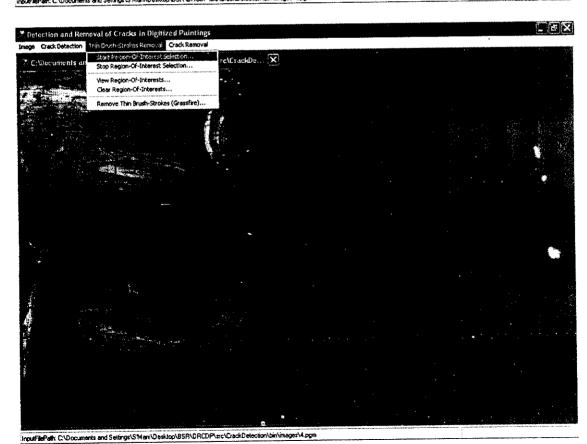


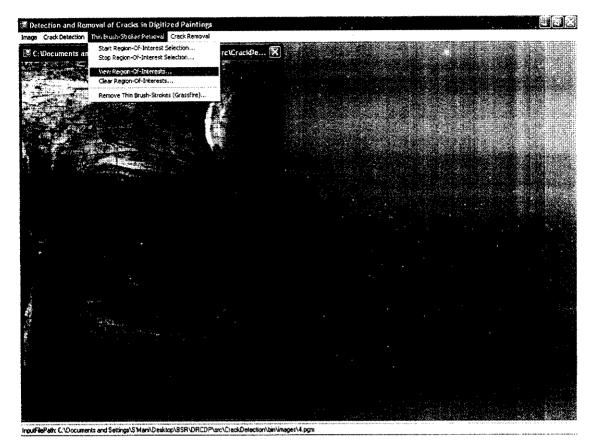


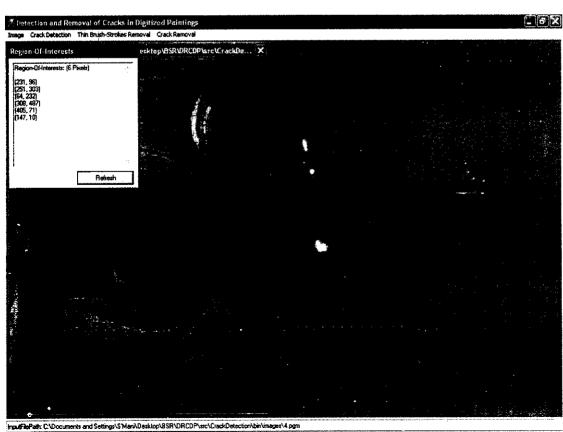


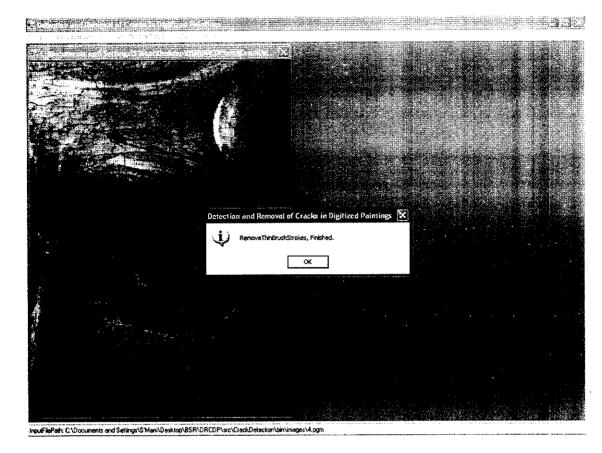
















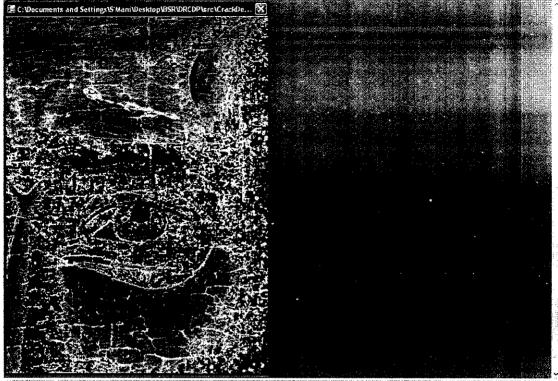


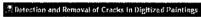
InputFilePath: C:\Documents and Settings\S'Mani\Desktop\BSR\DRCDP\src\CrackDetection\bin\images\4.pgm



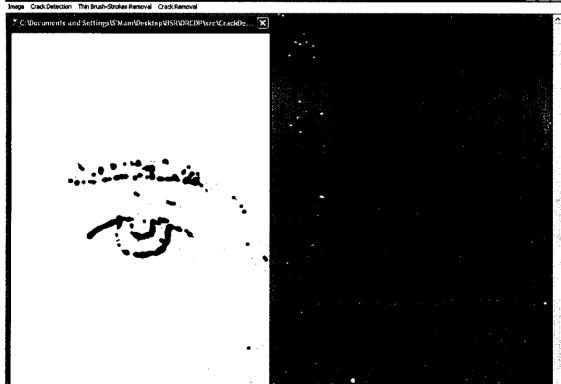
Image Crack Detection Thin Brush-Strokes Removal Crack Removal





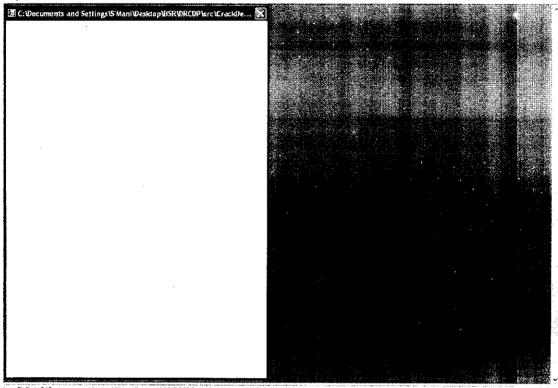




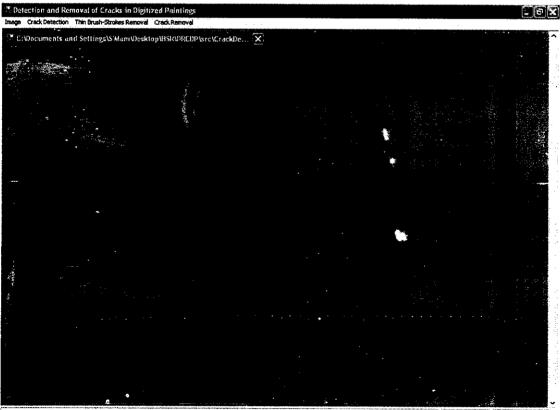


InputFilePath: C:\Documents and Settings\S'Mani\Desktop\BSR\DRCDP\src\CrackDetection\bin\images\4.pgm





InputFilePath: C:\Documents and Settings\S'Mani\Desktop\BSR\DRCDP\src\CrackDetection\bin\images\4.pgm



InputFiePath: C/L/Documents and Settings/SMani/Desktop/BSR/DRCDP/src/CrackDetection/bin/images/4.pgm

## 8. REFERENCES

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