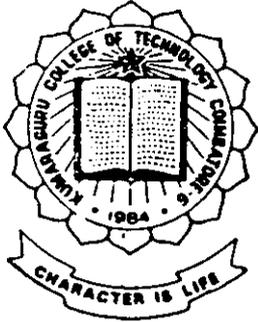


COMPUTER AIDED ANALYSIS OF COMPENSATED EHV LINES



1995 - 96



PROJECT REPORT

submitted by

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under the guidance of

Mr V SIVAKUMAR, B.E.

IN PARTIAL fulfilment of the REQUIREMENTS
for the AWARD of the degree of

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KUMARAGURU COLLEGE OF TECHNOLOGY
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**"COMPUTER AIDED ANALYSIS OF
COMPENSATED EHV LINES"**

is a bonafide work carried out by

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This is to certifiy that the following final year B.E. ELECTRICAL & ELECTRONICS ENGINEERING students of KUMARAGURU COLLEGE OF TECHNOLOGY, COIMBATORE have under taken a project under the title:

"COMPUTER AIDED ANALYSIS OF COMPENSATED EHV LINES"

in Power System division department of the Central Power Research Institute, Bangalore during the period September 1995 to March 1996.

1. A. RICHARD
2. V.ASHOK KUMAR
3. PRASHANTH CHANDRAN

The above students have taken great interest and have shown immense potential in the field of study. Their conduct and character have been good and have completed the project sucessfully.

Yours,


P.V. BALASUBRAMANYAM, M.Tech
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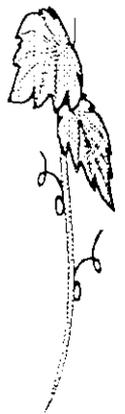


**DEDICATED
TO OUR
BELOVED PARENTS**





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ACKNOWLEDGEMENT

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SYNOPSIS



SYNOPSIS

The growing demand of electricity and the economics associated with its supply at low rates to consumers has resulted in the construction of large capacity generating station at suitable locations. Large load centres are often located at great distances from such generating stations. Bulk power is carried from these stations to load centres over Extra High Voltage transmission lines for which voltages upto 400 Kilo Volt have been used. Use of series capacitors to compensate line parameters has led to an economical and efficient method of improving stability and system performance.

The present work deals with the analysis of series capacitor compensated Extra High Voltage (E.H.V) lines. Further, the problems arising in the series capacitor compensation and their remedies have been mentioned.

A software in Fortran 77 has been developed to analyse the compensated line.



CONTENTS



CONTENTS

PAGE NO.

CERTIFICATE	i
ACKNOWLEDGEMENT	ii
SYNOPSIS	iii
CONTENTS	
I. INTRODUCTION	
1.1. STRUCTURE OF A POWER SYSTEM	01
1.2. LONG DISTANCE POWER TRANSMISSION	03
II TRANSMISSION LINE MODELLING	
2.1. TWO PORT REPRESENTATION	06
2.2. CLASSIFICATION OF TRANSMISSION LINES	07
2.3. DERIVATION OF ABCD CONSTANTS FOR TRANSMISSION LINES	07
2.4. ABCD CONSTANTS FOR SERIES CAPACITOR	14
2.5. ABCD CONSTANTS FOR NETWORK CONNECTED IN SERIES	15
2.6. POWER FLOW THROUGH A TRANSMISSION LINE	16
2.7. DERIVATION OF LOAD ANGLE	19
2.8. EFFICIENCY	20
2.9. DERIVATION OF CRITICAL VOLTAGE AND CRITICAL LOAD ANGLE	20

III	SERIES CAPACITOR COMPENSATION	
3.1.	SERIES COMPENSATION FACTOR	32
3.2.	PRINCIPLE OF SERIES COMPENSATION	33
3.3.	COMPENSATION SCHEMES	36
3.4.	ANALYSIS OF SERIES COMPENSATED TRANSMISSION LINE	37
3.5.	EVALUATION OF ABCD CONSTANTS OF COMPENSATED LINE	37
IV	EVALUATION OF VARIOUS PARAMETERS	
4.1.	LINE CONSTANTS	43
4.2.	ASSUMPTIONS	43
4.3.	PARAMETERS CONSIDERED FOR ANALYSIS	44
V	RESULTS AND COMPARATIVE STUDY	
5.1.	VARIATION OF RECEIVING END POWER	46
5.2.	VARIATION OF MAXIMUM RECEIVING END POWER	47
5.3.	VARIATION OF EFFICIENCY	47
5.4.	VARIATION OF B_0	48
5.5.	VARIATION OF RECEIVING END POWER WITH DELTA	49
5.6.	EFFECT OF $V_{R\ CRIT}$ AND δ_{CRIT} ON P_R AND $P_{R\ MAX}$	49
VI	DEVELOPMENT OF SOFTWARE	
6.1.	ALGORITHM	78
6.2.	FLOWCHART	80
6.3.	PROGRAM	83

VII PROBLEMS ASSOCIATED WITH SERIES
COMPENSATION

7.1. PROBLEMS IN APPLICATION OF SERIES CAPACITOR	94
7.2. EFFECT OF SSR ON POWER SYSTEMS	96
7.3. ANALYSIS OF SSR	97
7.4. SSR PREVENTIVE METHODS	97

VIII CONCLUSION

REFERENCE



INTRODUCTION



CHAPTER 1

INTRODUCTION

1.1. STRUCTURE OF POWER SYSTEM

The major parts of a power system are

- 1.1.1. Generating System.
- 1.1.2. Transmission Lines.
- 1.1.3. Distribution Systems.

These are schematically represented in fig (1.01).

1.1.1. GENERATING SYSTEM

This forms the head of the frame. Energy is generated by using the earth's natural resources to the fullest extent. The different types of generating plants are,

- 1.1.1.1. Diesel power plant.
- 1.1.1.2. Hydro-electric power plant.
- 1.1.1.3. Thermal power plant.
- 1.1.1.4. Nuclear power plant.

Voltages like 6.6, 11, 13.8 KV are generated.

1.1.2. TRANSMISSION LINES

Transmission lines and distribution systems are the connecting link between the generating station and lead to other power systems over interconnections.

The generated voltage is stepped up to transmission levels in the range of 115 to 765 KV.

They can be categorised as High Voltage (HV) and Extra High Voltage (EHV) at 330 KV. The above fall under EHV category.

In INDIA, 400 KV A.C. transmission system are in service. The behavior of these EHV lines are in many respect similar to the 220 KV lines.

Transmission of large blocks of power over long distance can be done most economically only by using EHV lines. Normally EHV A.C. lines are preferred.

Underground transmission cables are mostly used in heavily populated areas. Research is still being carried out on an ultra high voltage transmission in the range of 1000 KV to 1500 KV.

1.1.3. DISTRIBUTION SYSTEM

A distribution system connects all the individual loads to the transmission lines at sub stations, which perform voltage transformation and switching action.

1.2. LONG DISTANCE POWER TRANSMISSION

Long distance, bulk power transmission from remote generating stations to concentrated load centers is one of the most important needs of the power industry.

Now a days much progress in transmission engineering has been achieved. The most important of these developments are:

- i. Increasing the voltage levels of the transmission
- ii. The use of various methods of improving the stability limits

There are many problems associated with higher transmission voltages such as switching surges, insulation of systems etc.,

There are mainly two alternatives to utilise the existing line capacity fully and improve stability limits. They are:

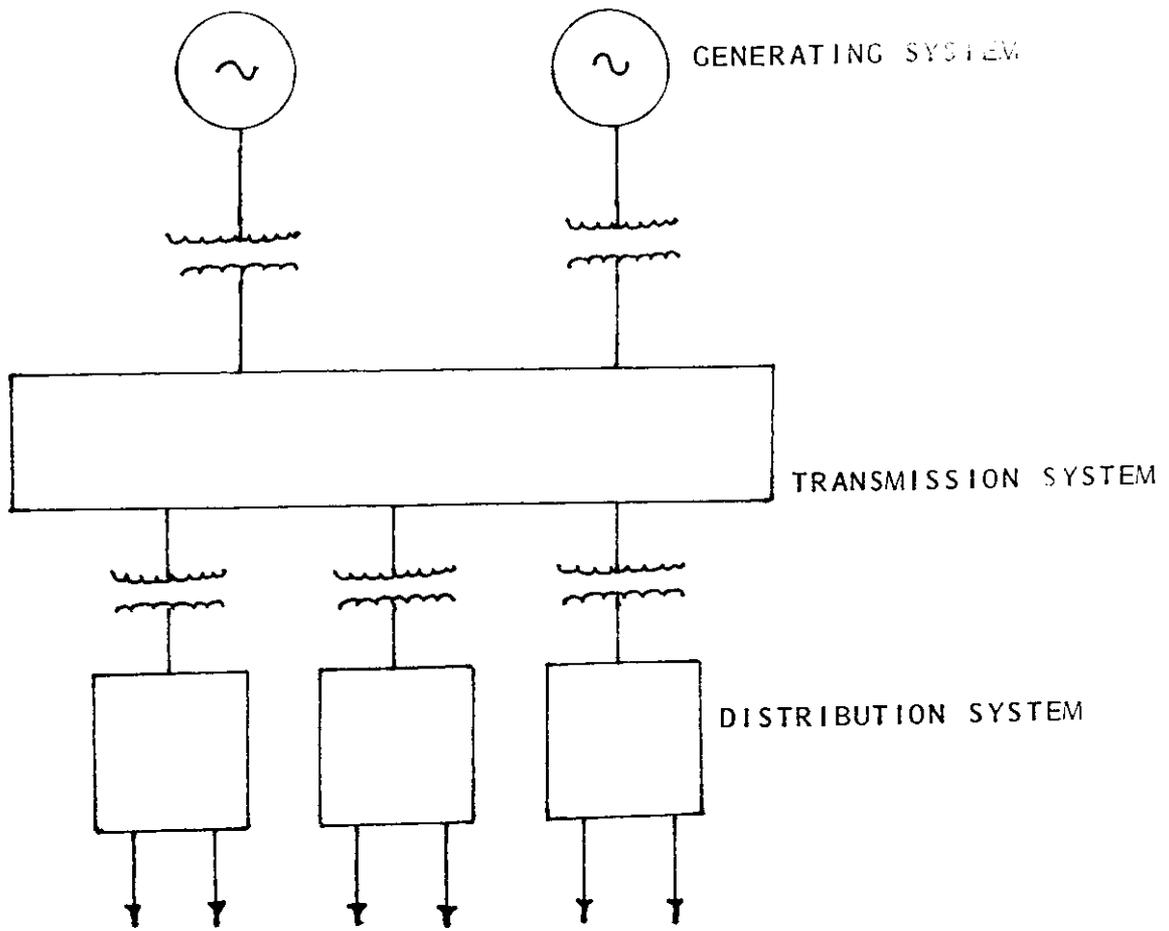
- i. Series and shunt compensation of lines
- ii. H.V.D.C. transmission

The H.V.D.C. transmission though has advantages, suffers the disadvantages of the impossibility of exchange of reactive power and high cost of the terminal equipments.

The compensation of transmission line inductance and capacitance by series capacitor and shunt reactor is considered as a powerful tool for the improvement of power system performance.

The series capacitors, by artificially reducing net amount of reactance presented by the line, to a degree depending on the percentage of compensation used, permits an increase of the permissible loading of the line.

The present work deals with compensation and analysis of transmission line with **SERIES CAPACITOR**.

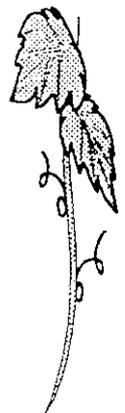


STRUCTURE OF POWER SYSTEM

FIG. 1.01



TRANSMISSION LINE MODELLING



CHAPTER 2

TRANSMISSION LINE MODELING

This part primarily deals with the characteristics and performance of transmission lines. Normally, transmission lines are operated with three phase balanced loads. Hence the analysis can proceed on a per phase basis.

2.1. TWO PORT REPRESENTATION

A transmission line may be regarded as a two port network where the sending end quantities are related to the receiving end quantities, through ABCD parameters. This is shown in figure (2.01).

Let V_s be the sending end voltage, V_R be the receiving end voltage, I_s be the sending end current, I_R be the receiving end current, then

$$V_s = A \cdot V_R + B \cdot I_R \quad (2.01)$$

$$I_s = C \cdot V_R + D \cdot I_R \quad (2.02)$$

Equations (2.01) and (2.02) can be represented in matrix form as

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \cdot \begin{bmatrix} V_R \\ I_R \end{bmatrix} \quad (2.03)$$

The ABCD constants of any transmission lines may be determined easily by making suitable assumptions.

2.2. CLASSIFICATION OF TRANSMISSION LINES

Transmission lines are classified into three types depending on their length.

- | | |
|-----------------|-------------------------------|
| 1. SHORT LINES | Line length 100 Km (or less). |
| 2. MEDIUM LINES | Line length 100 Km to 250 Km. |
| 3. LONG LINES | Line length over 250 Km. |

2.3. DERIVATION OF ABCD CONSTANTS FOR DIFFERENT TYPES OF TRANSMISSION LINES

2.3.1. SHORT LINES

The admittance of short lines is neglected. Thus the equivalent of short lines is as shown in fig. (2.02).

R is the resistance of the line and X is the impedance of the line.

The relationship between sending end and receiving end voltages and current are

$$V_S = V_R + (R+jX) \cdot I_R$$

$$V_S = V_R + Z \cdot I_R \quad (2.04)$$

where $Z = R + jX$

$$I_S = I_R$$

$$I_S = 0 \cdot V_R + I_R \quad (2.05)$$

Equations (4) and (5) can be represented as

$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} A & B \\ C & D \end{bmatrix} \cdot \begin{bmatrix} V_R \\ I_R \end{bmatrix} \quad (2.06)$$

Comparing equations (2.03) and (2.06)

The ABCD constants are $A = 1$; $B = Z$;
 $C = 0$; $D = 1$.

2.3.2. MEDIUM LINES

The shunt admittance cannot be neglected for medium lines. They are lumped at one or two places.

If the shunt admittance placed in the middle of the line, then the circuit is called as the NOMINAL "T" NETWORK and if it is placed at the two ends of the line the circuit is called as the NOMINAL " π " NETWORK

2.3.2.1. ABCD CONSTANTS FOR NOMINAL T NETWORK

The impedance z is derived into two (each $Z/2$) and the admittance (Y) is lumped at the centre, as shown in figure (2.03)

Let V_y be the voltage across the shunt admittance. Then,

$$V_C = V_R + I_R \cdot (Z/2)$$

$$I_S = I_R + V_C \cdot Y$$

substituting the value of V_C in I_S , we get,

$$I_S = I_R + Y \cdot V_R + I_R \cdot (Z/2) \cdot Y$$

$$I_S = Y \cdot V_R + (1 + YZ/2) \cdot I_R \quad (2.07)$$

$$V_S = V_C + I_S \cdot (Z/2)$$

$$V_S = V_R + I_R \cdot (Z/2) + I_S \cdot (Z/2)$$

$$V_S = V_R + I_R \cdot (Z/2) + (Y \cdot V_R + (1 + YZ/2) \cdot I_R) \cdot (Z/2)$$

$$V_S = V_R (1 + YZ/2) + I_R \cdot Z (1 + YZ/4) \quad (2.08)$$

Equations (2.07) and (2.08) can be represented as

$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} (1+YZ/2) & Z(1+YZ/4) \\ Y & (1+YZ/2) \end{bmatrix} \cdot \begin{bmatrix} V_R \\ I_R \end{bmatrix} \quad (2.09)$$

Comparing equations (2.08) and (2.09), we get

$$\begin{aligned} A &= 1 + YZ/2 & ; & & B &= Z(1 + YZ/4) \\ C &= Y & ; & & D &= (1 + YZ/2) \end{aligned}$$

2.3.2.2. ABCD CONSTANTS FOR NOMINAL - π NETWORK

The admittance (Y) is divided into 2 (ie., each is $Y/2$) and placed at the end of the π network, with impedance Z in the middle, as shown in the figure (2.04).

The relationship between sending end and receiving end voltages and currents are,

$$\begin{aligned} V_S &= V_R + (I_R + V_R \cdot Y/2) Z \\ V_S &= (1 + YZ/2) \cdot V_R + Z \cdot I_R \end{aligned} \quad (2.10)$$

$$\begin{aligned} I_S &= I_R + V_R \cdot Y/2 + V_S \cdot Y/2 \\ I_S &= I_R + V_R \cdot Y/2 + (1 + YZ/2 + I_R \cdot Z) Y/2 \\ I_S &= Y (1 + YZ/4) \cdot V_R + (1 + YZ/2) \cdot I_R \end{aligned} \quad (2.11)$$

Equations (10) and (11) can be represented as,

$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} (1 + YZ/2) & Z \\ Y(1 + YZ/4) & (1 + YZ/2) \end{bmatrix} \cdot \begin{bmatrix} V_R \\ I_R \end{bmatrix} \quad (2.12)$$



Comparing equations (2.03) and (2.12), we get.

$$A = \frac{1+YZ}{2} \quad ; \quad B = Z ;$$

$$C = Y\left(\frac{1+YZ}{4}\right) \quad ; \quad D = \left(\frac{1+YZ}{2}\right).$$

2.3.3. DERIVATION OF ABCD PARAMETERS FOR LONG TRANSMISSION LINE

For long transmission lines, the impedances are distributed uniformly all along the line. Figure (2.05) shows '**SINGLE PHASE EQUIVALENT CIRCUIT**' of a long transmission line.

Consider a small elemental length ' dx ' of the line at a distance ' x ' from the receiving end. Let ' L ' be the total length of the line measured from receiving end. Let ' Z ' be the impedance of the line per phase per unit length of line in ohms.

Let ' Y ' be the susceptance per phase per unit length of line in mhos.

From figure (2.05) we have,

$$dv = IZdx$$

or

$$\frac{dv}{dx} = IZ \quad (2.13)$$

$$\frac{dl}{dx} = VY \quad (2.14)$$

Differentiating equation (2.13) w.r.t. x. we get.

$$\frac{d^2v}{dx^2} = \frac{dl}{dx} \cdot z$$

substituting the value of dl/dx from equation (2.14).

$$\frac{d^2v}{dx^2} = YZV \quad (2.15)$$

This is a linear differential equation whose solution can be written as.

$$\begin{aligned} V &= K_1 \cdot e^{\sqrt{(YZ)}x} + K_2 \cdot e^{-\sqrt{(YZ)}x} \\ V &= K_1 \cdot e^{\gamma x} + K_2 \cdot e^{-\gamma x} \end{aligned} \quad (2.16)$$

where,

$$\gamma = \sqrt{(YZ)}$$

K_1, K_2 are arbitrary constants to be evaluated.

Differentiating equation (2.16) w.r.t. x.

$$\frac{dV}{dX} = K_1 \cdot \gamma \cdot e^{\gamma x} - K_2 \cdot \gamma \cdot e^{-\gamma x}$$

Substituting the value of dV/dX from eq.(2.13).

$$IZ = \gamma (K_1 \cdot e^{\gamma x} - K_2 \cdot e^{-\gamma x}) \quad (2.17)$$

Substituting the value of γ .

$$\begin{aligned} IZ &= \text{sqrt}(YZ) [K_1 \cdot e^{\gamma x} - K_2 \cdot e^{-\gamma x}] \\ I &= \text{sqrt}(Y/Z) [K_1 \cdot e^{\gamma x} - K_2 \cdot e^{-\gamma x}] \end{aligned}$$

Let $Z_0 = \text{sqrt}(Y/Z)$. then

$$I = 1/Z_0 \cdot (K_1 \cdot e^{\gamma x} - K_2 \cdot e^{-\gamma x}) \quad (2.18)$$

The constants K_1 & K_2 can be evaluated by using end conditions.

