



**B.E/B.TECH DEGREE EXAMINATIONS: NOV/DEC 2023**

(Regulation 2018)

Fifth Semester

**AUTOMOBILE ENGINEERING**

**U18AUI5204 & Finite Element Analysis**

**COURSE OUTCOMES**

- CO1:** Recognize the concepts of finite element method.  
**CO2:** Formulate finite element techniques for design problems.  
**CO3:** Devise equations in finite element analysis for 1D, 2D and 3D problems.  
**CO4:** Analyze and solve problems in heat transfer and structural problems.  
**CO5:** Familiarise a CAE software, to simulate engineering problems in heat transfer and structural mechanics.  
**CO6:** Apply finite element techniques for Non-Linear Analysis.

**Time: Three Hours**

**Maximum Marks: 100**

**Answer all the Questions:-**

**PART A (10 x 2 = 20 Marks)**

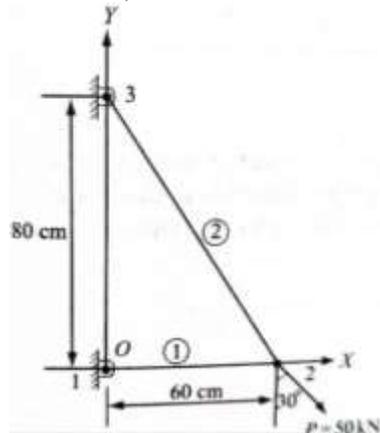
**(Answer not more than 40 words)**

1. Bring out the summary and the differences in Rayleigh-Ritz method and finite element method. CO1 [K<sub>1</sub>]
2. State and explain the principle of minimum potential energy. CO1 [K<sub>2</sub>]
3. Evaluate,  $\frac{du}{d\xi}$  for the one-dimensional element shown in Fig.1, if  $q_1 = 0.0762$  mm and  $q_2 = 0.127$  mm. CO2 [K<sub>2</sub>]



**Fig.1**

4. Find the stress corresponding to element 1 for the given loading condition for the truss shown in Fig.2 ( $q_3 = -0.032$  cm and  $q_4 = -0.507$  cm) CO2 [K<sub>2</sub>]



**Fig.2**

- |     |   |     |                   |
|-----|---|-----|-------------------|
| 5.  | State the necessary conditions to be satisfied in order to use axisymmetric elements                            | CO3 | [K <sub>1</sub> ] |
| 6.  | Compare the characteristics of CST and LST element.   | CO3 | [K <sub>2</sub> ] |
| 7.  | Describe the boundary conditions that will be considered in steady-state one dimensional heat transfer analysis | CO4 | [K <sub>2</sub> ] |
| 8.  | What is meant by an isoparametric element? Give an example  | CO4 | [K <sub>1</sub> ] |
| 9.  | Enumerate the difference between consistent and lumped mass matrix.   | CO5 | [K <sub>1</sub> ] |
| 10. | What are the methods used to treat material non linear problems in FEA?   | CO6 | [K <sub>1</sub> ] |

**Answer any FIVE Questions:-**  
**PART B (5 x 16 = 80 Marks)**  
**(Answer not more than 400 words)**

- |     |    |   |   |     |                   |
|-----|----|---|---|-----|-------------------|
| 11. | a) | The differential equation of a physical phenomenon is given by, | 8 | CO1 | [K <sub>3</sub> ] |
|-----|----|---|---|-----|-------------------|

$$\frac{d^2y}{dx^2} + 500x^2 = 0 \quad 0 \leq x \leq 1$$

Trail function,  $y = a_1 (x - x^4)$

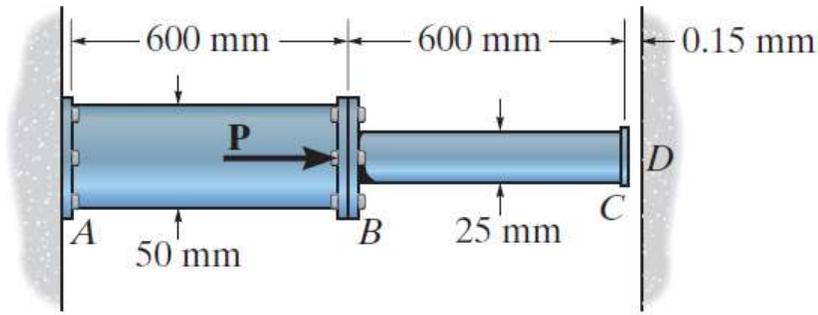
Boundary conditions are,  $y(0) = 0$  ,  $y(1) = 0$

Calculate the value of the parameter  $a_1$  by using

(i).Point collocation method

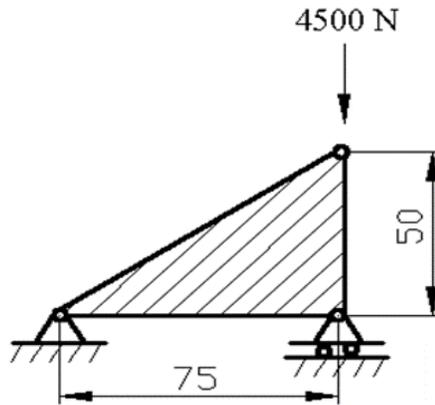
(ii).Subdomain collocation method.

- |     |    |  |    |     |                   |
|-----|----|--|----|-----|-------------------|
| 11. | b) | Briefly explain various steps in solving a finite element problem involving structural applications.   | 8  | CO1 | [K <sub>2</sub> ] |
| 12. | a) | The assembly shown in Fig.3 is made of solid A-36 steel cylinders whose Young's modulus is 200 GPa. If the gap between C and the rigid wall at D is initially 0.15 mm, determine the deflections at the nodal points and the element stresses when the force $P = 200$ kN is applied at B. | 16 | CO2 | [K <sub>4</sub> ] |



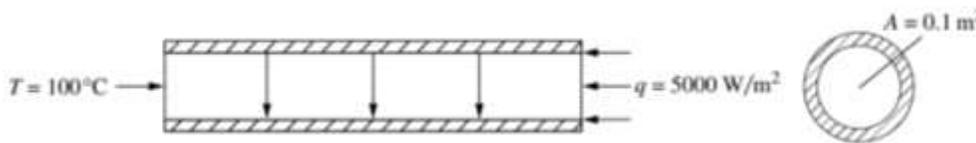
**Fig.3**

13. a) For the two-dimensional loaded plate shown in Fig.4, determine the nodal displacements using plane stress conditions. Body force may be neglected. Take thickness as 7 mm and Young's modulus as 200 GPa



**Fig.4**

14. a) The fin shown in Fig.5 is insulated on the perimeter. The left end has a constant temperature of  $100^{\circ}\text{C}$ . A positive heat flux of  $q = 5000 \text{ W/m}^2$  acts on the right end. Let  $K_{xx} = 6 \text{ W/(m}\cdot^{\circ}\text{C)}$  and cross-sectional area  $A = 0.1 \text{ m}^2$ . Determine the temperatures at  $L/4$ ,  $L/2$ ,  $3L/4$ , and  $L$ , where  $L = 0.4 \text{ m}$ .



**Fig.5**

15. a) Derive the shape function for a noded quadrilateral element

- b) Using one and two Gauss-point numerical integration formulae, evaluate the following integral: 8 CO5 [K4]

$$I = \int_3^5 \frac{1}{x} dx$$

Compare the results with the exact integration and trapezoidal rule.

16. a) Explain the different types of nonlinearities encountered in structural analysis. 16 CO6 [K2]

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