

B.E/B.TECH DEGREE EXAMINATIONS: NOV/DEC 2024

(Regulation 2018)

Fourth Semester

COMMON TO BT /FT /TXT

U18MAT4102: Numerical Methods

COURSE OUTCOMES

- CO1: Solve a set of algebraic equations representing steady state models formed in engineering problems.
- CO2: Fit smooth curves for the discrete data connected to each other or to use interpolation methods over these data tables.
- CO3: Find the trend information from discrete data set through numerical differentiation.
- CO4: Estimate integrals from discrete data through numerical methods.
- CO5: Predict the system dynamic behaviour through solution of ODEs modeling the system.
- CO6: Solve PDE models representing spatial and temporal variations in physical systems through numerical methods.

Time: Three Hours**Maximum Marks: 100****Answer all the Questions:-****PART A (10 x 2 = 20 Marks)****(Answer not more than 40 words)**

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|-----|---|-----|-------------------|
| 1. | What is the condition for the convergence to solve $\cos x = 3x - 1$ by iteration method. | CO1 | [K ₂] |
| 2. | Solve the linear system $4x - 3y = 11$, $3x + 2y = 4$ by Gauss Jordan method. | CO1 | [K ₃] |
| 3. | Write the normal equations to fit a second degree curve to a given data | CO2 | [K ₂] |
| 4. | Write the Lagrangian Inverse Interpolation formula for values | CO2 | [K ₂] |
| 5. | Write the Newton's forward difference formula for first and second derivative at $x=x_0$. | CO3 | [K ₂] |
| 6. | Form the divided difference table | CO3 | [K ₃] |
| 7. | $\left[\begin{array}{cccc} x: & 1 & 2 & 7 & 8 \\ y: & 1 & 5 & 5 & 4 \end{array} \right]$ Evaluate using trapezoidal rule | CO4 | [K ₃] |
| 8. | Evaluate by using Simpson's one-third rule | CO4 | [K ₃] |
| 9. | Apply fourth order Runge-Kutta method to find k_1, k_2 given | CO5 | [K ₃] |
| 10. | Write down the formula for one dimensional heat equation by Crank – Nicholson difference method | CO6 | [K ₂] |

Answer any FIVE Questions:-
PART B (5 x 16 = 80 Marks)
(Answer not more than 400 words)

11. a) Obtain the largest eigen value and the corresponding eigen vectors of the matrix 8 CO1 [K4]
starting the initial vector by using power method.

b) Using Gauss elimination method find the solution of linear system 8 CO1 [K4]
by Gauss elimination method

12. a) Fit a straight line to the data given below. 8 CO2 [K4]
: 0 1 2 3 4
: 1 1.8 3.3 4.5 6.3
Also estimate the value of at

b) From the following table, estimate the number of students who obtained marks 8 CO2 [K4]
between 40 and 45

Marks	30-40	40-50	50-60	60-70	70-80
No. of students	31	42	51	35	31

13. a) Find the first two derivatives of at x = 50 and x = 56 from the table: 10 CO3 [K4]

x	50	51	52	53	54	55	56
	3.6840	3.7084	3.7325	3.7563	3.7798	3.8030	3.8259

b) Evaluate , using trapezoidal rule. 6 CO4 [K4]

14. a) Given $y^1=1-y$, $y(0) = 0$. 16 CO5 [K4]
i) Find $y(0.1)$ by Taylor series method.
ii) Find $y(0.2)$ by Euler's method.
iii) Find $y(0.3)$ by Improved Euler's method.
iv) Find $y(0.4)$ by Milne's method.

15. a) Solve _____ subject to _____ with _____
 $h=0.2$ using Bender Schmidt method. 8 CO6 [K4]
- b) Solve the following equation taking $h=1$ and upto one half of the period of the oscillation _____, 8 CO6 [K4]
16. a) Find the root between 1 and 2 of _____ by Newton-Raphson method correct to three decimal places. 8 CO1 [K4]
- b) Solve _____ correct to two decimal places, at the nodal points of the following square grid, using the boundary values indicated. 8 CO6 [K4]