When $X = 0$: $V = V_R$ and $I = I_R$

substituting these values in eq.(2.16) and (2.18), we get.

$$\begin{aligned} V_R &= K_1 + K_2 \\ I_R &= 1/Z_0 \cdot (K_1 - K_2) \end{aligned}$$

Which on solving yields.

$$\begin{aligned} K_1 &= 1/2 (V_R + Z_0 \cdot I_R) \\ K_2 &= 1/2 (V_R - Z_0 \cdot I_R) \end{aligned}$$

Substituting the values of K_1 and K_2 in equations (2.16) and (2.18), we get.

$$V = \frac{(V_R + I_R \cdot Z_0) \cdot e^{\gamma X}}{2} + \frac{(V_R - I_R \cdot Z_0) \cdot e^{-\gamma X}}{2} \quad (2.19)$$

$$I = \frac{(V_R + I_R \cdot Z_0) \cdot e^{\gamma X}}{2 \cdot Z_0} - \frac{(V_R - I_R \cdot Z_0) \cdot e^{-\gamma X}}{2 \cdot Z_0} \quad (2.20)$$

Rearranging equations (2.19) and (2.20) we get.

$$\begin{aligned} V &= V_R \cdot \frac{(e^{\gamma X} + e^{-\gamma X})}{2} + I_R \cdot Z_0 \cdot \frac{(e^{\gamma X} - e^{-\gamma X})}{2} \\ I &= \frac{V_R}{Z_0} \cdot \frac{(e^{\gamma X} - e^{-\gamma X})}{2} + I_R \cdot \frac{(e^{\gamma X} + e^{-\gamma X})}{2} \end{aligned}$$

The above equations can be written as.

$$\begin{aligned} V &= V_R \cdot \text{COSH}(\gamma X) + I_R \cdot Z_0 \cdot \text{SINH}(\gamma X) \\ I &= (V_R/Z_0) \cdot \text{SINH}(\gamma X) + I_R \cdot \text{COSH}(\gamma X) \end{aligned}$$

When $X = L$: $V = V_s$ and $I = I_s$

$$\therefore V_s = V_R \cdot \text{COSH}(\gamma X) + I_R \cdot Z_o \cdot \text{SINH}(\gamma L) \quad (2.21)$$

$$\therefore I_s = (V_R/Z_o) \cdot \text{SINH}(\gamma L) + I_R \cdot \text{SINH}(\gamma L) \quad (2.22)$$

But we know that.

$$V_s = A.V_R + B.I_R \quad (2.23)$$

$$I_s = C.V_R + D.I_R \quad (2.24)$$

Comparing equations (2.21) and (2.23), equations (2.22) and (2.24), we get.

$$A = \text{COSH}(\gamma L) \quad B = Z_o \cdot \text{SINH}(\gamma L)$$

$$C = (1/Z_o) \cdot \text{SINH}(\gamma L) \quad D = \text{COSH}(\gamma L)$$

Where

Z_o is called the 'CHARACTERISTIC IMPEDANCE' and

γ is called the 'PROPAGATION CONSTANT'

2. 4 ABCD CONSTANTS FOR SERIES CAPACITOR COMPENSATING NETWORK

The series capacitor compensating network is shown in fig.(2.06).

We know that

$$V_s = A \cdot V_R + B \cdot I_R \quad (2.25)$$

$$I_s = C \cdot V_R + D \cdot I_R \quad (2.26)$$

From the above network, we have,

$$\begin{aligned} V_R &= V_S - I_R(-jX_C) \\ &= V_S + I_R \cdot jX_C \end{aligned}$$

$$\therefore V_S = V_R - (jX_C) \cdot I_R \quad (2.27)$$

$$I_S = 0 \cdot V_R + I_R \quad (2.28)$$

Comparing equations (2.25) and (2.27), equations (2.26) and (2.28) we get,

$$\begin{aligned} A_C &= 1 & B_C &= -jX_C \\ C_C &= 0 & D_C &= 1 \end{aligned}$$

2.5 ABCD CONSTANTS FOR A NETWORK CONNECTED IN SERIES

Whenever a power system consists of a series combination of networks, whose ABCD constants are known, the overall ABCD constants for the system may be determined as follows.

Consider two series networks of ABCD constants $A_{S1}, B_{S1}, C_{S1}, D_{S1}$ and $A_{S2}, B_{S2}, C_{S2}, D_{S2}$ as shown in fig. (2.07)

The two networks can be reduced to a single equivalent network as follows.

For the first network we have,

$$\begin{bmatrix} V_S \\ I_S \end{bmatrix} = \begin{bmatrix} A_{S1} & B_{S1} \\ C_{S1} & D_{S1} \end{bmatrix} \cdot \begin{bmatrix} V_X \\ I_X \end{bmatrix} \quad (2.29)$$

For the second network we have,

$$\begin{bmatrix} V_X \\ I_X \end{bmatrix} = \begin{bmatrix} A_{S2} & B_{S2} \\ C_{S2} & D_{S2} \end{bmatrix} \cdot \begin{bmatrix} V_R \\ I_R \end{bmatrix} \quad (2.30)$$

From equations (2.29) and (2.30), we get.

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} A_{s1} & B_{s1} \\ C_{s1} & D_{s1} \end{bmatrix} \cdot \begin{bmatrix} A_{s2} & B_{s2} \\ C_{s2} & D_{s2} \end{bmatrix} \cdot \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

On simplification we get.

$$\begin{bmatrix} V_s \\ I_s \end{bmatrix} = \begin{bmatrix} A_o & B_o \\ C_o & D_o \end{bmatrix} \cdot \begin{bmatrix} V_R \\ I_R \end{bmatrix}$$

Thus the overall ABCD constants of the network is equal to the product of the ABCD matrix of the networks.

$$\begin{bmatrix} A_o & B_o \\ C_o & D_o \end{bmatrix} = \begin{bmatrix} A_{s1} & B_{s1} \\ C_{s1} & D_{s1} \end{bmatrix} \cdot \begin{bmatrix} A_{s2} & B_{s2} \\ C_{s2} & D_{s2} \end{bmatrix}$$

2.6 POWER FLOW THROUGH A TRANSMISSION LINE

The sending end and receiving end voltages and currents of a transmission line are related by.

$$V_s = A_o \cdot V_R + B_o \cdot I_R \quad (2.31)$$

$$I_s = C_o \cdot V_R + D_o \cdot I_R \quad (2.32)$$

Let $V_R = V_R \angle 0$ and $V_s = V_s \angle \delta$

where δ is called the Torque or the power angle.

Let A_o, B_o, C_o, D_o be the net transmission line constants.

$$\text{Then } A_o = A_o \angle \alpha \quad B_o = B_o \angle \beta$$

$$C_o = C_o \angle \Delta \quad D_o = D_o \angle \delta$$

From eq.(2.31) we have.

$$I_R = (1/B_o) \cdot V_s - (A_o/B_o) \cdot V_R \quad (2.33)$$

Substituting the value of I_R from equations (2.33) in (2.32) we get.

$$\begin{aligned}
 I_S &= C_o \cdot V_R + \left[\frac{V_S}{B_o} - \frac{A_o}{B_o} \cdot V_R \right] \cdot D_o \\
 I_S &= \frac{D_o}{B_o} \cdot V_S + \left[C_o - \frac{(A_o \cdot D_o)}{B_o} \right] \cdot V_R \\
 I_S &= \frac{D_o}{B_o} \cdot V_S - (A_o \cdot D_o - C_o \cdot B_o) \cdot \frac{V_R}{B_o} \\
 \therefore I_S &= \frac{D_o}{B_o} \cdot V_S - \frac{V_R}{B_o} \tag{2.34}
 \end{aligned}$$

Therefore equations (2.33) and (2.34) can be written as.

$$\begin{aligned}
 I_R &= (1/B_o) \cdot |V_S| \underline{\delta - \beta} - (A_o/B_o) \cdot |V_R| \underline{\alpha - \beta} \\
 I_S &= (D_o/B_o) \cdot |V_S| \underline{\delta + \alpha - \beta} - (1/B_o) \cdot |V_R| \underline{\Delta - \beta}
 \end{aligned}$$

The complex power at the sending and receiving end are.

$$S_R = P_R + jQ_R = V_R I_R^* \tag{2.35}$$

$$S_S = P_S + jQ_S = V_S I_S^* \tag{2.36}$$

* represents conjugate.

Substituting the value of I_R from eq.(2.33) into (2.35) we get.

$$\begin{aligned}
 S_R &= |V_R| |I| \cdot \left[\frac{1}{|B_o|} \cdot |V_S| \underline{\beta - \delta} - \frac{|A_o|}{|B_o|} \cdot |V_R| \underline{\beta - \alpha} \right] \\
 \therefore S_R &= \frac{|V_S| |V_R|}{|B_o|} \cdot \underline{\beta - \delta} - \frac{|A_o|}{|B_o|} \cdot |V_R|^2 \cdot \underline{\beta - \alpha} \tag{2.37}
 \end{aligned}$$

Substituting the value of I_s from equation (2.32) into (2.36) we get

$$S_s = \frac{|A_o|}{|B_o|} |V_s|^2 \cos(\beta - \alpha) - \frac{|V_R||V_R|}{|B_o|} \cos(\beta + \alpha) \quad (2.38)$$

If equations (2.37) and (2.38) are expressed as real and imaginary parts, then real power at receiving end is given by.

$$P_R = \frac{|V_s||V_R|}{|B_o|} \cos(\beta - \delta) - \frac{|A_o||V_R|^2}{|B_o|} \cos(\beta - \alpha) \quad (2.39)$$

and real power at sending end is.

$$P_s = \frac{|D_o||V_s|^2}{|B_o|} \cos(\beta - \alpha) - \frac{|V_s||V_R|}{|B_o|} \cos(\beta + \delta) \quad (2.40)$$

Reactive power at receiving end is.

$$Q_R = \frac{|V_s||V_R|}{|B_o|} \sin(\beta - \delta) - \frac{|A_o||V_R|^2}{|B_o|} \sin(\beta - \alpha) \quad (2.41)$$

Reactive power at sending end is.

$$Q_s = \frac{|D_o||V_s|^2}{|B_o|} \sin(\beta - \alpha) - \frac{|V_s||V_R|}{|B_o|} \sin(\beta + \delta) \quad (2.42)$$

It is seen from equation (2.39) that the receiving end power (P_R) is maximum at $\delta = \beta$

$$P_{R \text{ MAX}} = \frac{|V_s||V_R|}{|B_o|} - \frac{|A_o||V_R|^2}{|B_o|} \cos(\beta - \alpha) \quad (2.43)$$

Let R be the ratio of sending end voltage (V_s) and receiving end voltage (V_R).

$$R = \frac{V_s}{V_R}$$

From this,

$$V_R = \frac{V_s}{R}$$

Substituting the value of V_R in equations (2.39), (2.40), (2.41), (2.42) and (2.43) we get,

$$P_R = \frac{|V_s|^2}{R|B_o|} \cos(\beta - \delta) - \frac{|V_s|^2 |A_o|}{R^2 |B_o|} \cos(\beta - \alpha) \quad (2.44)$$

$$P_s = \frac{|V_s|^2 |D_o|}{|B_o|} \cos(\beta - \alpha) - \frac{|V_s|^2}{R|B_o|} \cos(\beta + \delta) \quad (2.45)$$

$$Q_R = \frac{|V_s|^2}{R|B_o|} \sin(\beta - \delta) - \frac{|V_s|^2 |A_o|}{R^2 |B_o|} \sin(\beta - \alpha) \quad (2.46)$$

$$Q_s = \frac{|V_s|^2 |D_o|}{|B_o|} \sin(\beta - \alpha) - \frac{|V_s|^2}{R|B_o|} \sin(\beta + \delta) \quad (2.47)$$

$$P_{R \text{ MAX}} = \frac{|V_s|^2}{R|B_o|} - \frac{|V_s|^2 |A_o|}{R^2 |B_o|} \cos(\beta - \alpha) \quad (2.48)$$

2.7 DERIVATION FOR LOAD ANGLE (δ)

For a power factor equal to $\cos \phi$, the ratio of real to reactive power is given by,

$$\begin{aligned} \frac{P_R}{Q_R} &= \frac{\cos \phi}{\sin \phi} = \frac{\frac{E_s^2}{RB} \cos(\beta - \delta) - \frac{E_s^2}{R^2 B} A \cos(\beta - \alpha)}{\frac{E_s^2}{RB} \sin(\beta - \delta) - \frac{E_s^2}{R^2 B} A \sin(\beta - \alpha)} \\ &= \frac{\cos(\beta - \delta) - \frac{A}{R} \cos(\beta - \alpha)}{\sin(\beta - \delta) - \frac{A}{R} \sin(\beta - \alpha)} \end{aligned}$$

$$\Rightarrow \frac{\cos\phi}{\sin\phi} = \frac{R \cos(\beta - \delta) - A \cos(\beta - \alpha)}{R \sin(\beta - \delta) - A \sin(\beta - \alpha)}$$

$$R \cos\phi \sin(\beta - \delta) - A \cos\phi \sin(\beta - \delta) = R \sin\phi \cos(\beta - \delta) - A \sin\phi \cos(\beta - \alpha)$$

$$R [\cos\phi \sin(\beta - \delta) - \sin\phi \cos(\beta - \delta)] = A [\cos\phi \sin(\beta - \alpha) - \sin\phi \cos(\beta - \alpha)]$$

$$-R [\sin(\phi - \beta + \delta)] = -A [\sin(\phi - \beta + \alpha)]$$

$$\sin(\phi - \beta + \delta) = \frac{A}{R} \sin(\phi - \beta + \alpha)$$

$$\phi - \beta + \delta = \sin^{-1} \left[\frac{A}{R} \sin(\phi - \beta + \alpha) \right]$$

$$\therefore \delta = \phi - \beta + \sin^{-1} \left[\frac{A}{R} \sin(\phi - \beta + \alpha) \right] \quad (2.49)$$

2.8 EFFICIENCY

The efficiency of the system is given by

$$\text{Efficiency } (\eta) = (PR/PS) \cdot 100 \quad (2.50)$$

2.9 DERIVATION OF CRITICAL VOLTAGE ($V_{R \text{ CRIT}}$) AND CRITICAL LOAD ANGLE (δ_{CRIT})

We know that,

$$P_R = \frac{V_S \cdot V_R}{B} \cos(\beta - \delta) - \frac{A V_R^2}{B} \cos(\beta - \alpha) \quad (2.51)$$

$$Q_R = \frac{V_S \cdot V_R}{B} \sin(\beta - \delta) - \frac{A V_R^2}{B} \sin(\beta - \alpha) \quad (2.52)$$

Where,

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} |A| \underline{\alpha} & |B| \underline{\beta} \\ |c| \underline{\gamma} & |d| \underline{\Delta} \end{bmatrix}$$

are the ABCD constants of transmission line.

The two equations can be written as a function of V_s, V_R, δ and are given by

$$F_1 = P_R - \frac{V_s V_R}{B} \cos(\beta - \delta) + \frac{A V_R^2}{B} \cos(\beta - \alpha) \quad (2.53)$$

$$F_2 = Q_R - \frac{V_s V_R}{B} \sin(\beta - \delta) + \frac{A V_R^2}{B} \sin(\beta - \alpha) \quad (2.54)$$

Where F_1 and F_2 are dependant on V_s, V_R, δ

Assuming V_s is fixed at 1PU, F_1 and F_2 depends on V_R and δ

From equations (2.53) and (2.54), small variations of F_1 and F_2 in V_R and δ can be obtained and are,

$$\Delta F_1 = \frac{\partial F_1}{\partial \delta} \Delta \delta + \frac{\partial F_1}{\partial V_R} \Delta V_R \quad (2.55)$$

$$\Delta F_2 = \frac{\partial F_2}{\partial \delta} \Delta \delta + \frac{\partial F_2}{\partial V_R} \Delta V_R \quad (2.56)$$

putting it in matrix form we get,

$$\begin{bmatrix} \Delta F_1 \\ \Delta F_2 \end{bmatrix} = \begin{bmatrix} \partial F_1 / \partial \delta & \partial F_1 / \partial V_R \\ \partial F_2 / \partial \delta & \partial F_2 / \partial V_R \end{bmatrix} \cdot \begin{bmatrix} \Delta \delta \\ \Delta V_R \end{bmatrix} \quad (2.57)$$

The maximum power transfer criterion is determined by considering the singularity of equation (2.57)

$$\frac{\partial F_1}{\partial \delta} \cdot \frac{\partial F_2}{\partial V_R} - \frac{\partial F_2}{\partial \delta} \cdot \frac{\partial F_1}{\partial V_R} = 0 \quad (2.58)$$

From equations (2.53) and 2.54) we get,

$$\frac{\partial F_1}{\partial \delta} = 0 - \frac{V_s \cdot V_R}{B} \left[-\sin(\beta - \delta)(-1) \right]$$

$$\frac{\partial F_1}{\partial \delta} = - \frac{V_s \cdot V_R}{B} \left[\sin(\beta - \delta) \right] \quad (2.59)$$

$$\frac{\partial F_1}{\partial V_R} = \frac{-V_s}{B} \cos(\beta - \delta) + 2 \frac{A}{B} V_R \cos(\beta - \alpha) \quad (2.60)$$

$$\frac{\partial F_2}{\partial \delta} = \frac{-V_s \cdot V_R}{B} \left[\cos(\beta - \delta)(-1) \right]$$

$$\frac{\partial F_2}{\partial \delta} = \frac{V_s \cdot V_R}{B} \cos(\beta - \delta) \quad (2.61)$$

$$\frac{\partial F_2}{\partial V_R} = \frac{-V_s}{B} \sin(\beta - \delta) + 2 \frac{A}{B} V_R \sin(\beta - \alpha) \quad (2.62)$$

Substituting equations (2.59), (2.60), (2.61) and (2.62) in equation (2.58) we get.

$$\left[\frac{-V_s V_R}{B} \sin(\beta - \delta) \right] \left[\frac{-V_s}{B} \sin(\beta - \delta) + 2 \frac{A}{B} V_R \sin(\beta - \alpha) \right] -$$

$$\left[\frac{-V_s}{B} \cos(\beta - \delta) + 2 \frac{A}{B} V_R \cos(\beta - \alpha) \right] \left[\frac{V_s V_R}{B} \cos(\beta - \delta) \right]$$

$$\Rightarrow \frac{V_s^2 V_R}{B_2} \sin^2(\beta - \delta) - 2 \frac{A}{B_2} V_s V_R^2 \sin(\beta - \delta) - \sin(\beta - \alpha) +$$

$$\frac{V_s^2 V_R}{B_2} \cos^2(\beta - \delta) - 2 \frac{A}{B_2} V_s V_R^2 \cos(\beta - \alpha) \cos(\beta - \delta) = 0$$

$$\frac{V_s \cdot V_R}{B_2} \left[V_s - \sin^2(\beta - \delta) + V_s \cos^2(\beta - \delta) - 2A V_R \sin(\beta - \delta) \sin(\beta - \alpha) \right.$$

$$\left. - 2A V_R \cos(\beta - \delta) \cos(\beta - \alpha) \right] = 0$$

$$V_s \left[\sin^2(\beta - \delta) + \cos^2(\beta - \delta) \right] - 2AV_r \left[\sin(\beta - \delta)\sin(\beta - \alpha) + \cos(\beta - \delta)\cos(\beta - \alpha) \right] = 0$$

$$V_s - 2AV_r \cos(\beta) = 0$$

$$V_s = 2AV_r \cos(\alpha - \delta)$$

$$V_r = \frac{V_s}{2A \cos(\alpha - \delta)}$$

Where V_r is the critical voltage.

