

B.E/B.TECH DEGREE EXAMINATIONS: NOV/DEC 2024

(Regulation 2018)

Sixth Semester

MECHANICAL ENGINEERING

U18MEI6203: Finite Element Analysis

COURSE OUTCOMES

- CO1:** Solve problems by applying standard finite element techniques
- CO2:** Analyze 1-D finite elements and to build the stiffness matrix
- CO3:** Examine 2-D finite element continuum for structural applications
- CO4:** Solve 1-D and 2-D heat transfer problems using finite element approach.
- CO5:** Apply axisymmetric formulation for specific applications.
- CO6:** Make use of finite element principles in iso-parametric applications

Time: Three Hours**Maximum Marks: 100**

Answer all the Questions: -
PART A (10 x 2 = 20 Marks)
(Answer not more than 40 words)

- | | | | |
|----|--|-----|-------------------|
| 1 | State the three phases of finite element method. | CO1 | [K ₂] |
| 2 | List out the advantages of finite element method over other numerical analysis method. | CO1 | [K ₂] |
| 3 | What is the need for developing the overall stiffness matrix of the entire structure in terms of its global coordinate system? Give example | CO2 | [K ₃] |
| 4 | What are the h and p versions of finite element method? | CO2 | [K ₃] |
| 5 | Write down the nodal displacement equation for a two dimensional triangular elasticity element? | CO3 | [K ₃] |
| 6 | State whether plane stress or plane strain elements can be used to model the following structures with reasons. a. A wall subjected to wind load b. A wrench subjected to a force in the plane of the wrench | CO3 | [K ₃] |
| 7 | Write the conduction, free end convection and thermal load matrices for 1D heat transfer through a fin | CO4 | [K ₂] |
| 8 | Give four examples of practical applications of axisymmetric applications | CO5 | [K ₂] |
| 9 | When isoperimetric elements are used? | CO6 | [K ₂] |
| 10 | Write down the shape functions for 4 noded rectangular elements using natural coordinate system | CO6 | [K ₂] |

Answer any FIVE Questions:-
PART B (5 x 16 = 80 Marks)
(Answer not more than 400 words)

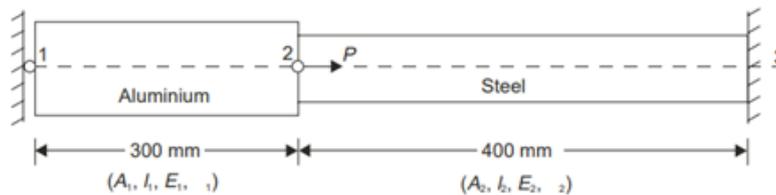
11. a) For the differential equation: $d/dx [(1+x) dy/dx] = 0$ for $0 < x < 1$ with the boundary conditions: $y(0) = 0$ and $y(1) = 1$, obtain a two parameter Ritz approximation for the solution using Rayleigh-Ritz method 10 CO1 [K₂]
- b) State the different types of analysis that can be carried out using finite element analysis. Explain anyone of them briefly. 06 CO1 [K₂]

12. Consider a bar as shown in Fig. An axial load of $P=200$ kN is applied at point 2. Consider the following data. 16 CO2 [K₃]

$A_1 = 2400 \text{ mm}^2$. $A_2 = 600 \text{ mm}^2$
 $E_1 = 70 \times 10^9 \text{ N/m}^2$. $E_2 = 200 \times 10^9 \text{ N/m}^2$

Determine the following:

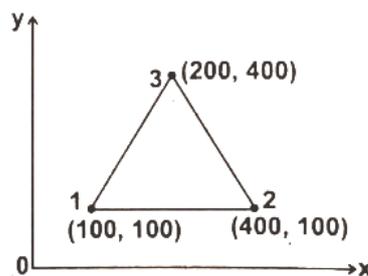
- (a) Nodal displacements at node 2,
 (b) Stresses in each material



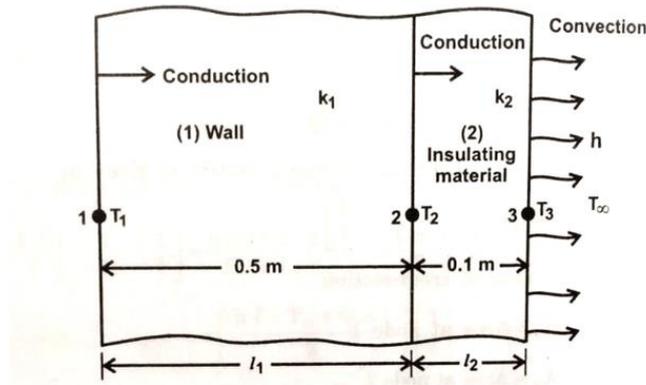
13. For the plane stress element shown in figure. The nodal displacements are 16 CO3 [K₃]

$u_1=2$ mm, $v_1=1$ mm,
 $u_2= 1$ mm, $v_2=1.5$ mm,
 $u_3= 2.5$ mm, $v_3=0.5$ mm.

Determine the element stresses. Assume $E = 200 \text{ GN/m}^2$: $\mu = 0.3$ and $t = 10$ mm. All coordinates are in millimeters.

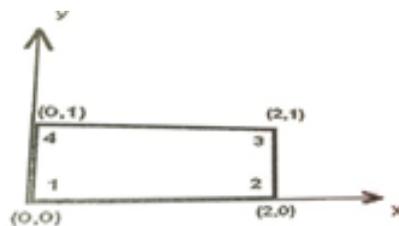


14. a) A wall of 0.5 m thickness having thermal conductivity of 6 W/mk. The wall is to be insulated with a material of thickness 0.1 m having an average thermal conductivity of 0.3 W/mk. The inner surface temperature is 1200°C and outside of the insulation is exposed to atmospheric air at 30°C with heat transfer co-efficient of 40 W/m² k. Calculate the nodal temperature.



- b) What are the different types of elements? Explain the significance of each.
15. a) Evaluate the strain-displacement matrix for the axisymmetric element as shown in figure. Take $E = 2.1 \times 10^5 \text{ N/mm}^2$, $\nu = 0.25$. The coordinates are in mm .

- b) Distinguish plane stress and plane strain analysis with suitable examples.
16. a) For the four noded element shown in figure, determine the Jacobian matrix and evaluate its value at the point (0,0).



- b) Evaluate by applying 3 point Gaussian quadrature and compare with the exact solution.