$$\therefore V_{R \text{ CRIT}} = \frac{V_s}{2A \cdot \cos(\alpha - \delta)} \quad (2.63)$$

To find the critical load angle ,
we know that ,

$$Q_r = P_r \tan \phi$$

$$Q_r = P_r \frac{\sin \phi}{\cos \phi}$$

Where $\cos \phi$ is the load power factor

Then $\tan \phi = Q_r / P_r$

Substituting,

$$\tan \phi = \frac{\frac{V_s V_r}{B} \sin(\beta - \delta) - \frac{A}{B} V_r^2 \sin(\beta - \alpha)}{\frac{V_s V_r}{B} \cos(\beta - \delta) - \frac{A}{B} V_r^2 \cos(\beta - \alpha)}$$

Substituting the value of $V_{R \text{ CRT}}$ from equation (2.63) we get.

$$\begin{aligned} \text{TAN } \phi &= \frac{\frac{V_s^2 \text{ SIN}(\beta - \delta)}{2AB \text{ COS}(\alpha - \delta)} - \frac{A V_s^2 \text{ SIN}(\beta - \alpha)}{4A^2B \text{ COS}^2(\alpha - \delta)}}{\frac{V_s^2 \text{ COS}(\beta - \delta)}{2AB \text{ COS}(\alpha - \delta)} - \frac{A V_s^2 \text{ COS}(\beta - \alpha)}{4A^2B \text{ COS}^2(\alpha - \delta)}} \\ &= \frac{\text{SIN}(\beta - \delta) \text{ COS}(\alpha - \delta) - \text{SIN}(\beta - \alpha)}{2 \text{ COS}(\beta - \delta) \text{ COS}(\alpha - \delta) - \text{COS}(\beta - \alpha)} \\ &= \frac{\text{SIN}(\beta + \alpha - 2\delta) + \text{SIN}(\beta - \delta - \alpha - \delta) - \text{SIN}(\beta - \alpha)}{\text{COS}(\beta - \delta + \alpha - \delta) + \text{COS}(\beta - \delta - \alpha + \delta) - \text{COS}(\beta - \alpha)} \\ &= \frac{\text{SIN}(\beta + \alpha - 2\delta) + \text{SIN}(\beta - \alpha) - \text{SIN}(\beta - \alpha)}{\text{COS}(\beta + \alpha - 2\delta) + \text{COS}(\beta - \alpha) - \text{COS}(\beta - \alpha)} \end{aligned}$$

$$\therefore \text{TAN } \phi = \text{TAN}(\beta + \alpha - 2\delta)$$

$$\Rightarrow \phi = \beta + \alpha - 2\delta$$

$$\therefore \delta = \frac{\alpha + \beta - \phi}{2}$$

where δ is the critical load angle.

$$\therefore \delta_{\text{CRT}} = \frac{\alpha + \beta - \phi}{2} \quad (2.64)$$

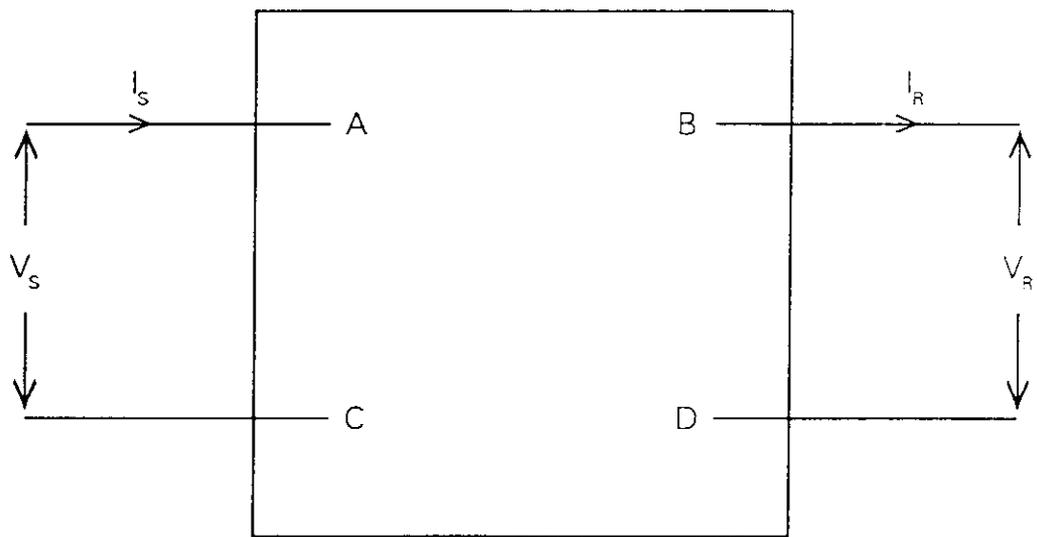


Fig 2.01

TWO PORT REPRESENTATION

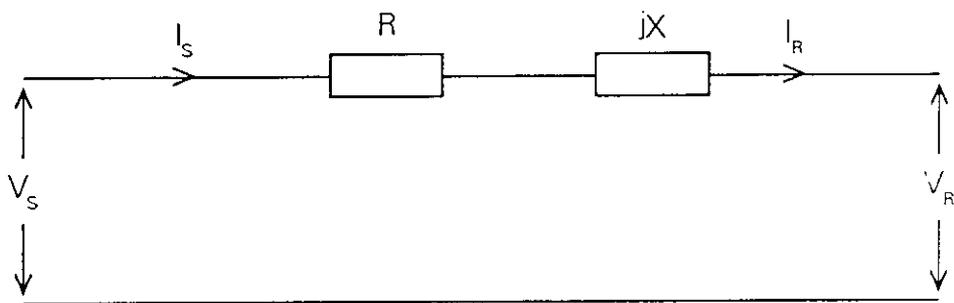


Fig 2.02

EQUIVALENT CIRCUIT OF SHORT LINE

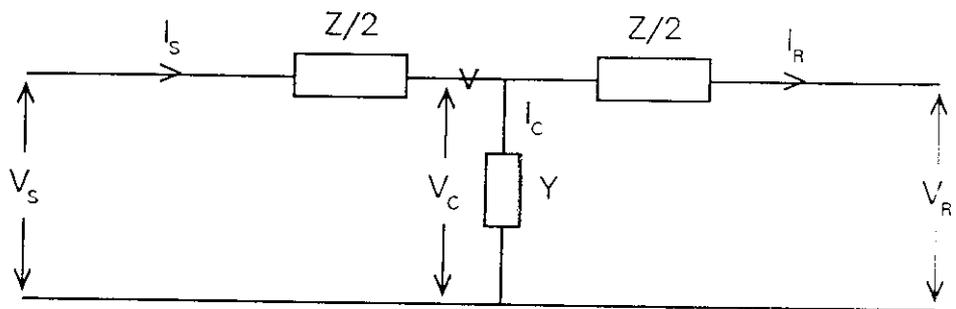


Fig 2.03

**EQUIVALENT CIRCUIT OF MEDIUM LINE
NOMINAL - T NETWORK**

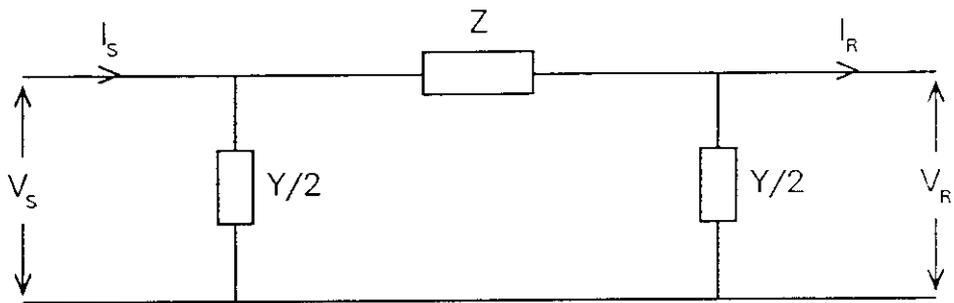


Fig 2.04

**EQUIVALENT CIRCUIT OF MEDIUM LINE
NOMINAL - π NETWORK**

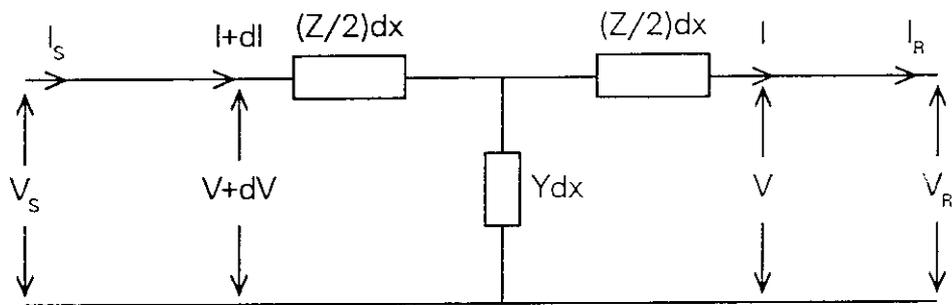


Fig 2.05

EQUIVALENT CIRCUIT OF LONG TRANSMISSION LINE

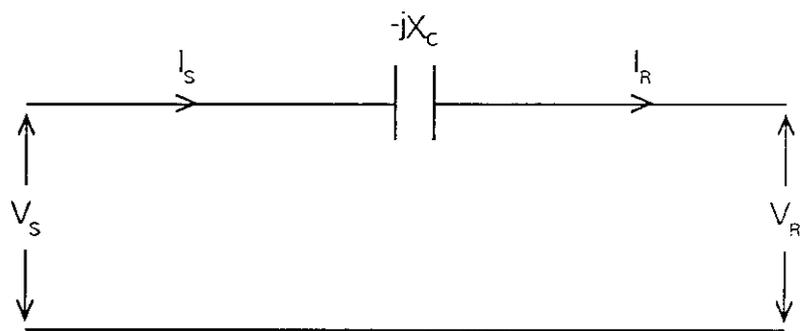


Fig 2.06

SERIES CAPACITOR NETWORK

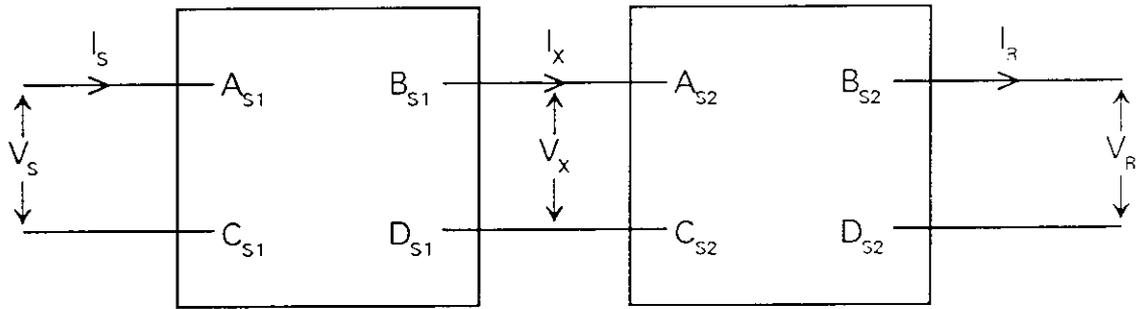


Fig 2.07

TWO PORT NETWORK CONNECTED IN SERIES



SERIES CAPACITOR COMPENSATION



CHAPTER 3

SERIES COMPENSATION

The stability requirement limits the permissible power on E.H.V. lines, which decreases with increase in the line length.

The implementation of series capacitor in long distance lines offer an effective and economical means of improving stability limits and permits the line to carry more power.

3.1. SERIES COMPENSATION FACTOR

The series compensation factor is defined as the ratio of the capacitive reactance of the series capacitor to the total inductive reactance of the line.

If X_c is the reactance of the capacitor and X_L is the total reactance of the transmission line, then

$$\text{Series compensation factor} = \frac{X_c}{X_L}$$

3.2. PRINCIPAL OF SERIES COMPENSATION

3.2.1. POWER TRANSFERABILITY OF AN UN-COMPENSATED E.H.V - A.C TRANSMISSION SYSTEM

Consider an E.H.V transmission line as shown in the figure (3.01).

Let V_s be the sending end voltage and V_r be the receiving end voltage and δ be the load angle or transmission angle.

Let X_L be the series reactance of the transmission line (all values in P.U.)

Power transferability of the a.c transmission system is given by the equation

$$P_{ac} = \frac{V_s \cdot V_r}{X_L} \cdot \sin \delta$$

For analysis purpose, let V_s and V_r be kept at 1 p.u. and the value of the load angle δ be take as 90 degrees. Then the equation reduces to

$$P_{ac} \propto \frac{1}{X_L}$$

Hence the series reactance X_L is inversely proportional to the power transferability and directly proportional to the length of the line. Now it becomes essential to reduce X_L , for which we go for series compensation.

3.2.2. POWER TRANSFERABILITY OF SERIES COMPENSATED E.H.V - A.C TRANSMISSION SYSTEM

The power transferability can be increased by reducing the equivalent series reactance X_L of the line by installing the series capacitors having reactance X_C .

Consider a series capacitor bank installed on the E.H.V. transmission line as shown in the figure (3.02).

By introducing series capacitor banks in series with the A.C. lines, the effective series reactance X_L of the A.C. line is reduced to

$$X_L' = X_L - X_C$$

Where X_L' is the equivalent series reactance of the line, after installing series capacitors.

X_L is the series inductive reactance of the line, without series capacitive reactance X_C .

X_C is the series capacitive reactance of the capacitor bank.

Hence the power transferability equation reduces to

$$P_{ac} \propto \frac{1}{X_L'}$$

$$\text{ie.... } P_{ac} \propto \frac{1}{X_L - X_C}$$

Now by increasing the value of the series capacitive reactance (X_c), the net equivalent reactance of the line i.e., ($X_L - X_c$) can be reduced and the power transferability can be increased.

Hence power flow is given by,

$$P_{ac} = \frac{V_s \cdot V_R}{X_L - X_c} \cdot \sin \delta$$

By choosing series compensation factor as K, then $\frac{X_c}{X_L} = K$

$$\therefore X_c = K \cdot X_L$$

Substituting in equation

$$P_{ac} = \frac{V_s \cdot V_R}{X_L - X_L \cdot K} \cdot \sin \delta$$

$$\text{ie., } P_{ac} = \frac{V_s \cdot V_R}{(1-K) \cdot X_L} \cdot \sin \delta$$

Usually 40% to 60% of the X_L is compensated by the series capacitor.

For 50% compensation, the value of $K = 0.5$

Then

$$P_{ac} = \frac{V_S \cdot V_R}{0.5 \cdot X_L} \cdot \sin \delta$$

$$\therefore P_{ac} = \frac{2 V_S \cdot V_R}{X_L} \cdot \sin \delta$$

Power flow is doubled by 50% compensation of the series reactance.

3.3. COMPENSATION SCHEMES

Two types of compensation schemes are implemented. They are

3.3.1. Single capacitor compensation

3.3.2. Twin capacitor compensation

In single capacitor compensation scheme the capacitor is located at

3.3.1.1. sending end

3.3.1.2. receiving end

3.3.1.3. centre

and the performance of the line was studied.

In twin capacitor compensation scheme the capacitor was located at

3.3.2.1. Capacitor at both ends.

3.3.2.2. Capacitor at one-third end locations.

and the performance of the line was studied.

3.4. ANALYSIS OF SERIES COMPENSATED TRANSMISSION SYSTEMS

For analysis the total compensation line was divided into a number of sections and ABCD line constants of the individual sections was determined . The total ABCD constants of the line was obtained by connecting all the sections in series as explained in section (2.5).

3.5. EVALUATION OF ABCD CONSTANTS OF COMPENSATED LINE

The circuit configuration and process followed to determine the total ABCD constants of the transmission line for the different compensating schemes are as given below.

3.5.1. SINGLE CAPACITOR CONFIGURATION

3.5.1.1. Capacitor Located At Sending End

The ABCD constants of the compensating capacitor is A_x, B_x, C_x, D_x and that of the transmission line is A_1, B_1, C_1, D_1 . The total ABCD constants of the compensated line ie. A_o, B_o, C_o, D_o . is obtained by multiplying the ABCD constants (A_x, B_x, C_x, D_x) of the compensating network with the ABCD constants (A_1, B_1, C_1, D_1) of the transmission line.

The net ABCD constants A_o, B_o, C_o, D_o . of all the above compensating network schemes have been calculated referring to section (2.5).

3.5.1.2. Capacitor At Receiving End

The total ABCD constants of the compensated line is obtained by the product of the ABCD constants of the line (A_1, B_1, C_1, D_1) and the ABCD constants of the compensating network (A_x, B_x, C_x, D_x) .

3.5.1.3. Capacitor At Centre

The total ABCD constants of the compensated line (A_o, B_o, C_o, D_o) is obtained by the triple product of the ABCD constants of the half-line, the ABCD Constants of the compensating network and the ABCD constants of the other half of the line.

3.5.2. TWIN CAPACITOR COMPENSATION

3.5.2.1. Capacitor Located At Both The Ends

The total ABCD constants of the compensated line (A_o, B_o, C_o, D_o) is obtained as follows.

The ABCD constants of the compensating network (A_o, B_o, C_o, D_o) is multiplied with that of the transmission line (A_x, B_x, C_x, D_x) . This value is again multiplied with the ABCD constants of the compensation network (A_x, B_x, C_x, D_x) .

3.5.2.2. Capacitor at one third location

The total ABCD constants of the compensated line (A_o, B_o, C_o, D_o) is obtained by the product of ABCD constant of line (A_1, B_1, C_1, D_1) with ABCD constants of the compensation network (A_x, B_x, C_x, D_x). this is now multiplied with the ABCD constants of the line (A_1, B_1, C_1, D_1) and the whole is now multiplied with the ABCD constant of the compensation network (A_x, B_x, C_x, D_x). The whole expression is now multiplied with the ABCD constants of the line (A_1, B_1, C_1, D_1).

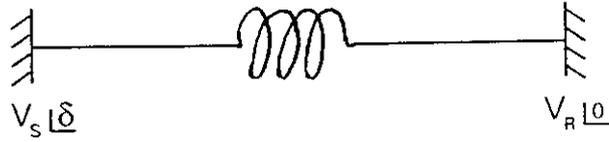


Fig 3.01

UN-COMPENSATED TRANSMISSION LINE

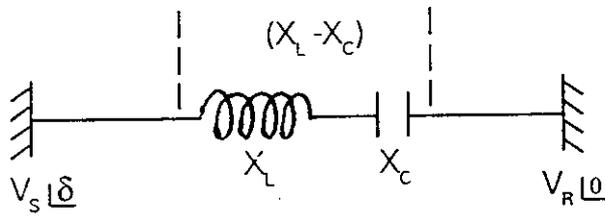


Fig 3.02

SERIES CAPACITOR COMPENSATED TRANSMISSION LINE



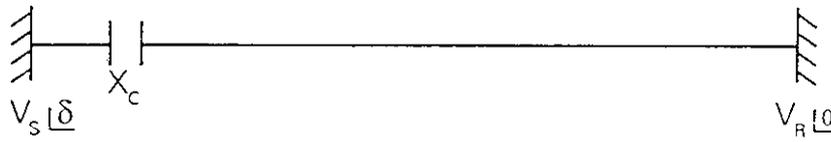


Fig 3.03

SERIES CAPACITOR LOCATED AT SENDING END



Fig 3.04

SERIES CAPACITOR LOCATED AT RECEIVING END

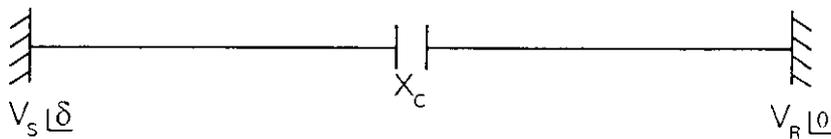


Fig 3.05

SERIES CAPACITOR LOCATED AT CENTRE

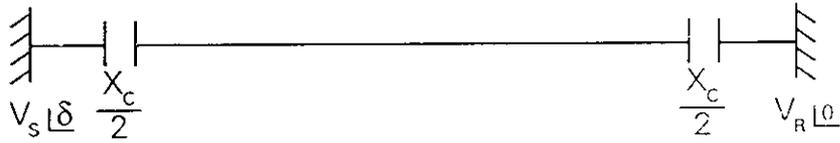


Fig 3.06

SERIES CAPACITORS LOCATED AT BOTH ENDS



Fig 3.07

SERIES CAPACITORS LOCATED AT ONE - THIRD DISTANCE FROM BOTH ENDS



EVALUATION OF PARAMETERS



CHAPTER 4

EVALUATION OF VARIOUS PARAMETERS

For each compensating network scheme, the value of compensating factor is varied from 10% to 60% to determine the line performance.

4.1. LINE CONSTANTS AND THEIR ASSUMPTIONS

For analysis the system having following constants was considered,

- a. Line length (D_L) = 400 KM
- b. Operating voltage = 400 KV
- c. Resistance of the line (R) = 0.274E-01
- d. Reactance of the line (X_L) = 0.332
- e. Susceptance of the line (BB) = 3.47E-06
- f. Conductance of the line (GG) = 0.0
- g. Base voltage = 400 KV
- h. Base MVA = 100

4.2. ASSUMPTION MADE IN THE ANALYSIS

Since the analysis is mainly for determining the effect and influence of series compensation on the line performance the terminal equipments with power

factors 0.8, 0.9 and 1.0 are only considered.

The terminal loading limits of the transmission line are not considered.

Under normal operating condition with the sending end voltage (V_S) taken as constant at 1 p.u. the value of $R = V_S/V_R$ was varied from 1.1 to 2.0 with incremental value of 0.1.

4.3. PARAMETERS CONSIDERED FOR ANALYSIS

4.3.1. POWER AT RECEIVING END (P_R)

The receiving end power of the transmission line was determined by using the equation (2.44) for various power factors 0.8, 0.9 and 1.0.

4.3.2. MAXIMUM POWER AT THE RECEIVING END ($P_{R \text{ MAX}}$)

The maximum receiving end power of the transmission line was determined by using the equation (2.48) of section 2.6.

4.3.3. EFFICIENCY OF THE SYSTEM

The efficiency of a system is an important factor for optimal operation of a system. The efficiencies of various compensation network locations was

calculated using the equation (2.50) in section 2.8.

4.3.4. CALCULATION OF B_0

From the expression of $P_{R\text{ MAX}}$ it is seen that the value of $P_{R\text{ MAX}}$ depends on V_S , V_R and B_0 , but in the system considered V_S and V_R are fixed. Hence the only variable which has any effect on the value $P_{R\text{ MAX}}$ is B_0 . Therefore the value of B_0 was determined for various compensation schemes.

4.3.5. CALCULATION OF $V_{R\text{ CRIT}}$ AND δ_{CRIT}

The critical receiving end voltage ($V_{R\text{ CRIT}}$) is the value below which the value of the receiving end power (P_R) decreases. Hence it is calculated using the equation (2.63) for various compensation schemes. The value of the critical load angle (δ_{CRIT}) is the value above which the value of the receiving end power (P_R) decreases and stability problems arise. Hence it is calculated using the equation (2.64) for various compensation schemes.

4.3.6. POWER ANGLE CHARACTERISTICS

The power angle characteristics of any electrical systems are useful for stability studies. Hence the power angle calculations are done by varying the value of delta (δ) from 10° to 90° for various compensation schemes.



**RESULTS AND
COMPARATIVE STUDY**



CHAPTER 5

TABULATION OF RESULTS AND COMPARATIVE STUDY

With the procedure described, the results obtained have been tabulated for the compensation network at various locations as from the point of view of.

- 5.1. P_R vs Compensation factor for power factors 0.8, 0.9 and 1.0.
- 5.2. $P_{R\text{ MAX}}$ vs Compensation factor.
- 5.3. Efficiency vs Compensation factor.
- 5.4. $|B_0|$ vs Compensation factor.
- 5.5. P_R vs δ
- 5.6. Effect of $V_{R\text{ CRIT}}$ and δ_{CRIT} on P_R and $P_{R\text{ MAX}}$.

5.1. VARIATIONS OF RECEIVING END POWER (P_R)

From the table no. (5.03) to (5.05) it is seen that, for each location the power transfer increases with the compensating factor. At low compensation, it has been seen that the value of P_R is practically independent of the type of the location of the series capacitor and at higher degree of compensation, it is also seen that the value of P_R is maximum when the series capacitor is located at the receiving end. It has been seen that the value of P_R is almost same when the capacitors are located at the centre, one third and both ends.

The value of P_R is lowest when the capacitor is located at sending end.

5.2. VARIATIONS OF $P_{R\text{ MAX}}$

From the table no. (5.01) and the graph no. (5.01) the following conclusions can be drawn.

The value of $P_{R\text{ MAX}}$ increases with the compensation factor for various positions of the series capacitor. At low compensating factor, the values of $P_{R\text{ MAX}}$ is almost same for all the positions of the series capacitors. As the compensating factor increases the location of series capacitor will be an important factor and should be taken into consideration. It is seen that the value of $P_{R\text{ MAX}}$ obtained is maximum when the series capacitor is located at one-third distance from both the ends. The value of $P_{R\text{ MAX}}$ at the center is slightly lower than that for the series capacitors located at one third distance from both ends and so for all practical purposes, it can be taken as the same. The value of $P_{R\text{ MAX}}$ for the sending end and the receiving end is the lowest and almost the same. when the capacitor is located at both ends, the values of $P_{R\text{ MAX}}$ is higher than that for the sending end or the receiving end but lower than that for the centre.

5.3. VARIATIONS OF THE EFFICIENCY

The table no. (5.06) to (5.08) and the graph no. (5.06) to (5.08) shows the variations of the efficiency with the compensation factor for the various positions of the series capacitor.

The efficiency is found to be decreasing with the increase in the series compensation factor. At lower degree of compensation factors, the value of the efficiency is the same irrespective of the type of location of the series capacitor. When the compensation factor is increased to higher degrees of compensation, it is seen that the maximum efficiency is got when a single series capacitor is located at the sending end of the transmission line. The efficiency is marginally lower when the capacitor is located at the centre, one third or at both ends of the transmission line. The least efficiency is got when the capacitor is located at the receiving end of the transmission line.

5.4. VARIATION OF B_0

The table no. (5.02) and the graph no. (5.02) shows the variations of $|B_0|$ with the compensation factors for various positions of the capacitor, which determines the power transfer capability of the line.

It is seen that the value of $|B_0|$ is inversely proportional to the compensation factor.

The transfer impedance $|B_0|$ is minimum, when the series capacitor is located at one-third distances from both the ends of the line. It is also seen that the value of $|B_0|$ is exactly the same for a given value of the compensation factor when the capacitor is located either at the receiving end or at the sending end.

It can also be seen that the value of $|B_0|$, when the capacitor is located at the centre is only slightly higher than that for the capacitor located at one third

distance and so it can be taken as the same.

The value of $|B_0|$ when twin capacitors are located at both ends of the transmission line is lower than that for the receiving end (or) sending end but higher than that of the centre.

5.5. VARIATIONS OF P_R WITH δ

The table nos. 5.09 to 5.13 shows the variation of P_R with δ . It is seen that the value of the receiving end power (P_R) increases with increase in the value of δ upto a certain value and thereafter it decreases. Also for the same value of δ , the value of P_R increases with increase in the compensation factor.

5.6. EFFECT OF $V_{R\text{ CRIT}}$ AND δ_{CRIT} ON P_R AND $P_{R\text{ MAX}}$

From the table nos. (5.14) & (5.15) it is seen that the critical values of $V_{R\text{ CRIT}}$ and δ_{CRIT} determine the maximum real power transfer limit of the transmission line. As the value of receiving end voltage (V_R) decreases below its critical value the value of load angle δ exceeds its critical value. Therefore, the value of P_R & $P_{R\text{ MAX}}$ starts decreasing.

TABULATION OF PRMAX

COMP FACTOR	SENDING END	RECEIVING END	CENTRE	BOTH ENDS	ONE-THIRD DISTANCE
Ø.1	1Ø.529	1Ø.545	1Ø.591	1Ø.542	1Ø.587
Ø.2	11.6Ø4	11.643	11.757	11.648	11.75
Ø.3	12.917	12.992	13.2Ø4	13.Ø21	13.199
Ø.4	14.553	14.684	15.Ø46	14.769	15.Ø49
Ø.5	16.637	16.864	17.458	17.Ø58	17.485
Ø.6	19.359	19.758	2Ø.725	2Ø.158	2Ø.8Ø4

TABLE NO. 5.01

TABULATION OF BM

COMP FACTOR	SENDING END	RECEIVING END	CENTRE	BOTH ENDS	ONE-THIRD DISTANCE
Ø.1	.Ø73232	.Ø73232	.Ø72855	.Ø73196	.Ø72885
Ø.2	.Ø65725	.Ø65725	.Ø64969	.Ø65578	.Ø65005
Ø.3	.Ø58228	.Ø58228	.Ø57095	.Ø57896	.Ø57111
Ø.4	.Ø50745	.Ø50745	.Ø49236	.Ø50158	.Ø49208
Ø.5	.Ø43285	.Ø43285	.Ø41401	.Ø42370	.Ø41306
Ø.6	.Ø35862	.Ø35862	.Ø33609	.Ø34552	.Ø33423

TABLE NO. 5.02

TABULATION OF PR VS COMPENSATION FOR 0.8 PF					
COMP FACTOR	SENDING END	RECEIVIN END	CENTRE	BOTH ENDS	ONE-THIRD DISTANCE
0.1	2.733	2.893	2.828	2.815	2.826
0.2	2.843	3.199	3.057	3.028	3.055
0.3	2.974	3.578	3.342	3.296	3.34
0.4	3.134	4.058	3.708	3.64	3.707
0.5	3.337	4.686	4.194	4.098	4.197
0.6	3.603	5.54	4.87	4.737	4.885

TABLE NO. 5.03

TABULATION OF PR VS COMPENSATION
FOR 0.9 PF

COMP FACTOR	SENDING END	RECEIVIN END	CENTRE	BOTH ENDS	ONE-THIRD DISTANCE
0.1	3.577	3.768	3.629	3.813	3.69
0.2	3.73	4.16	3.992	3.955	3.989
0.3	3.91	4.641	4.363	4.303	4.36
0.4	4.125	5.247	4.834	4.745	4.833
0.5	4.33	6.033	5.452	5.327	5.456
0.6	4.724	7.09	6.296	6.124	6.747

TABLE NO. 5.04

TABULATION OF PR VS COMPENSATION FOR 1.0 PF					
COMP FACTOR	SENDING END	RECEIVIN END	CENTRE	BOTH ENDS	ONE-THIRD DISTANCE
0.1	6.424	6.638	6.566	6.535	6.563
0.2	6.813	7.303	7.143	7.077	7.139
0.3	-	8.112	7.847	7.738	7.841
0.4	-	9.119	8.72	8.559	8.718
0.5	-	10.4	9.83	9.605	9.837
0.6	-	12.079	11.277	10.968	11.304

TABLE NO. 5.05

TABULATION OF EFFICIENCY VS COMPENSATION FOR 1.0 PF					
COMP FACTOR	SENDING END	RECEIVING END	CENTRE	BOTH ENDS	ONE-THIRD DISTANCE
0.1	94.28	93.97	94.13	94.13	94.13
0.2	93.99	93.3	93.63	93.63	93.63
0.3	-	92.5	93.04	93.04	93.03
0.4	-	91.51	92.31	92.31	92.3
0.5	-	90.29	91.4	91.4	91.37
0.6	-	88.74	90.23	90.23	90.18

TABLE NO. 5.06

TABULATION OF EFFICIENCY VS COMPENSATION FACTOR
FOR 0.8 PF

COMP FACTOR	SENDING END	RECEIVING END	CENTRE	BOTH ENDS	ONE-THIRD DISTANCE
0.1	96.97	96.62	96.79	96.8	96.79
0.2	96.88	96.11	96.49	96.49	96.49
0.3	96.77	95.49	96.11	96.11	96.1
0.4	96.63	94.71	95.61	95.62	95.61
0.5	96.44	93.72	94.97	94.97	94.95
0.6	96.19	92.39	94.07	94.07	94.03

TABLE NO. 5.07

TABULATION OF EFFICIENCY VS COMPENSATION FOR 0.9 PF					
COMP FACTOR	SENDING END	RECEIVING END	CENTRE	BOTH ENDS	ONE-THIRD DISTANCE
0.1	96.54	96.21	96.38	96.38	96.38
0.2	96.42	95.7	96.05	96.05	96.05
0.3	96.28	95.08	95.66	95.66	95.65
0.4	96.11	94.31	95.15	95.15	95.15
0.5	95.9	93.330	94.5	94.5	94.48
0.6	95.62	92.04	93.62	93.62	93.58

TABLE NO. 5.08

FOR CAPACITOR LOCATED AT SENDING END

COMP -> DELTA	Ø.Ø	Ø.1	Ø.2	Ø.3	Ø.4	Ø.5	Ø.6
1Ø	1.91	2.112	2.362	2.677	3.Ø86	3.639	4.423
2Ø	3.6Ø5	3.975	4.429	4.997	5.729	6.7Ø6	8.Ø66
3Ø	5.169	5.691	6.328	7.124	8.143	9.489	11.345
4Ø	6.556	7.2Ø9	8.ØØ3	8.991	1Ø.25	11.9Ø5	14.162
5Ø	7.723	8.481	9.4Ø2	1Ø.543	11.99	13.879	16.431
6Ø	8.634	9.47	1Ø.483	11.733	13.3Ø9	15.352	18.Ø83
7Ø	9.762	1Ø.146	11.213	12.523	14.167	16.28	19.Ø68
8Ø	9.587	1Ø.487	11.569	12.891	14.538	16.633	19.355
9Ø	9.6Ø1	1Ø.485	11.541	12.825	14.41	16.4Ø2	18.937

TABLE NO. 5.09

TABULATION OF PR VS DELTA
FOR CAPACTOR LOCATD AT RECEIVING ENDDDD

COMP -> DELTA ↓	0.0	0.1	0.2	0.3	0.4	0.5	0.6
10	1.91	2.128	2.4	2.751	3.218	3.866	4.822
20	3.605	3.99	4.467	5.071	5.861	6.933	8.465
30	5.169	5.707	6.367	7.198	8.273	9.716	11.744
40	6.556	7.274	8.042	9.065	10.381	12.132	14.561
50	7.723	8.497	9.441	10.615	12.121	14.106	16.83
60	8.634	9.486	10.522	11.807	13.44	15.579	18.482
70	9.762	10.161	11.251	12.597	14.298	16.507	19.467
80	9.587	10.503	11.608	12.965	14.669	16.89	19.755
90	9.501	10.5	11.58	12.899	14.541	16.629	19.336

TABLE NO. 5.10

TABULATION OF PR VS DELTA

FOR CAPACITOR LOCATED AT CENTRE

COMP -> DELTA↓	0.0	0.1	0.2	0.3	0.4	0.5	0.6
10	1.91	2.131	2.409	2.769	3.253	3.935	4.96
20	3.605	4.003	4.5	5.135	5.976	7.136	8.832
30	5.169	5.728	6.422	7.303	8.459	10.039	12.313
40	6.556	7.254	8.116	9.207	10.629	12.559	15.296
50	7.723	8.533	9.531	10.788	12.419	14.611	17.69
60	8.634	9.527	10.624	12	13.744	16.14	19.424
70	9.262	10.206	11.361	12.804	14.654	17.098	20.443
80	9.587	10.549	11.721	13.179	15.032	17.456	20.718
90	9.501	10.546	11.693	13.109	14.895	17.202	20.24

TABLE NO. 5.11

TABULATION OF PF VS DELTA
FOR CAPACITOR LOCATED AT BOTH ENDS

COMP -> DELTA ↓	Ø.Ø	Ø.1	Ø.2	Ø.3	Ø.4	Ø.5	Ø.6
1Ø	1.91	2.121	2.387	2.731	3.193	3.845	4.824
2Ø	3.6Ø5	3.985	4.458	5.Ø64	5.866	6.973	8.591
3Ø	5.169	5.7Ø2	6.362	7.7Ø2	8.3Ø4	9.8Ø9	11.976
4Ø	6.556	7.22	8.Ø4	9.Ø79	1Ø.434	12.269	14.878
5Ø	7.723	8.493	9.442	1Ø.639	12.191	14.276	17.2Ø7
6Ø	8.634	9.483	1Ø.525	11.833	13.521	15.771	18.893
7Ø	9.262	1Ø.158	11.256	12.627	14.385	16.7Ø7	19.884
8Ø	9.587	1Ø.5	11.612	12.995	14.755	17.Ø56	2Ø.152
9Ø	9.5Ø1	1Ø.49	11.584	12.927	14.621	16.8Ø8	19.686

TABLE NO. 5.12

TABULATION OF PR VS DELTA

FOR CAPAOR LOCATED AT ONE-THIRD DISTANCE FROM BOTH ENDSHE ENDS

COMP -> DELTA ↓	Ø.Ø	Ø.1	Ø.2	Ø.3	Ø.4	Ø.5	Ø.6
1Ø	1.91	2.13	2.4Ø8	2.769	3.256	3.946	4.992
2Ø	3.6Ø5	4.ØØ2	4.498	5.134	5.979	7.153	8.883
3Ø	5.169	5.726	6.418	7.3Ø1	8.464	1Ø.Ø61	12.378
4Ø	6.556	7.751	8.111	9.7Ø4	1Ø.634	12.582	15.372
5Ø	7.723	8.529	9.525	1Ø.784	12.424	14.639	17.773
6Ø	8.634	9.523	1Ø.617	11.995	13.779	16.17	19.5Ø9
7Ø	9.762	1Ø.2Ø2	11.355	12.799	14.658	17.177	2Ø.527
8Ø	9.587	1Ø.545	11.714	13.172	15.Ø35	17.483	2Ø.796
9Ø	9.5Ø1	1Ø.542	11.686	13.1Ø3	14.898	17.225	2Ø.3Ø7

TABLE NO. 5.13

TABULATION OF VRCRIT

COMP FACTOR	SENDING END	RECEIVING END	CENTRE	BOTH END	ONE-THIRD DISTANCE
0.0	.60	.60	.60	.60	.60
0.1	.59	.60	.60	.60	.60
0.2	.58	.60	.59	.59	.59
0.3	.56	.60	.58	.58	.58
0.4	.55	.60	.57	.57	.57
0.5	.54	.59	.56	.56	.56
0.6	.53	.59	.55	.55	.55

TABLE NO. 5.14

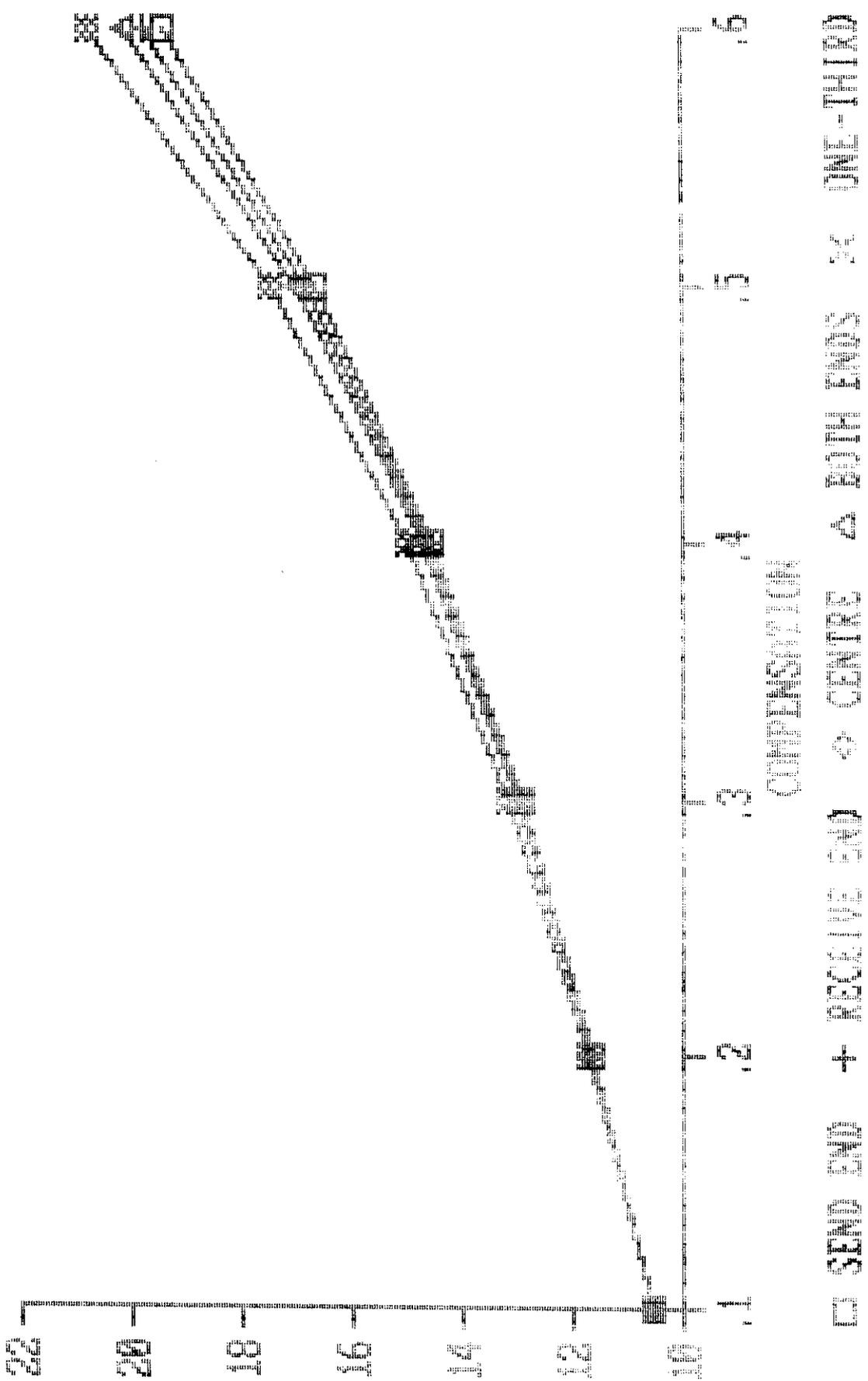
TABULATION OF DELCRIT					
COMP FACTOR	SENDING END	RECEIVING END	CENTRE	BOTH ENDS	ONE-THIRD DISTANCE
0.0	24.514	24.514	24.514	24.514	24.514
0.1	24.252	24.255	24.252	24.252	24.252
0.2	23.930	23.936	23.927	23.927	23.925
0.3	23.527	23.536	23.513	23.512	23.508
0.4	23.006	23.017	22.966	22.966	22.956
0.5	22.305	22.319	22.214	22.213	22.190
0.6	21.315	21.332	21.111	21.110	21.060

TABLE NO. 5.15

10
20
30
40
50
60
70
80
90
100

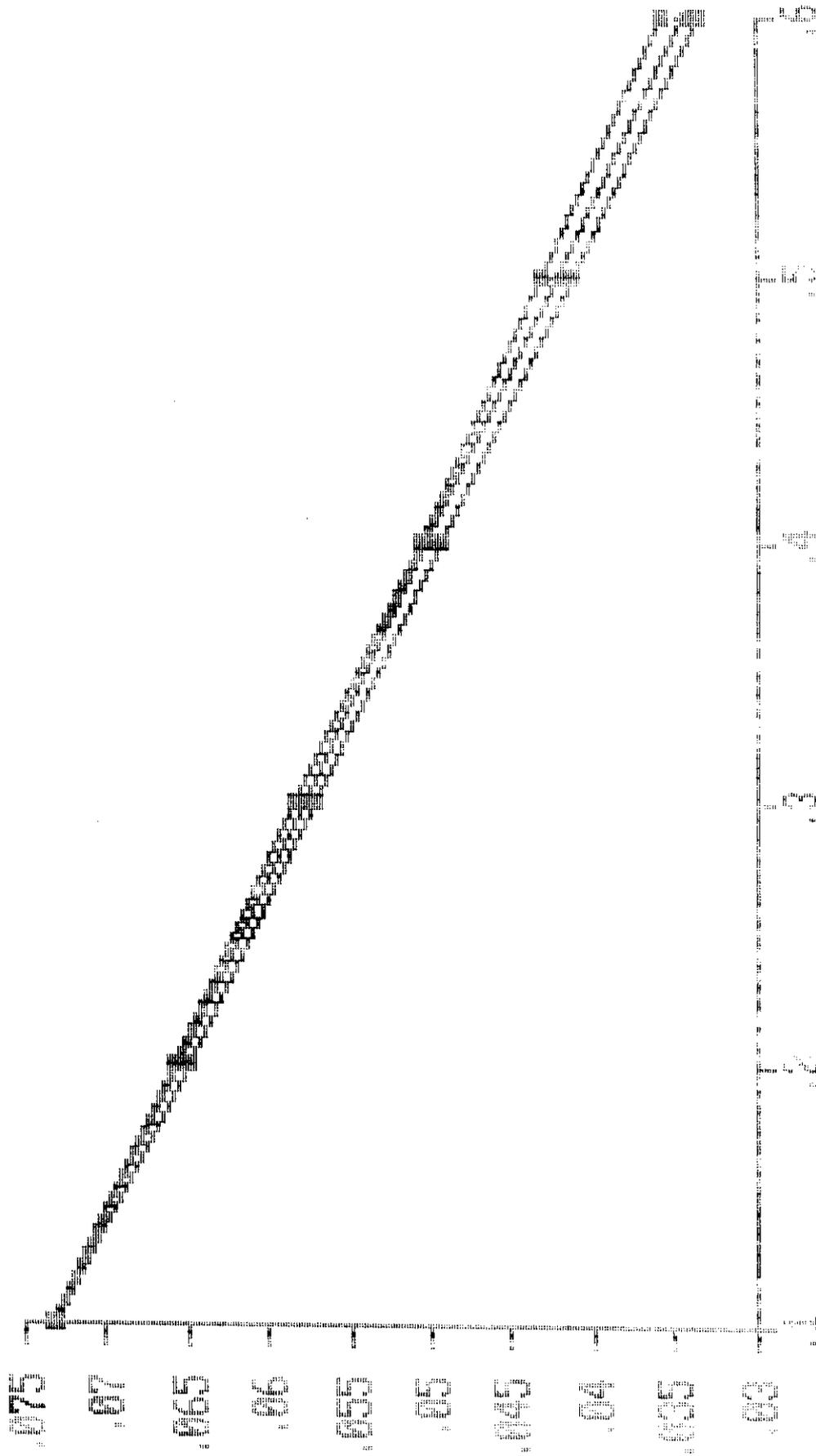
100
90
80
70
60
50
40
30
20
10
0

PERCENT



GRAPH NO. 5.01

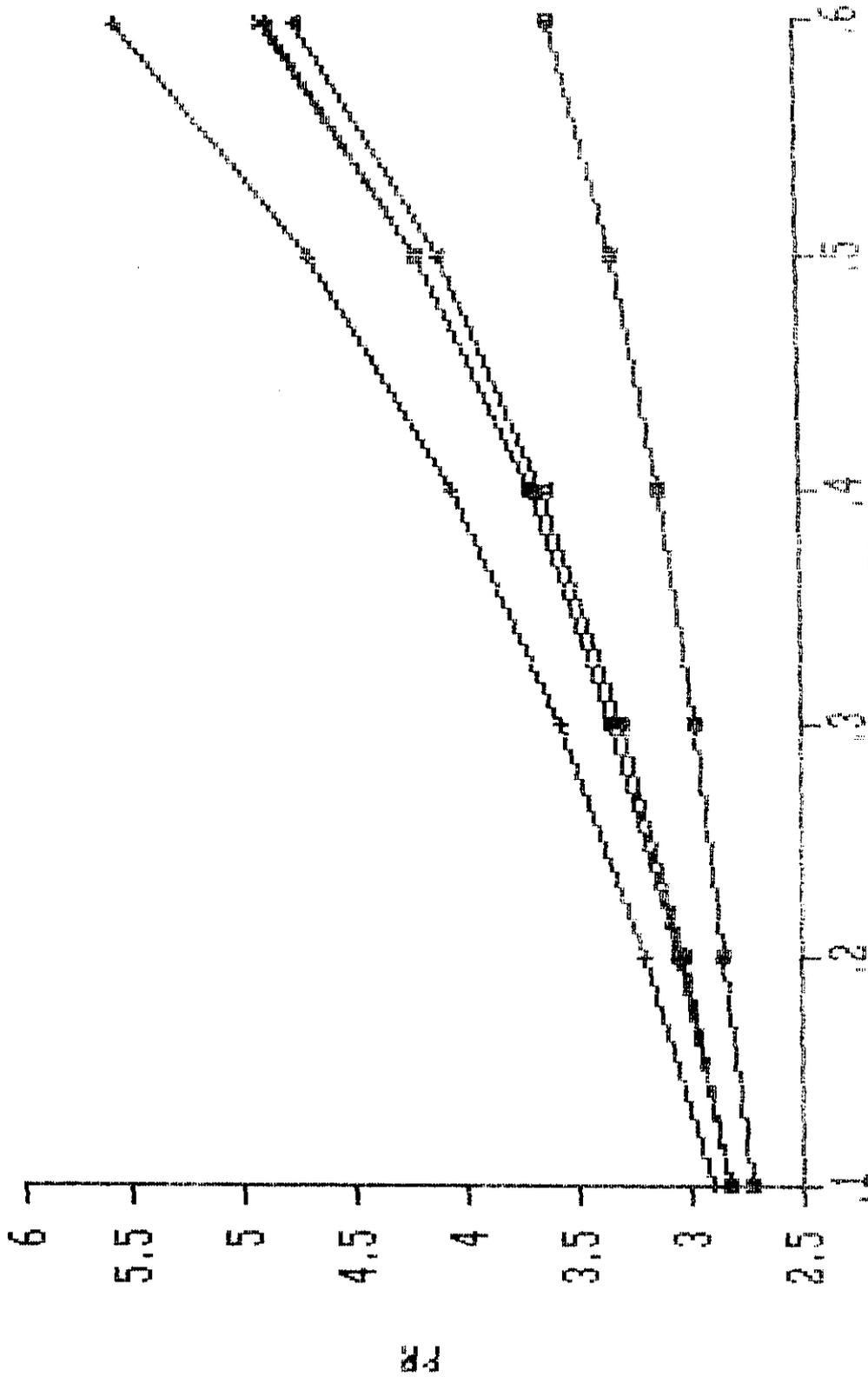
PLS CORRELATION



PLS CORRELATION

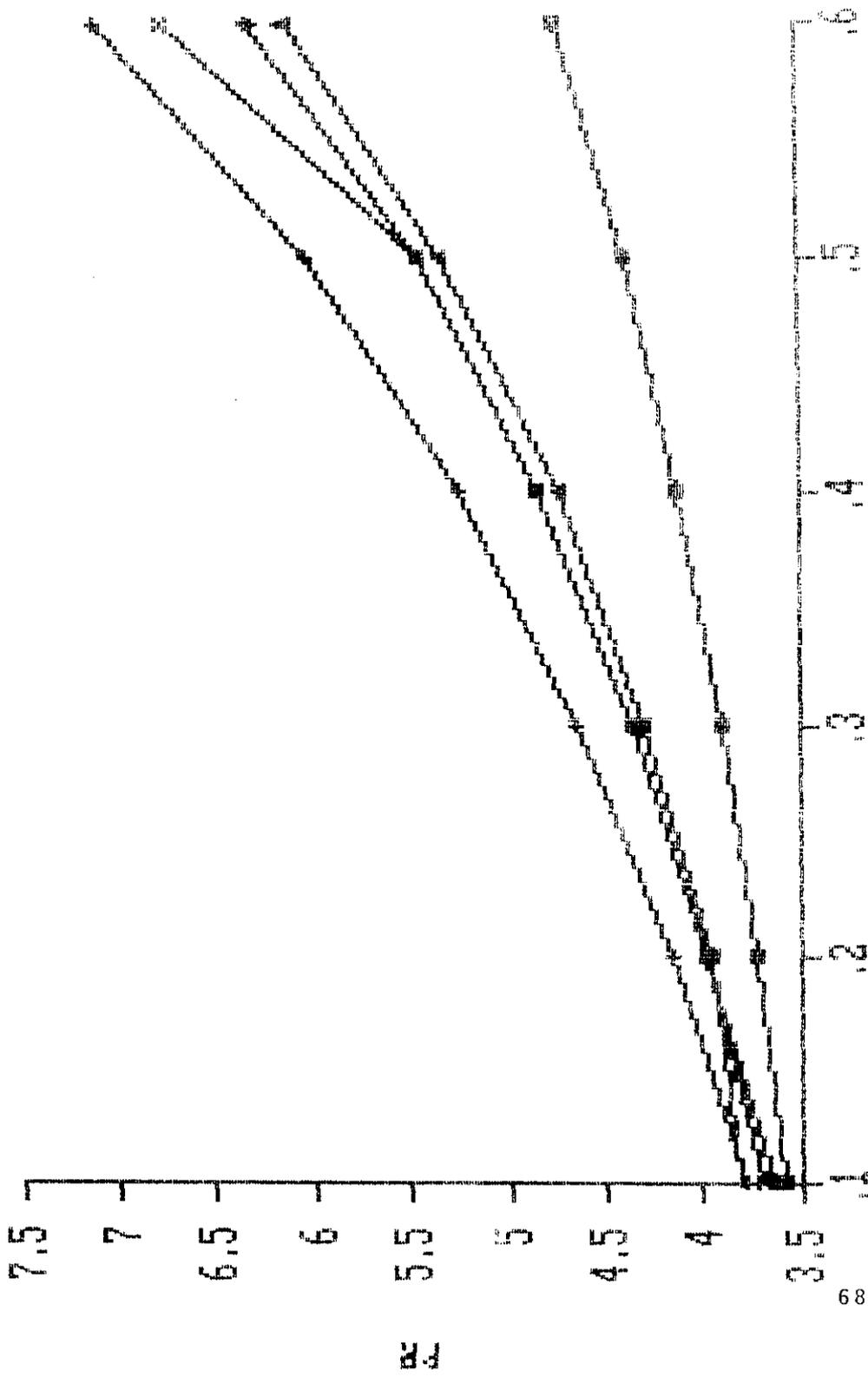
GRAPH NO. 5.02

PR VS COMP
FOR 0.8 PE



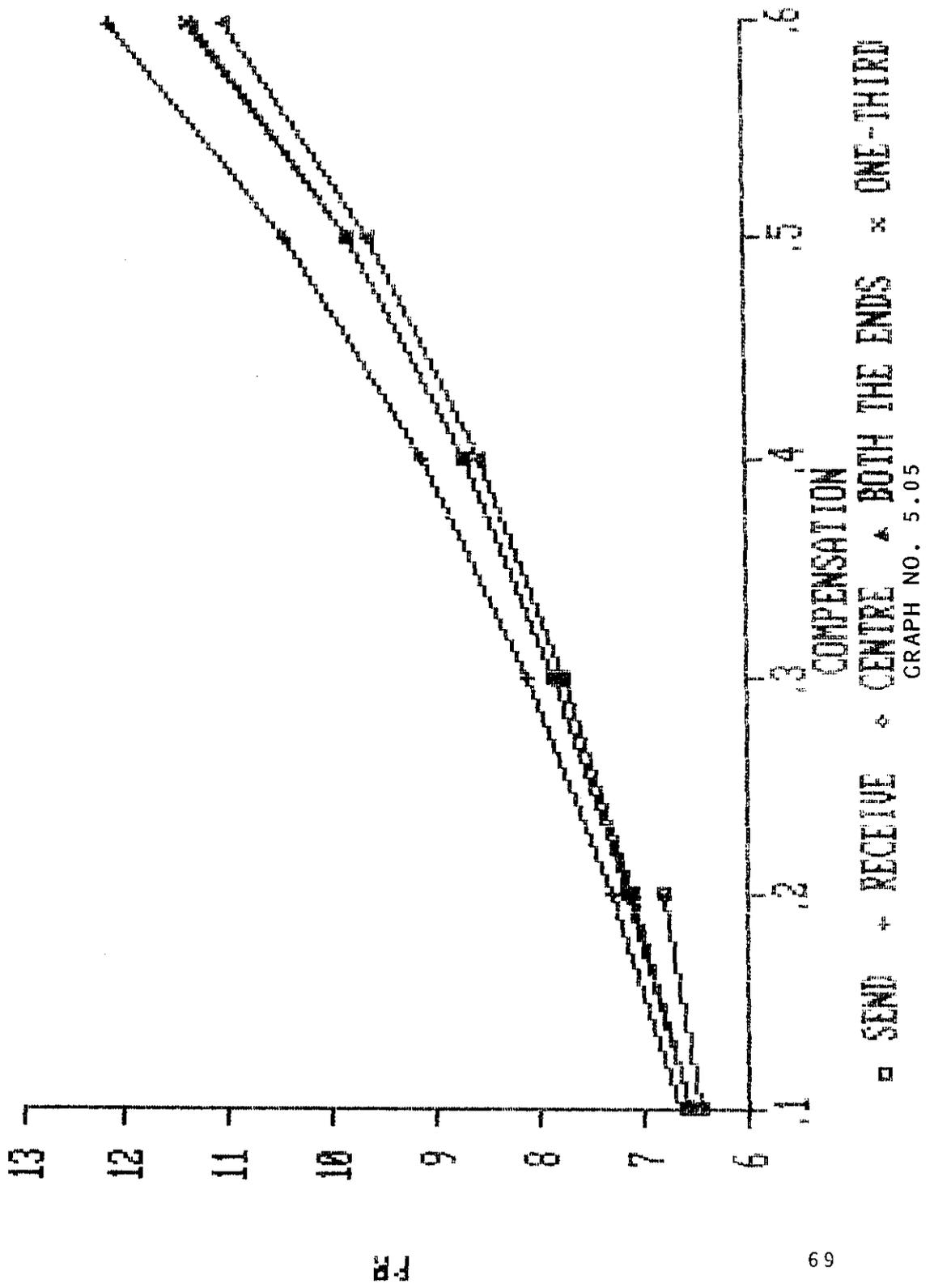
□ SEND + RECEIVE • CENTRE ▲ BOTH THE ENDS × ONE-THIRD
COMPENSATION
GRAPH NO. 5.03

PR VS COMP
FOR 0.9 COMP

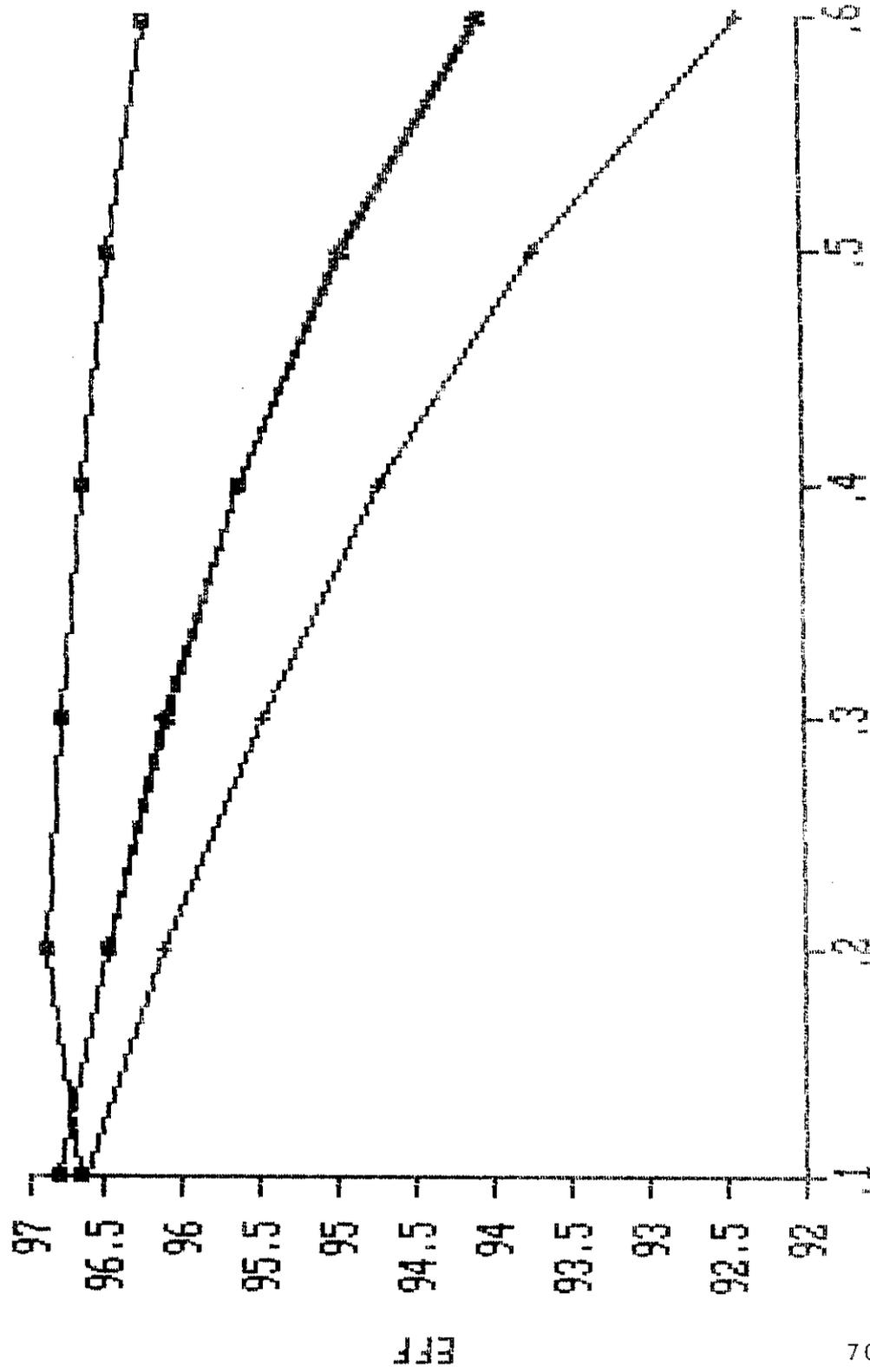


COMPENSATION
 □ SEND + RECEIVE ◆ CENTRE ▲ BOTH THE ENDS × ONE-THIRD
 GRAPH NO. 5.04

PR VS COMP
FOR 1.0 PF

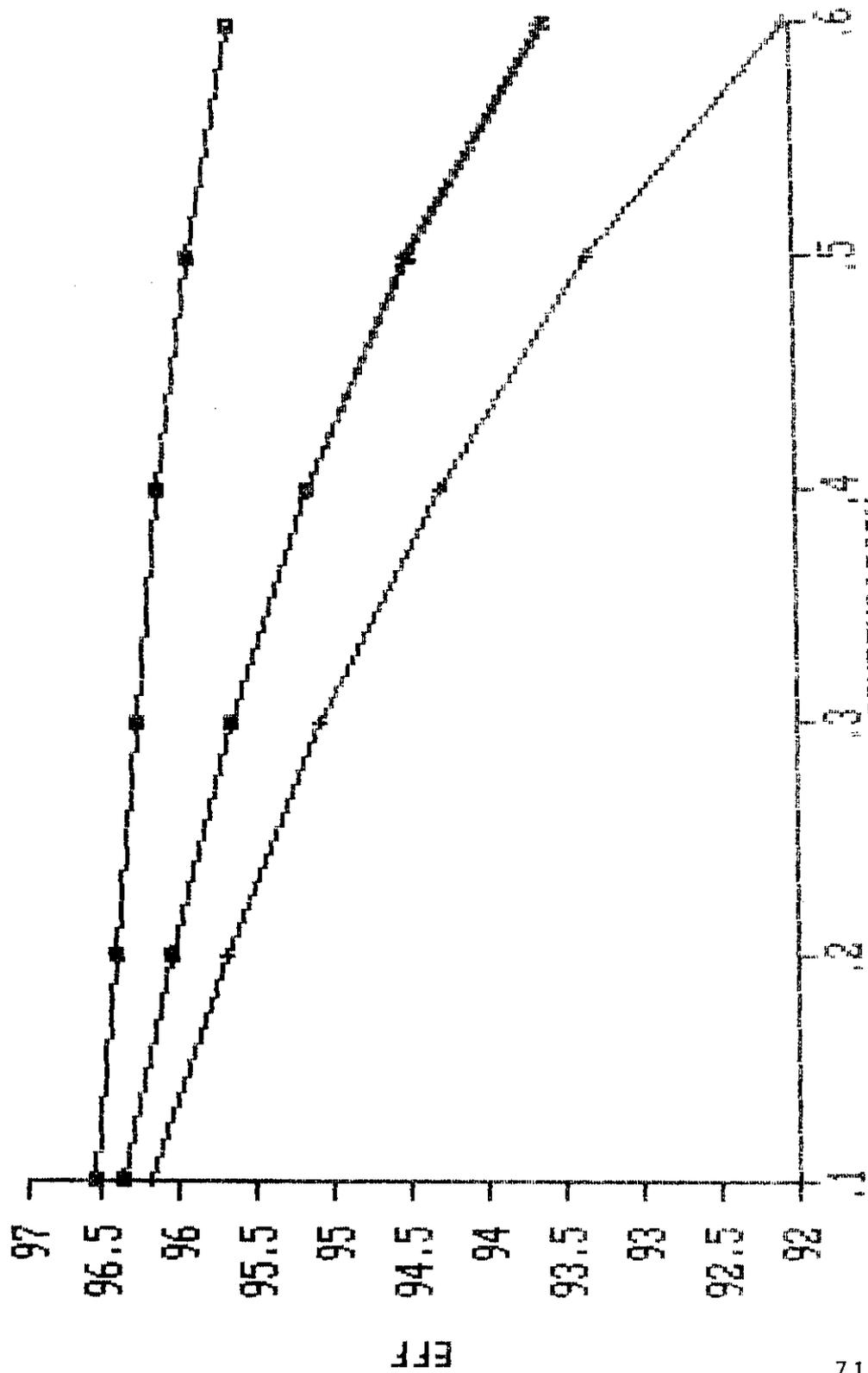


EFF VS COMP
FOR VARIOUS POSITIONS

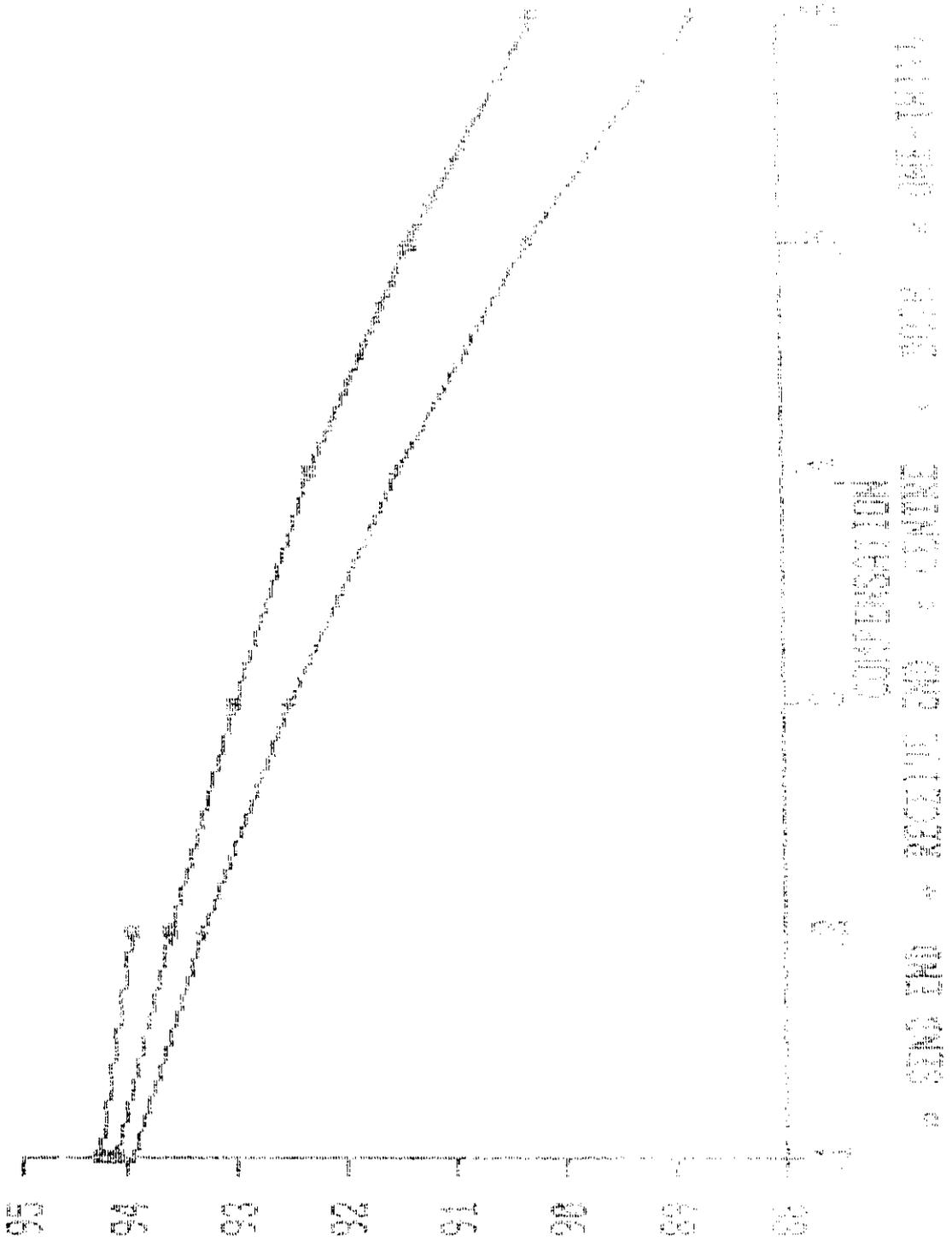


COMPENSATION
 □ SENDING END + RECEIVING END ◊ CENTRE ▲ BOTH THE ENDS × ONE-1
 GRAPH NO. 5.06

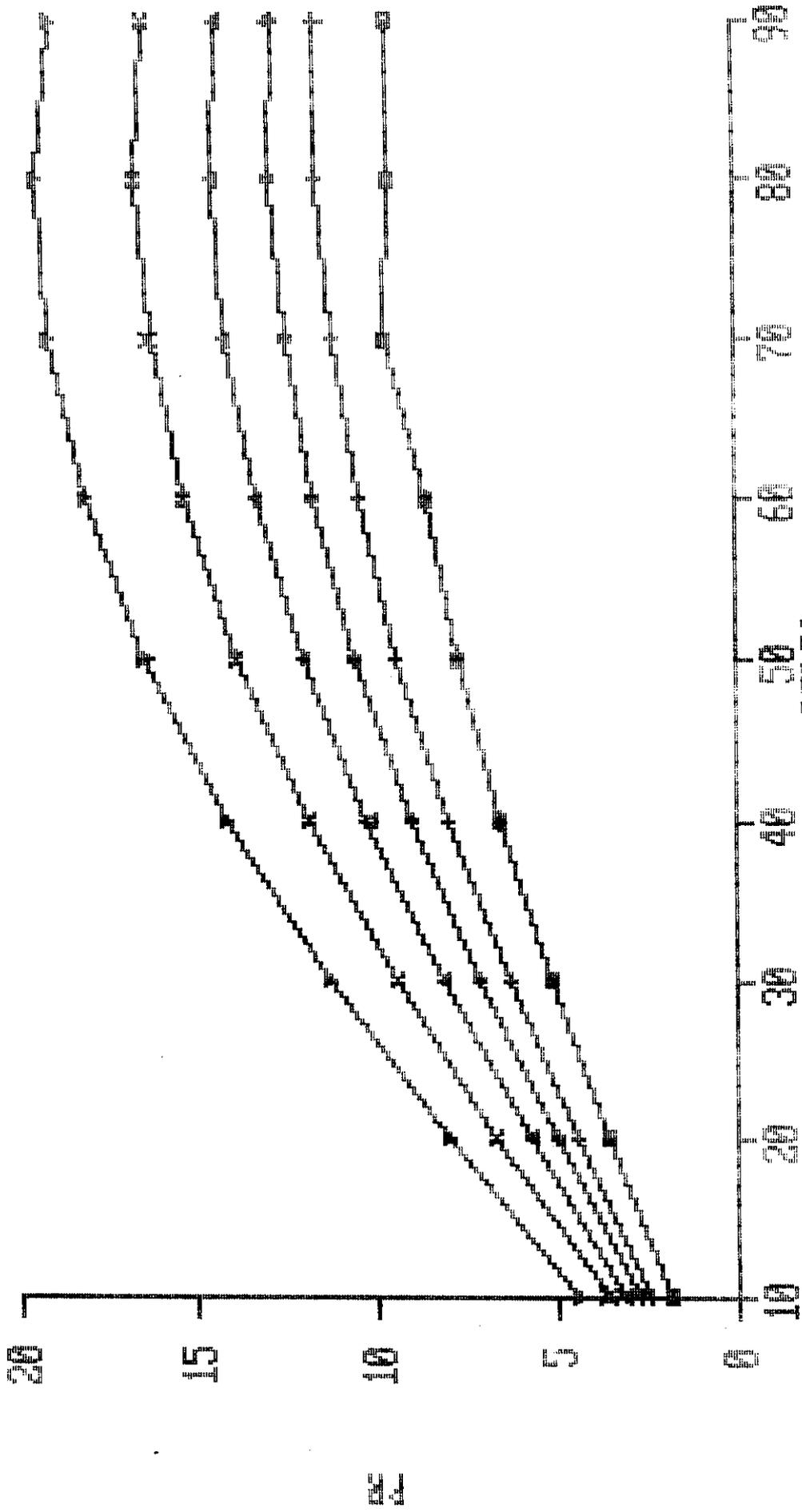
EFF VS COMP
FOR 0.9 PF



11 2 03
103 1 0 01



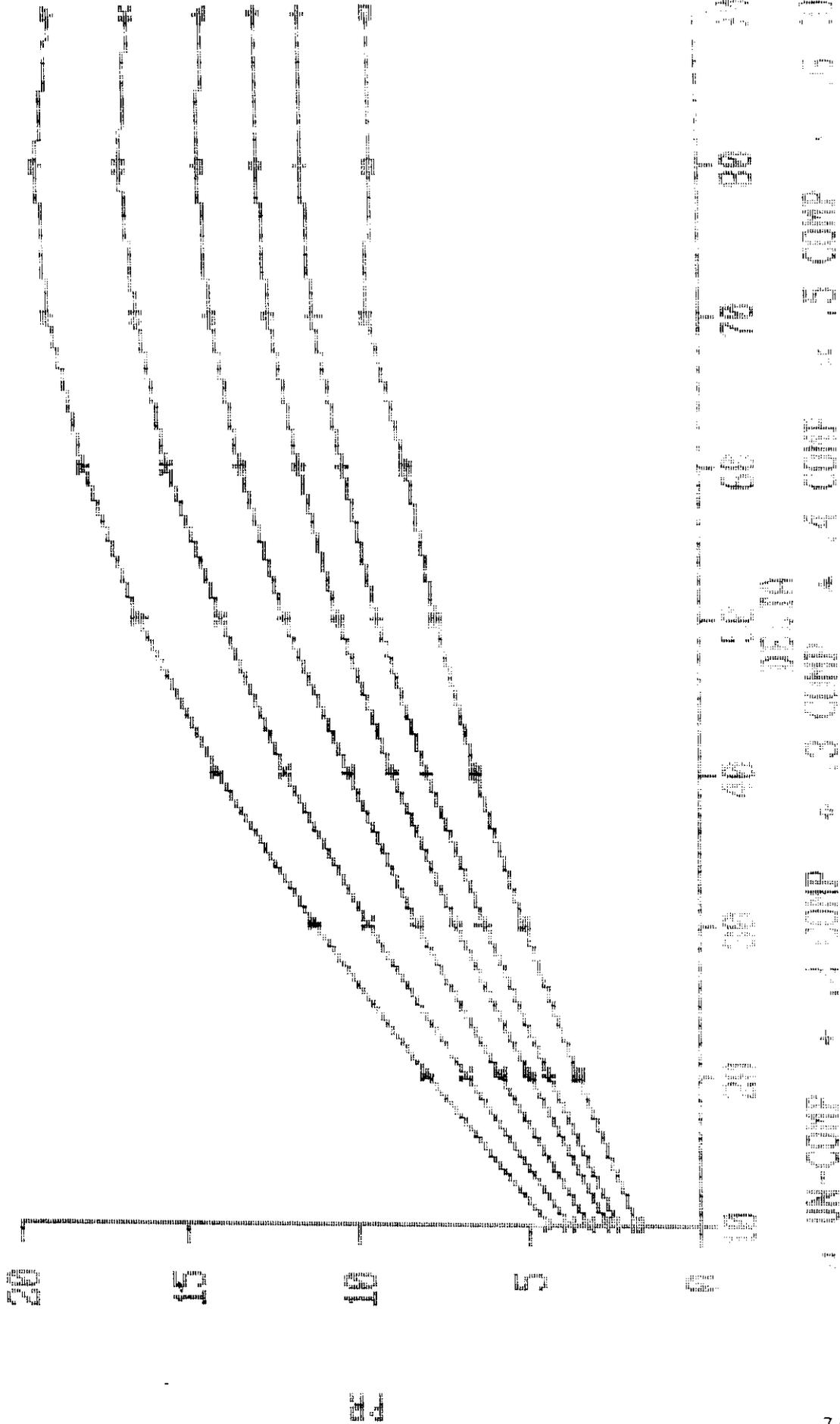
PR VS DELTA
FOR SENDING END



UNCOMPENSATED + 2 COMP + 3 COMP + 4 COMP + 5 COMP

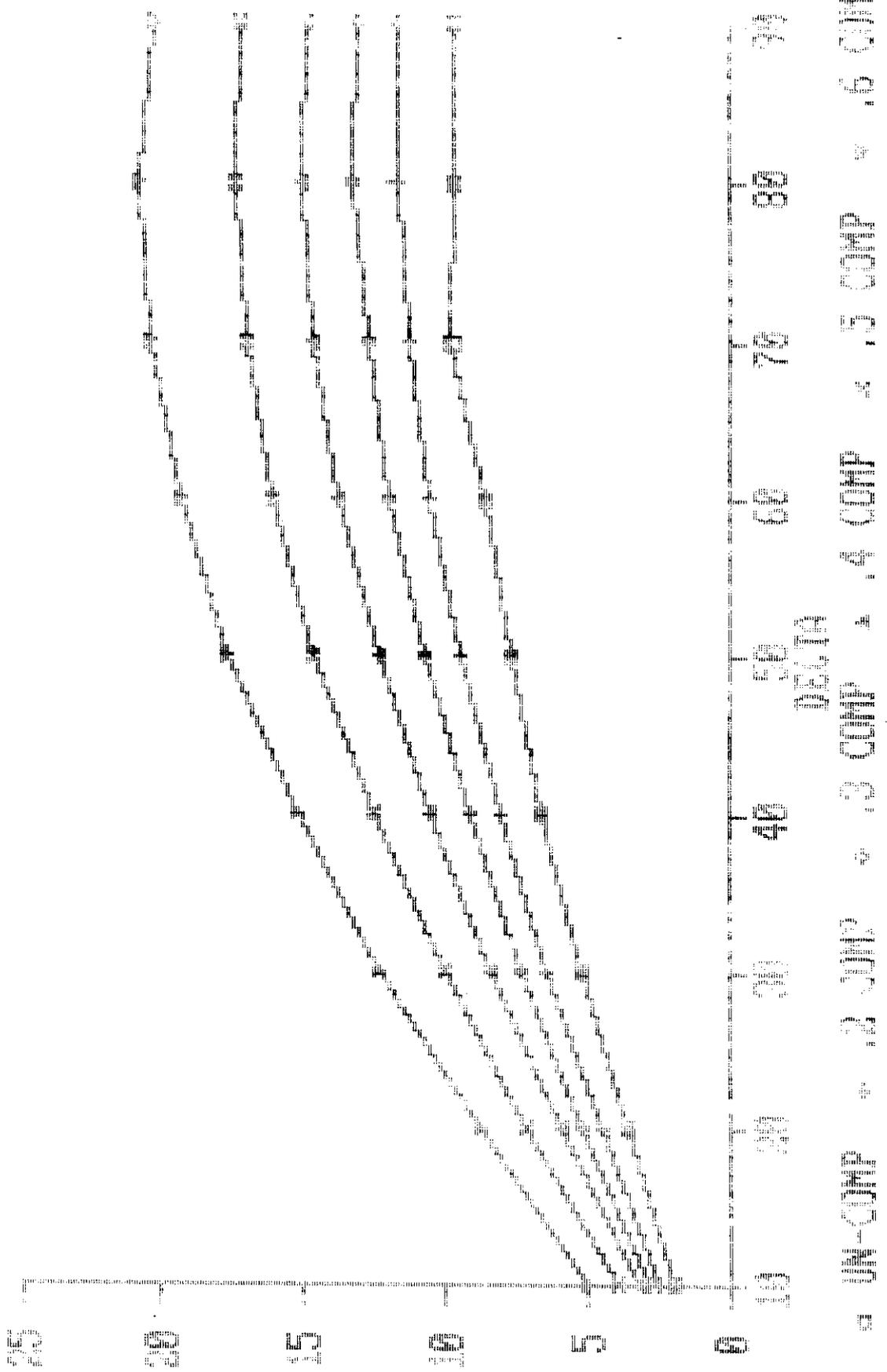
GRAPH NO. 5.09

RUS DELTA FOR REVIEW AND



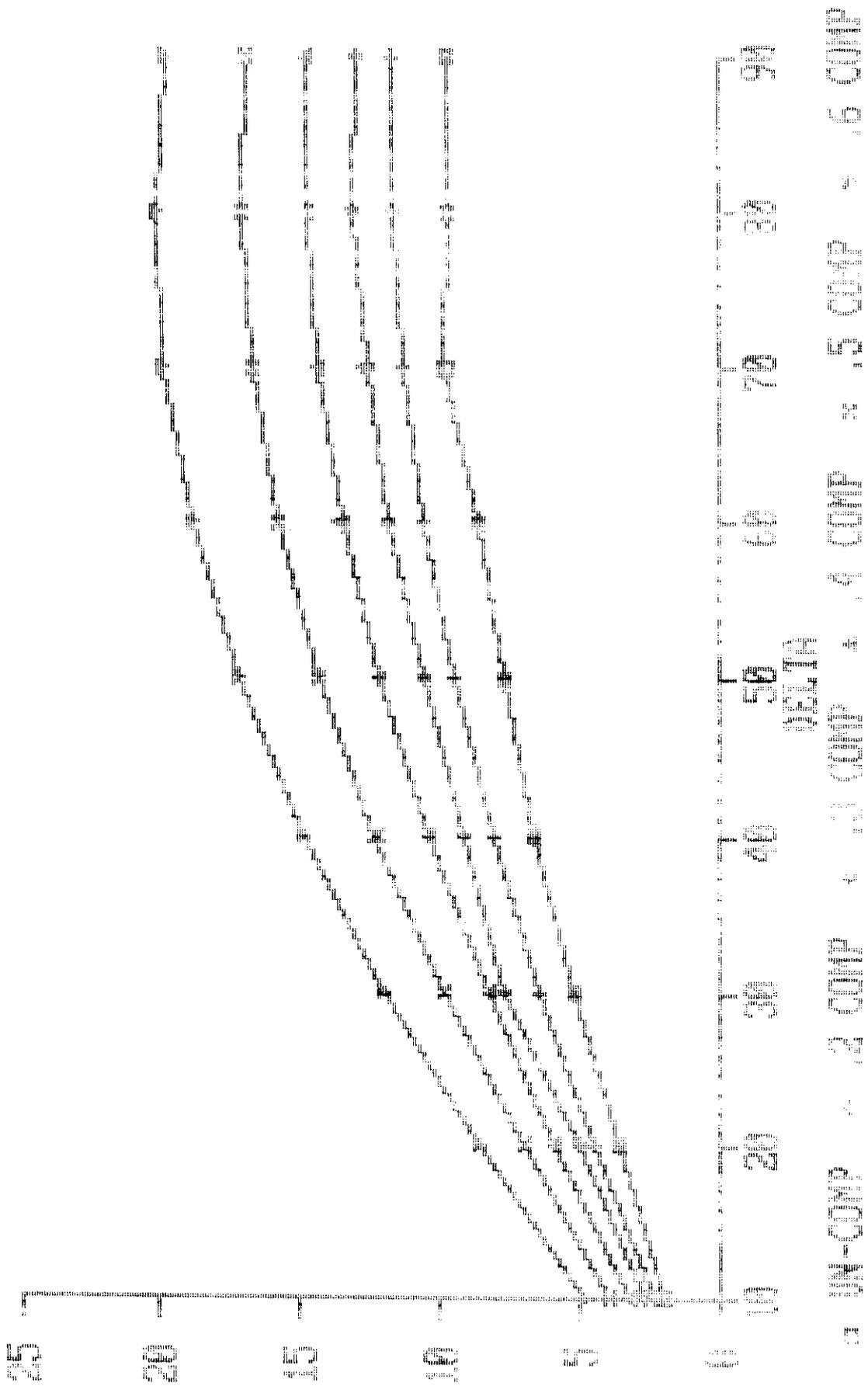
GRAPH NO. 5.10

7000
7000



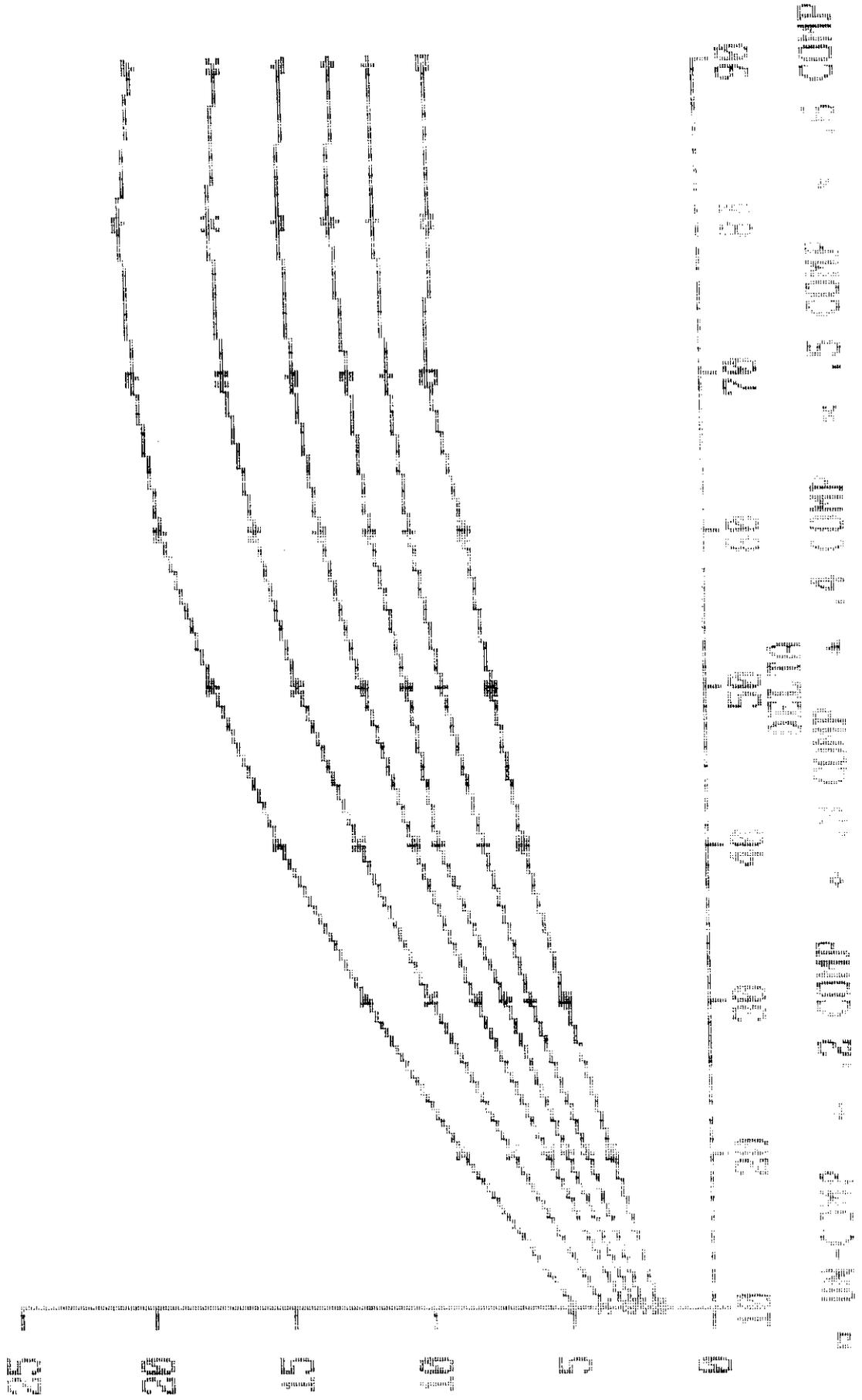
GRAPH NO. 5.11

RESULTS



GRAPH NO. 5.12

PR VS DELTA
FOR ONE-THIRD DISTANCE



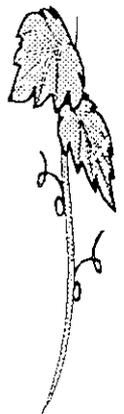
GRAPH NO. 5.13

**COMPARISON OF VARIOUS PARAMETERS
FOR DIFFERENT POSITIONS**

	SENDING END	RECEIVING END	CENTRE	BOTH ENDS	ONE-THIRD
PRMAX	LOWEST	LOWER	HIGHEST	HIGHER	HIGHEST
PR	LOWEST	HIGHEST	HIGHER	MODERATE	HIGHER
EFFICIENCY	HIGHEST	LOWEST	MODERATE	MODERATE	MODERATE
BM	LOWEST	LOWEST	HIGHEST	HIGHER	HIGHEST



SOFTWARE DEVELOPMENT



CHAPTER 6

DEVELOPMENT OF SOFTWARE

A software in FORTRAN 77 has been developed and various parameters are computed for the line data given in the section. The software also has the option of evaluating the various parameters for any line data input. The results obtained are tabulated.

The VPP package is used to draw the characteristic curves.

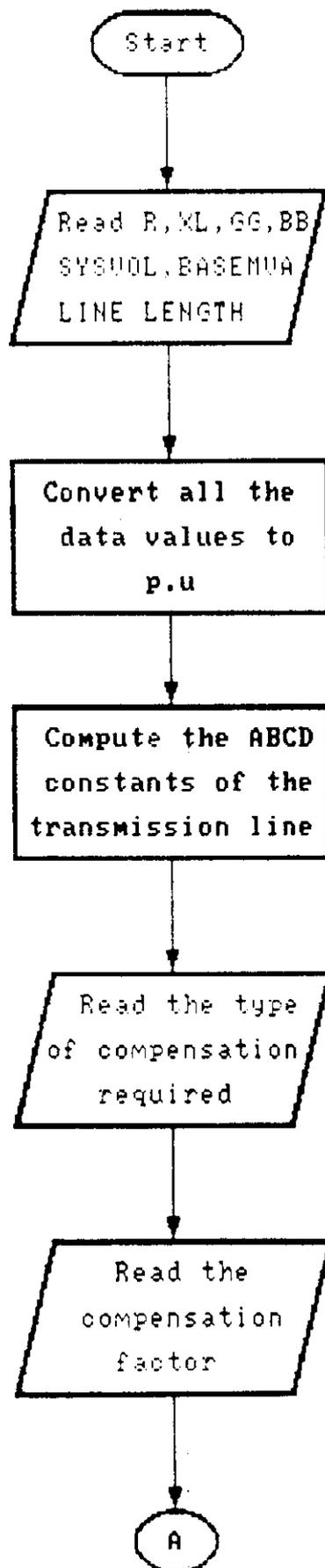
The flow chart in the section indicates the sequence of steps involved in computations.

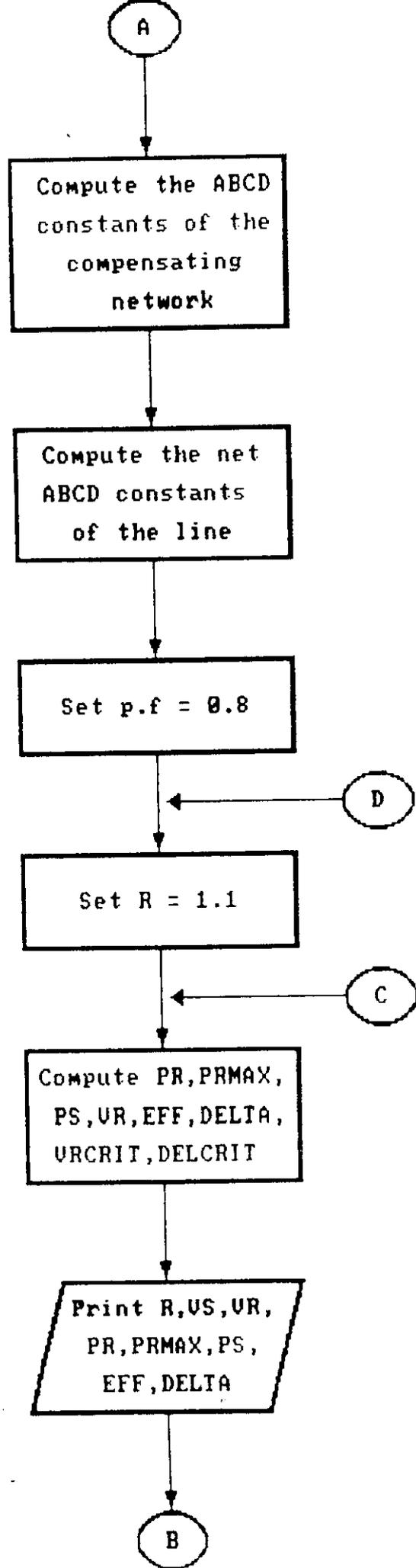
6.1. ALGORITHM

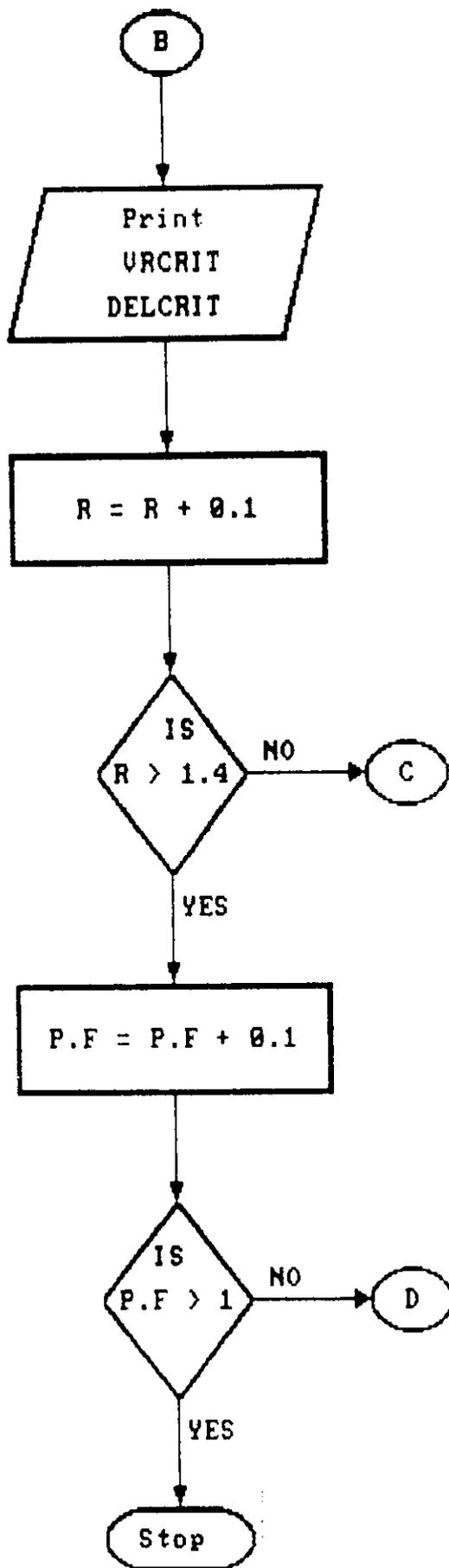
1. Read the values of resistance, inductance, line length, conductance, susceptance and system voltage of the transmission line.
2. Read the initial, increment and final values of R which is equal to V_S/V_R .
3. Convert all line values to P.U.
4. Compute the ABCD constants of the transmission line.
5. Read the type of compensation required and the compensating factor.

6. Compute the ABCD constants of the compensating network for the given compensating factor.
7. Compute the net ABCD constant of the series capacitor compensated line.
8. Compute the receiving end power P_R for different power factors of 0.8, 0.9 and 1.0.
9. Compute the maximum receiving end power $P_{R\text{ MAX}}$, efficiency, $V_{R\text{ CRIT}}$ and δ_{CRIT}
10. Print the values of P_R , $P_{R\text{ MAX}}$, B_0 , efficiency, $V_{R\text{ CRIT}}$ and δ_{CRIT}

6.2 FLOW CHART







```

C *****
C
C      COMPUTER AIDED ANALYSIS OF COMPENSATED EHV LINES
C
C *****
CHARACTER *1,CHOICE
INTEGER CAP
COMPLEX CMPLX,CSQRT
COMPLEX A,B,C,D,AS,BS,CS,DS,A0,B0,C0,D0
COMPLEX A01,B01,C01,D01,A02,B02,C02,D02,A03,B03,C03,D03
COMPLEX ABCD1,ZL,YL,ZC,YC,GMA
PRINT 101
101  FORMAT(12X,'*****  TITLE OF THE PROJECT  *****'/)
      WRITE(*,115)
      WRITE(*,102)
102  FORMAT(80('~'))
      PRINT 103
103  FORMAT(15X,'COMPUTER AIDED ANALYSIS OF COMPENSATED EHV LINES'/)
      WRITE(*,102)
      PRINT 104
104  FORMAT(30X,'carried out by')
      PRINT 105
105  FORMAT(/30X,'ASHOK KUMAR V.',
+      /30X,'PRASHANTH CHANDRAN.',
+      /30X,'RICHARD A.',
+      /30X,' ',
+      /35X,'at',

```

```

+ /30X,' ',
+ /15X,'CENTRAL POWER RESEARCH INSTITUTE,BANGALORE.',
+ /30X,' ',
+ /30X,'guided by',
+ /30X,' ',
+ /5X,'Guide at the Organisation',10X,'Guide at the College'
+ /5X,'MR. P. V. BALASUBRAMANYAM',10X,'MR. SIVA KUMAR',
+ /10X,' ',
+ /25X,'Head Of The Dept.',
+ /5X,'DR.K.A.PALANISWAMY, B.E., M.Sc.(Engg), Ph.D.',
+ ' M.I.S.T.E., C.Eng.(I), F.I.E'
+ /10X,' ',
+ /10X,' '/)

```

```

READ *,

```

```

PRINT *,'ASSUME STANDARD VALUES (Yes/No)'

```

```

READ *,CHOICE

```

```

IF (CHOICE .EQ. 'Y') GOTO 106

```

```

PRINT *,'ENTER THE VALUE OF SYSTEM VOLTAGE'

```

```

READ (*,*) SYSVOL

```

```

VS = SYSVOL

```

```

PRINT *,'ENTER THE TRANSMISSION LINE LENGTH'

```

```

READ (*,*) DL

```

```

PRINT *,'ENTER THE VALUES OF RL , XL , GG AND BB'

```

```

READ (*,*) RL,XL,GG,BB

```

```

PRINT *,'ENTER THE VALUE OF RINI , RINC AND RMAX'

```

```

READ (*,*) RINI,RINC,RMAX

```

```

PRINT *,'ENTER THE VALUES OF PFINI , PFINC AND PFMAX'

```

```

READ (*,*) PFINI,PFINC,PFMAX

GOTO 107

C   STANDARD VALUES
106  SYSVOL = 400.0

    DL = 400.0
    RL = 0.0274
    XL = 0.332
    GG = 0.0
    BB = 3.47E-06
    VS = SYSVOL
    RINI = 1.1
    RINC = 0.1
    RMAX = 2.0
    PFINI = 0.8
    PFINC = 0.1
    PFMAX = 1.0
107  WRITE(*,108) SYSVOL
108  FORMAT(20X,'SYSTEM VOLTAGE (KV) = ',F10.6)
    WRITE(*,109) DL
109  FORMAT(/20X,'TOTAL LENGTH OF THE LINE = ',F8.2)
    WRITE(*,110) RL,XL,GG,BB
110  FORMAT (/20X,'LINE RESISTANCE (OHMS/KM) = ',E14.7,
+       /20X,'LINE INDUCTIVE REACTANCE (OHMS/KM) = ',E14.7,
+       /20X,'GG = ',E14.7,/,20X,'BB = ',E14.7)
    WRITE(*,111) VS
111  FORMAT(/20X,'SENDING END VOLTAGE (KV) = ',F10.6/)
    WRITE(*,112) RINI,RINC,RMAX

```

```

112  FORMAT(/10X,'RINI = ',F10.6,5X,'RINC = ',F10.6,5X,'RMAX = ',F10.6)
      WRITE(*,130) PFINI,PFINC,PFMAX
130  FORMAT(/10X,'PFINI=',F10.6,5X,'PFINC=',F10.6,5X,'PFMAX=',F10.6)
C
      WRITE(*,116)
C
      BASMVA = 100.0
      WRITE(*,113) BASMVA
113  FORMAT(/30X,'BASEMVA = ',F10.4)
      BASIMP = (SYSVOL*SYSVOL)/BASMVA
      RL = RL/BASIMP
      XL = XL/BASIMP
      GG = GG*BASIMP
      BB = BB*BASIMP
      VS = VS/SYSVOL
      YL = CMPLX(GG,BB)
      ZL = CMPLX(RL,XL)
      ZC = CSQRT(ZL/YL)
      GMA = CSQRT(ZL*YL)
      YC = 1.0/ZC
      ZCM = CABS(ZC)
      DL1 = DL
C
      WRITE(*,114) ZC,GMA,ZCM
114  FORMAT(/10X,'CHARACTERISTIC IMPEDANCE = ',2E14.7,
+       /10X,'PROPOGATION CONSTANT = ',2E14.7
+       /10X,'MAGNITUDE OF SURGE IMPEDANCE = ',F10.6)

```

C

```
WRITE(*,115)
```

```
115 FORMAT(80(' '))
```

```
WRITE(*,116)
```

```
116 FORMAT(80('*'))
```

```
READ *,
```

```
117 FORMAT(80('-'))
```

C TYPES OF SERIES COMPENSATION

```
WRITE(*,118)
```

```
118 FORMAT(/12X,'SERIES CAPACITANCE AT THE SENDING END (1)',
```

```
+ /12X,'SERIES CAPACITANCE AT THE RECEIVING END (2)',
```

```
+ /12X,'SERIES CAPACITANCE IN THE MIDDLE (3)',
```

```
+ /12X,'SERIES CAPACITANCES AT BOTH THE ENDS (4)',
```

```
+ /12X,'SERIES CAPACITANCES AT ONE-THIRD DISTANCE FROM'
```

```
+ ' BOTH THE ENDS (5)',
```

```
+ /12X,'UNCOMPENSATED LINE (6)')
```

```
WRITE(*,116)
```

```
WRITE(*,119)
```

```
119 FORMAT(/12X,'ENTER THE TYPE OF COMPENSATION REQUIRED')
```

```
READ *,CAP
```

```
IF (CAP .EQ. 3) DL = DL/2
```

```
IF (CAP .EQ. 5) DL = DL/3
```

```
YY = DL
```

C

C CALCULATION OF ABCD PARAMETERS

```
CALL ABCD(GMA,YY,ZC,YC,A,B,C,D)
```

```
IF( CAP .EQ. 6) GOTO 7
```

```

C      COMPENSATION FACTOR
      WRITE(*,120)
120   FORMAT(/12X,'ENTER THE COMPENSATION FACTOR')
      READ *,COMP
      WRITE(*,117)
      AS = CMPLX (1.0,0.0)
      CS = CMPLX (0.0,0.0)
      DS = AS
      C1 = - COMP*XL*DL1
      IF (CAP .EQ. 4) C1= C1/2
      IF (CAP .EQ. 5) C1= C1/2
      BS = CMPLX (0.0,C1)
      GOTO (1,2,3,4,5),CAP
1     CALL MATMUL(AS,BS,CS,DS,A,B,C,D,A0,B0,C0,D0)
      GOTO 8
2     CALL MATMUL(A,B,C,D,AS,BS,CS,DS,A0,B0,C0,D0)
      GOTO 8
3     CALL MATMUL(A,B,C,D,AS,BS,CS,DS,A0,B0,C0,D0)
      CALL MATMUL(A0,B0,C0,D0,A,B,C,D,A01,B01,C01,D01)
      GOTO 6
4     CALL MATMUL(AS,BS,CS,DS,A,B,C,D,A0,B0,C0,D0)
      CALL MATMUL (A0,B0,C0,D0,AS,BS,CS,DS,A01,B01,C01,D01)
      GOTO 6
5     CALL MATMUL (A,B,C,D,AS,BS,CS,DS,A0,B0,C0,D0)
      CALL MATMUL (A0,B0,C0,D0,A,B,C,D,A01,B01,C01,D01)
      CALL MATMUL (A01,B01,C01,D01,AS,BS,CS,DS,A02,B02,C02,D02)
      CALL MATMUL (A02,B02,C02,D02,A,B,C,D,A03,B03,C03,D03)

```

```

A0 = A03
B0 = B03
C0 = C03
D0 = D03
GOTO 8
6  A0 = A01
   B0 = B01
   C0 = C01
   D0 = D01
   GOTO 8
7  A0 = A
   B0 = B
   C0 = C
   D0 = D
8  CALL MAG(A0,B0,C0,D0,AM,BM,CM,DM)
   CALL ANG(A0,B0,C0,D0,AN,BN,CN,DN)
   PRINT 121
121 FORMAT(30X,'ABCD PARAMETERS OF THE TOTAL LINE (PU)')
    WRITE(*,122)A,B,C,D
122 FORMAT(/20X,'A = ',2F10.6,5X,'B = ',2F10.6/,
+         20X,'C = ',2F10.6,5X,'D = ',2F10.6)
C
   WRITE(*,123) AM,BM,CM,DM
123 FORMAT (/20X,'AM=',F10.6,5X,'BM=',F10.6/,
+         20X,'CM=',F10.6,5X,'DM=',F10.6)
   WRITE(*,124) AN,BN,CN,DN
124 FORMAT(/20X,'AN=',F10.6,5X,'BN=',F10.6/,

```

```

+          20X,'CN=',F10.6,5X,'DN=',F10.6)
ABCDL=A*D-B*C
WRITE(*,125) ABCDL
125  FORMAT(50X,'ABCD=',2F10.6)
WRITE (*,117)
READ *,
PI = 22.0/7.0

C
C  INITIAL VALUE OF R (VS/VR RATIO)
C
R = RINI
PF = PFINI
C  -----

131  PRINT *, 'TABULATION FOR PF = ',PF
      PRINT *, ' R      VS      VR      DELTA      PR      PRMAX      PS      EFF
+ VRCRIT  DELCRIT'
      THETA = ACOS(PF)
      THE = THETA-BN+AN
126  THE1 = (AM/R)*SIN(THE)
      DELTA = BN-THETA+ASIN(THE1)
      PR = (1/(R*BM))*COS(BN-DELTA)-(AM/(BM*R*R))*COS(BN-AN)
      PS = (DM/BM)*COS(BN-AN)-(1/(R*BM))*COS(BN+DELTA)
      PRM = (1/(R*BM))-(AM/(BM*R*R))*COS(BN-AN)
      EFF = (PR/PS)*100
      VR = VS/R
      DELCRIT = ((AN+BN)-THETA)/2.0

```

```

VRCRIT = VS/(2.0*AM*COS(AN-DELCRIT))
WRITE(*,127) R,VS,VR,DELTA*57.3,PR,PRM,PS,EFF,
+VRCRIT,DELCRIT*57.3
127  FORMAT(1F4.2,2X,1F4.2,2X,1F4.2,2X,1F8.3,2X,1F6.3,2X,1F6.3,
+2X,1F6.3,2X,1F5.2,2X,1F4.2,2X,1F8.3)
R = R +RINC
IF (R .LE. RMAX) GOTO 126
R = RINI
PF = PF+PFINC
READ *,
IF (PF .LE. PFMAX) GOTO 131
C  VARIATION OF PR WITH DELTA
PRINT *, ' DELTA PR'
DEL1 =10
R = 1.2
345  PRDEL = (1/(R*BM))*COS(BN-DEL1/57.3)-(AM/(BM*R*R))*COS(BN-AN)
WRITE(*,489)DEL1,PRDEL
489  FORMAT(1F10.6,5X,1F6.3)
DEL1 = DEL1 + 10
IF (DEL1 .LE. 90) GOTO 345
STOP
END
SUBROUTINE ABCD(GMA,X,ZC,YC,A,B,C,D)
COMPLEX A,B,C,D,ZC,YC,GX,CMPLX,GMA
GX = GMA*X
ALPHA = REAL(GX)
BETA = AIMAG(GX)

```

```

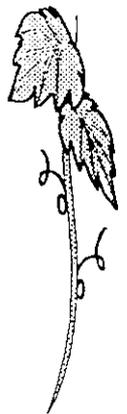
C1 = EXP(ALPHA)
C2 = 1.0/C1
SNH = (C1-C2)*0.5
CSH = (C1+C2)*0.5
A1 = CSH*COS(BETA)
A2 = SNH*SIN(BETA)
B1 = SNH*COS(BETA)
B2 = CSH*SIN(BETA)
A = CMPLX(A1,A2)
B = CMPLX(B1,B2)
C = YC*B
B = ZC*B
D = A
RETURN
END
SUBROUTINE MATMUL(A,B,C,D,E,F,G,H,P,Q,R,S)
COMPLEX A,B,C,D,E,F,G,H,P,Q,R,S,PL,QL,RL,SL
P = A*E+B*G
Q = A*F+B*H
R = C*E+D*G
S = C*F+D*H
RETURN
END
SUBROUTINE MAG(A0,B0,C0,D0,AM,BM,CM,DM)
COMPLEX A0,B0,C0,D0
AM = CABS(A0)
BM = CABS(B0)

```

```
CM = CABS(CO)
DM = CABS(DO)
RETURN
END
SUBROUTINE ANG(AO,BO,CO,DO,AN,BN,CN,DN)
COMPLEX AO,BO,CO,DO
REAL REAL,AIMAG,ATAN2
PI = 22.0/7.0
T1 = AIMAG(AO)
T2 = REAL(AO)
AN = ATAN2(T1,T2)
T1 = AIMAG(BO)
T2 = REAL(BO)
BN = ATAN2(T1,T2)
T1 = AIMAG(CO)
T2 = REAL(CO)
CN = ATAN2(T1,T2)
T1 = AIMAG(DO)
T2 = REAL(DO)
DN = ATAN2(T1,T2)
RETURN
END
```



**PROBLEMS IN SERIES
COMPENSATION**



CHAPTER 7

PROBLEMS ASSOCIATED WITH SERIES COMPENSATED TRANSMISSION LINE

The application of series capacitor for the transmission line has the following advantages.

- i. Increasing the power transfer capability.
- ii. Voltage and reactive power control.
- iii. Load sharing in parallel and loss minimization.

But series compensation is also associated with certain problems like dynamic system instability, switching over voltage, sub-synchronous oscillations, etc. In this chapter, an attempt is made to explain the problems and their analysis. Some preventive methods have also been suggested.

7.1. PROBLEMS IN THE APPLICATION OF SERIES CAPACITOR

7.1.1. The voltage drops across the capacitor results in the voltage to ground at the terminals of the capacitor being different. Thus there is a possibility of an over voltage on one side of the capacitor under certain conditions. This must be examined in detail at the planning stage. The over voltage can be overcome by connecting switched shunt reactors.

7.1.2. SSR Phenomena

The basic sub-synchronous electrical oscillation phenomena may be explained as follows.

For a generator connected to an infinite bus through a series compensated line, if the speed of the generator and its angular position relative to the infinite bus are constant, then the system will have a natural resonant frequency decided by the total effective inductance and capacitance of the system. As a result of any small system disturbance, the RLC circuit will ring down at its sub-synchronous resonant frequency, causing generator armature current. But at this sub-synchronous frequency the synchronous machine behaves as an induction generator with negative slip.

Therefore energy is fed into the RLC circuit at the synchronous frequency and hence will tend to sustain or amplify the sub-synchronous currents. Under certain unfavourable conditions, this action will cause sub-synchronous currents to grow to disruptive magnitudes throughout the transmission systems. The sub-synchronous currents flowing in the armature of the synchronous machine will give rise to a component of air gap torque. Components at frequencies equal to the system frequency plus or minus the sub-synchronous frequency may be large enough, especially when the torsional resonance frequency of the system is close enough to the frequency of the torque pulsation, to damage the turbine generator shafts.

7.2. EFFECT OF SSR ON POWER SYSTEMS

Though series capacitors have added new dimensions to the solutions of large power transfer associated with E.H.V. long lines, it also causes some problems as given below.

The sub-synchronous current flowing in the armature of the synchronous machine gives rise to a pulsating air gap torque. If the frequency of this torque is nearer to the natural frequency of the mechanical system, resonance will occur causing damage to the turbine shaft. SSR has become a subject of great concern, especially after the damage to the two generator shafts at Mohava generating station in Southern Nevada, U.S.A., on,

- i. December 9, 1970 and,
- ii. October 26, 1971.

The sub-synchronous frequency oscillation also possess a natural danger to the system stability, because a disturbance seems to inject more energy into the system by its induction generator action. If the net resistance of the system is negative, the induction generator action is amplified, thereby causing system instability.

At sub-synchronous frequency, the increased reactance of the series capacitor causes a proportionally high voltage to appear across the capacitor bank, leading to the possible incorrect capacitor gap flash over.

7.3. VARIOUS METHODS OF ANALYSIS OF SSR

The methods available in the frequency domain to simulate and analyse the phenomena of SSR are,

- i. ROUTH HURWITH stability criteria.
- ii. Frequency scanning technique and.
- iii. Eigen value analysis.

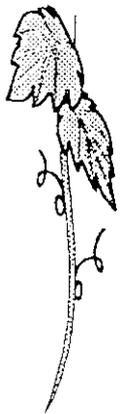
7.4. SSR PREVENTIVE METHODS

Prevention against SSR is normally provided by one of the following methods.

- i. Filtering and damping.
- ii. Relaying and protective devices.



CONCLUSION



CHAPTER 8

CONCLUSION

In this project the various types of compensating schemes are compared from the point of view of,

8.1. $P_{R \text{ MAX}}$

8.2. EFFICIENCY

8.3. B_0

The best method of compensation and location is also suggested.

8.1. $P_{R \text{ MAX}}$

The maximum value of $P_{R \text{ MAX}}$ is obtained when the series capacitor is located at the centre or one-third distance from both the ends of the transmission line. Hence from the economic point of view, it is advisable and preferable to have a single capacitor located at the centre.

8.2. EFFICIENCY

It is found that the efficiency is maximum for series capacitor located at the sending end and is slightly lower for centre, one-third and both the ends. As the

value of P_R is more for the centre, it is better to select the centre location of the series capacitor, for the best efficiency.

8.3. B_o

The value of $P_{R\text{ MAX}}$ is inversely proportional to $|B_o|$ of the line. Hence if the type of compensation to be employed from the point of view of $|B_o|$ is taken into consideration, the compensation scheme which gives maximum $P_{R\text{ MAX}}$ is preferred. Hence the centre location is preferred as it gets the least value of $|B_o|$.



REFERENCE



REFERENCE

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